

$B^0 \rightarrow \eta' (\rightarrow \eta\pi^+\pi^-) K_S^0$ Time Dependent \mathcal{CP} sensitivity study for BelleII

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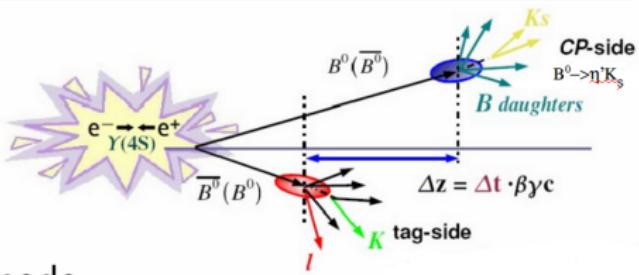
INFN Padova

B2GM,
Tsukuba, 21 June 2016

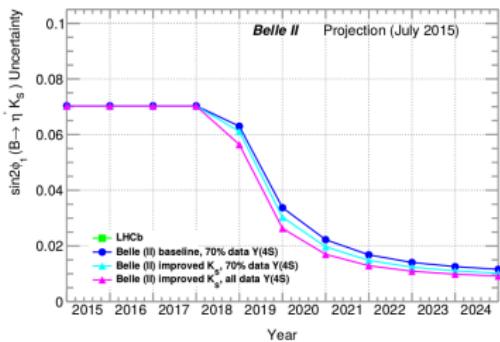
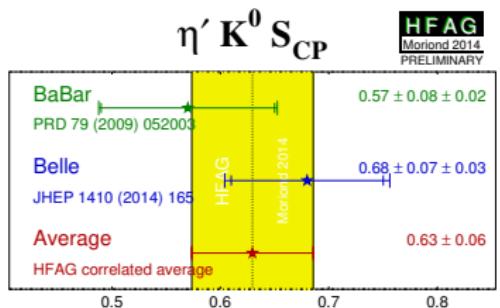
A sensitivity study for Time-Dependent CP violation analysis in the $B^0 \rightarrow \eta' K^0$ channel, a charmless $b \rightarrow s q \bar{q}$ decay

CP asymmetry from time-dependent decay rate into CP eigenstates;

- $B^0 \rightarrow \eta' K^0$ is a penguin dominated mode
- Precision not competitive with that from golden channel $B^0 \rightarrow J/\psi \phi$
- $S_{\eta' K^0} = \sin 2\phi_1^{eff}$ tightly related to $\sin 2\phi_1$ measured in $b \rightarrow c s \bar{s}$ decay
- identical if only penguin diagram were present: not so;
 - ▶ QCD factorization: $\Delta S_{\eta' K^0} \in [-0.03, 0.03]$ [Williamson and Zupan(2006)]
 - ▶ $SU(3)_F$ approach: $\Delta S_{\eta' K^0} \in [-0.05, 0.09]$ [Gronau et al.(2006)]
 - ▶ new physics can enter in the loop, shifting $\Delta S_{\eta' K^0}$ more than SM expectation



- Channel have been analyzed in B-factory [BABAR(2009), Belle(2007), Belle(2014)];
- analysis based on quasi-two body approach;
- $\sin 2\phi_1^{\text{eff}} = +0.68 \pm 0.07 \pm 0.03$ [Belle(2014)] = $+0.57 \pm 0.08 \pm 0.02$ [BABAR(2009)]
- uncertainties are mostly statistical (~ 3500 events for all final states);
 - syst: ± 0.025 from Δt resolution, ± 0.014 from vertexing, ± 0.013 from $\eta' K_S^0$ fraction;



- projected for 50 ab^{-1} $\sigma_{\text{stat}} = 0.008$, $\sigma_{\text{syst}} = 0.008$ [Urquijo(2015)]
- no competition from LHCb

many decay channels available $B^0 \rightarrow \eta' K^0$

decay channel		
$\eta' \rightarrow \rho^0 (\rightarrow \pi^+ \pi^-) \gamma$	BR=29%	not yet
$\eta' \rightarrow \eta \pi^+ \pi^-$	43%	today
$\searrow \eta \rightarrow \gamma\gamma$ $\searrow \eta \rightarrow \pi^+ \pi^- \pi^0$	40% 23%	$\eta_{\gamma\gamma}$ $\eta_{3\pi}$
$K_S^0 \rightarrow \pi^+ \pi^-$	69%	today
$K_S^0 \rightarrow \pi^0 \pi^0$	31%	just started
K_L^0		not yet
$B_0 \rightarrow \eta' (\rightarrow \eta_{\gamma\gamma} / \eta_{3\pi} \pi^+ \pi^-) K_S^0 (\rightarrow \pi^+ \pi^-)$	BR=19%	

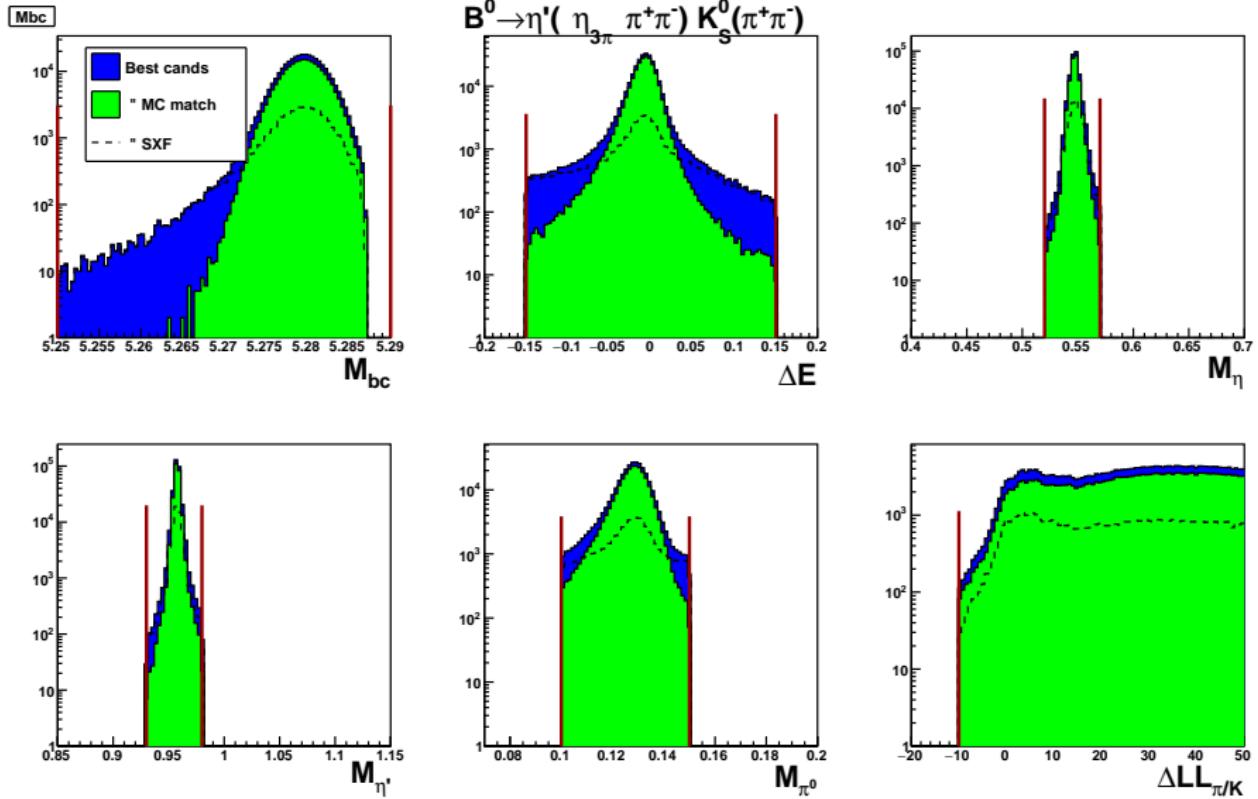
- Complex final state, neutrals, large combinatorics;
- **final states considered so far in red**
- more to be studied ($\rho^0, K_S^0 \rightarrow \pi^0 \pi^0, K_L^0$)

candidate selection: main cuts

- Reconstruct decay chain with mass constrains for π^0 , η , η' , K_S^0 ,
 - ▶ vertex only (w/o mass) for B^0 (more later)
 - π^0 , $\eta_{\gamma\gamma}$:
 - ▶ $0.06 < E_\gamma < 6 \text{ GeV}$, $E_9/E_{25} > 0.75$
 - ▶ $M(\pi^0) \in [100, 150] \text{ MeV}$
 - ▶ $M(\eta_{\gamma\gamma}) \in [0.52, 0.57] \text{ GeV}$;
 - $\eta' \rightarrow \eta_{\gamma\gamma}\pi^+\pi^-$:
 - ▶ $d_0(\pi^\pm) < 0.08 \text{ mm}$;
 $z_0(\pi^\pm) < 0.1 \text{ mm}$;
 - ▶ $N \text{ hits}_{PXD}(\pi^\pm) > 1$, PID
 - ▶ $M(\eta') \in [0.93, 0.98] \text{ GeV}$;
 - $\eta' \rightarrow \eta_{3\pi}\pi^+\pi^-$:
 - ▶ $M(\eta') \in [0.93, 0.98] \text{ GeV}$;
 - $K^0 \rightarrow \pi^+\pi^-$:
 - ▶ $M(K_S^0 \rightarrow \pi^+\pi^-) \in [0.48, 0.52] \text{ GeV}$;
 - $B^0 \rightarrow \eta' (\rightarrow \eta_{\gamma\gamma}\pi^+\pi^-) K_S^{0+-}$
 - ▶ $M_{bc} > 5.25 \text{ GeV}$;
 - ▶ $|\Delta E| < 0.1 \text{ GeV}$;
 - $B^0 \rightarrow \eta' (\rightarrow \eta_{3\pi}\pi^+\pi^-) K_S^{0+-}$
 - ▶ $|\Delta E| < 0.15 \text{ GeV}$;

if $N_{cands} > 1$, select that with best reduced χ^2 for η, η', K_S^0 inv. masses

Best candidates, after selections

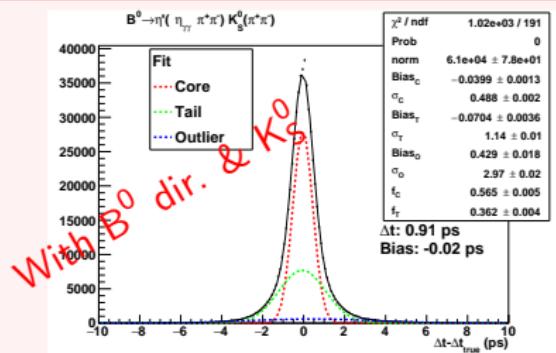
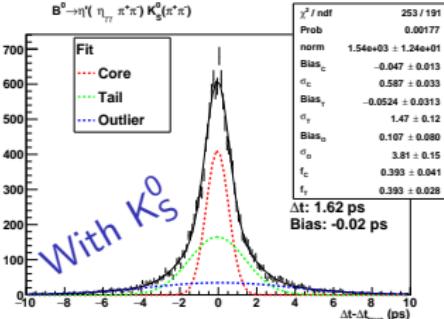
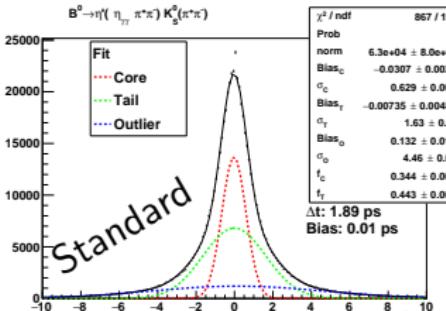


channel	ϵ %	SxF %	cands/ev
$B^0 \rightarrow \eta'(\rightarrow \eta_{\gamma\gamma} \pi^+ \pi^-) K_S^0 (\rightarrow \pi^+ \pi^-)$	29.4	1.1	1.06
$B^0 \rightarrow \eta'(\rightarrow \eta_{3\pi} \pi^+ \pi^-) K_S^0 (\rightarrow \pi^+ \pi^-)$	12.1	3.1	1.45
$B^0 \rightarrow \eta'(\rightarrow \eta_{\gamma\gamma} \pi^+ \pi^-) K_S^0 (\rightarrow \pi^0 \pi^0)$	13.5	2.2	~ 5
$B^0 \rightarrow \eta'(\rightarrow \eta_{3\pi} \pi^+ \pi^-) K_S^0 (\rightarrow \pi^0 \pi^0)$	6.0	3.8	~ 30

- Efficiency drop due to π^0 reco, likely to improve;
- presence of π^0 increase also combinatorics and signal cross feed
SxF : signal event but with wrong particle association;
- $B^0 \rightarrow \eta'(\rightarrow \eta_{3\pi} \pi^+ \pi^-) K_S^0 (\rightarrow \pi^0 \pi^0)$ not used in Belle and BaBar analysis.

Vtx reco and Δt resolution: $\eta_{\gamma\gamma}$ channel

- ➊ Fit the B_0 vertex from charged tracks; (π^\pm from $\eta' \rightarrow \eta\pi^\pm$)
- ➋ add also constraint from reconstructed K_S^0 direction; ($K_S^0 \rightarrow \pi^+\pi^-$)
- ➌ add also constraint from B^0 boost direction, transverse plane only.



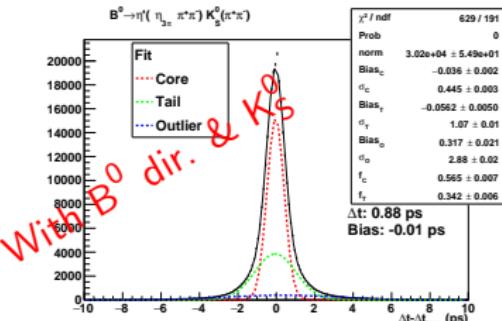
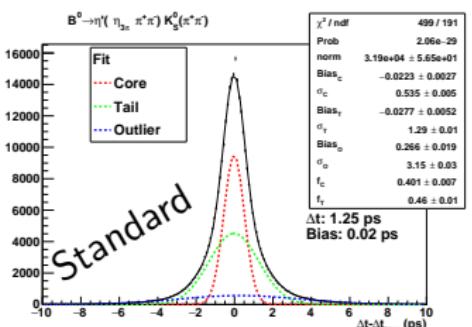
With beamspot (x, y) & K_S^0 :

No efficiency loss
important improvement in Δt resolution

$1.89 \rightarrow 1.62 \rightarrow 0.91 \text{ ps}$

Standard reconstruction uses four charged tracks:

π^\pm from $\eta' \rightarrow \eta\pi^\pm$ and $\eta \rightarrow \pi^\pm\pi^0$



With B^0 dir. & K_S^0 :

No efficiency loss

$1.25 \rightarrow 0.88 \text{ ps}$

In both cases, Δt resolution better than in Belle, in spite of lower boost

Backgrounds

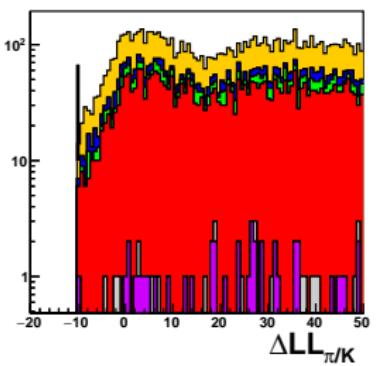
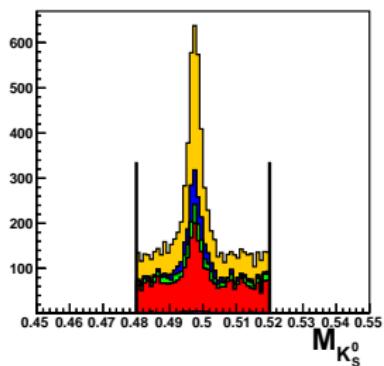
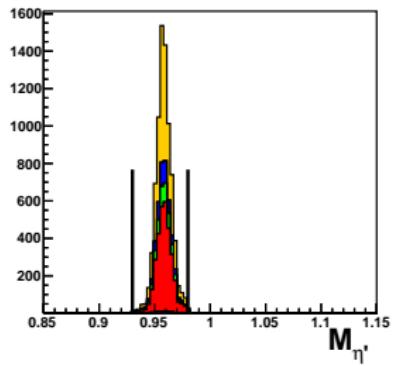
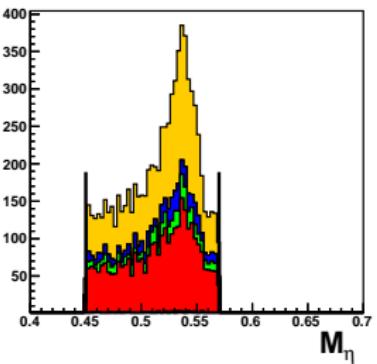
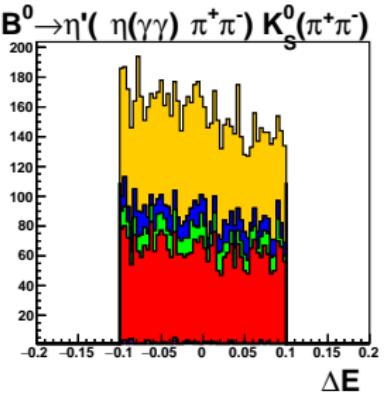
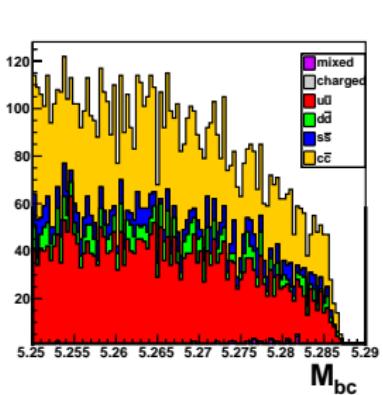
- **Combinatorial:** from continuum background $e^+e^- \rightarrow u\bar{u}, d\bar{d}, s\bar{s}, c\bar{c}$
 - ▶ evaluated from M_{bc} side bands on real data
 - ▶ now from MC production: **NB: still w/o machine background!**
 - ▶ use **Continuum Suppression variable**
 - ★ multivariate variables sensitive to event topology
 - ★ central (signal) vs jet-like (continuum)
 - ★ past issues w/ variables “fixed”
- **Peaking:** any other B decays possibly with real η' and/or K_S^0
 - ▶ evaluated from MC of generic $B^0\bar{B}^0, B^+\bar{B}^-$
 - ★ actual $B^0 \rightarrow \eta' K^0$ removed.
- Current results based on BGx0 production, namely w/o machine background
 - ▶ impact of machine background under study
 - ▶ signal w/ machine background already produced
- Next table numbers before Continuum Suppression cut

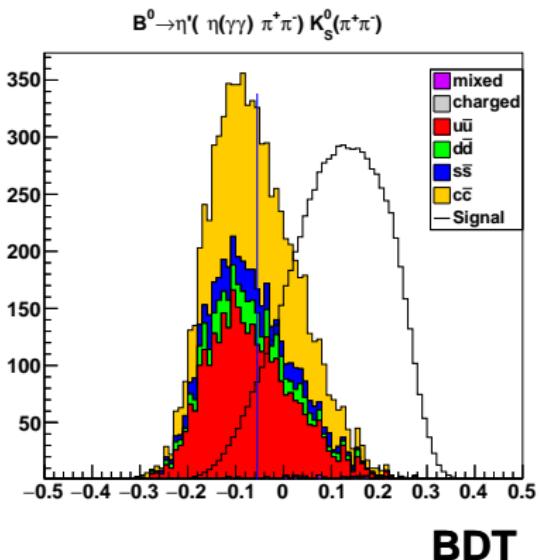
Sample	$u\bar{u}$	$d\bar{d}$	$s\bar{s}$	$c\bar{c}$	continuum	$B^0\bar{B}^0$	B^+B^-
Input ev (M)	1284	321	306	1063	2974	2160	2070
$B^0 \rightarrow \eta' (\rightarrow \eta_{\gamma\gamma} \pi^+ \pi^-) K_S^0 \pi^+$							
$\epsilon_{sel} (\cdot 10^{-6})$	2.69	3.06	2.40	3.62	3.0	0.11	0.038
ev for 300 fb^{-1}	1247	369	275	1445	3335	13	6
$B^0 \rightarrow \eta' (\rightarrow \eta_{3\pi} \pi^+ \pi^-) K_S^0 \pi^+$							
$\epsilon_{sel} (\cdot 10^{-6})$	0.34	0.54	0.17	1.50	0.76	0.14	0.02
ev for 300 fb^{-1}	166	65	20	597	847	24	3

- Background reduction better for $\eta_{3\pi}$ than for $\eta_{\gamma\gamma}$
 - $\eta_{\gamma\gamma}$ mostly $u\bar{u}$ and $c\bar{c}$
 - $\eta_{3\pi}$ mostly $c\bar{c}$
- peaking background is small
 - ▶ analyzed whole 5 ab^{-1} dataset from MC5
- preliminary study on w/ machine background shows similar rates

Background distributions

Best candidates, after selections





Working point

- **Tight:** $BDT > 0.124$, $\epsilon_{signal} = 50\%$, $(1 - \epsilon_{background}) = 97.5\%$,
- **Loose:** $BDT > -0.055$, $\epsilon_{signal} = 95\%$, $(1 - \epsilon_{background}) = 58\%$,
- **no cut:** include the BDT in the likelihood

Multi dim. extended maximum likelihood fit to extract **S** and **C**.

Pdf is of the form:

$$\mathcal{P}_j^i = \underbrace{\mathcal{T}_j\left(\Delta t^i, \sigma_{\Delta t}^i, \eta_{CP}^i\right)}_{\text{time-dep part}} \prod_k \underbrace{\mathcal{Q}_{k,j}(x_k^i)}_{\text{time integrated}}$$

time-dependent part, taking into account mistag rate ($\eta_f = \pm 1$ is CP state):

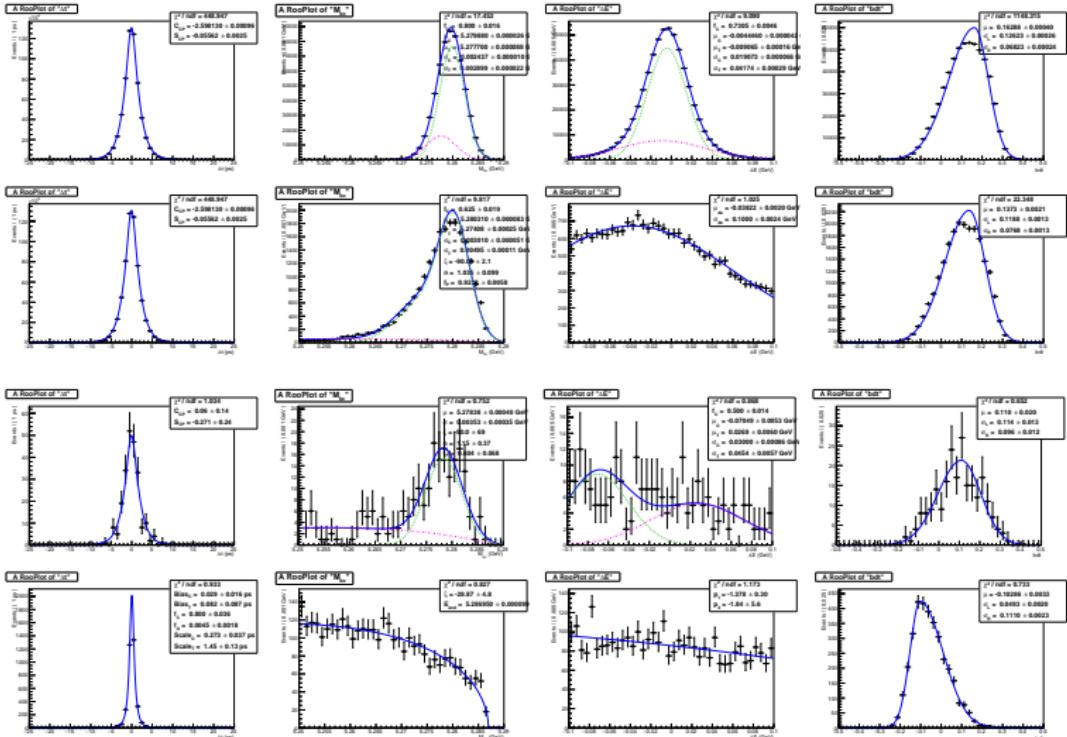
$$f(\Delta t) = \frac{e^{-|\Delta t|/\tau}}{4\tau} \left\{ 1 \mp \Delta w \pm (1 - 2w) \times [-\eta_f S_f \sin(\Delta m \Delta t) - C_f \cos(\Delta m \Delta t)] \right\}$$

Parameters:

variables (x_k) used, in addition to Δt

- effective tagging efficiency:
 $Q = \epsilon(1 - 2w)^2 = 0.33$
 - ▶ $w = 0.21$, $\Delta w = 0.02$
 - Δt resolution as shown previously
(convoluted)
 - τ , Δm from PDG
- M_{bc}
 - ΔE
 - Cont. Suppr.

PDF fit results examples



ΔT

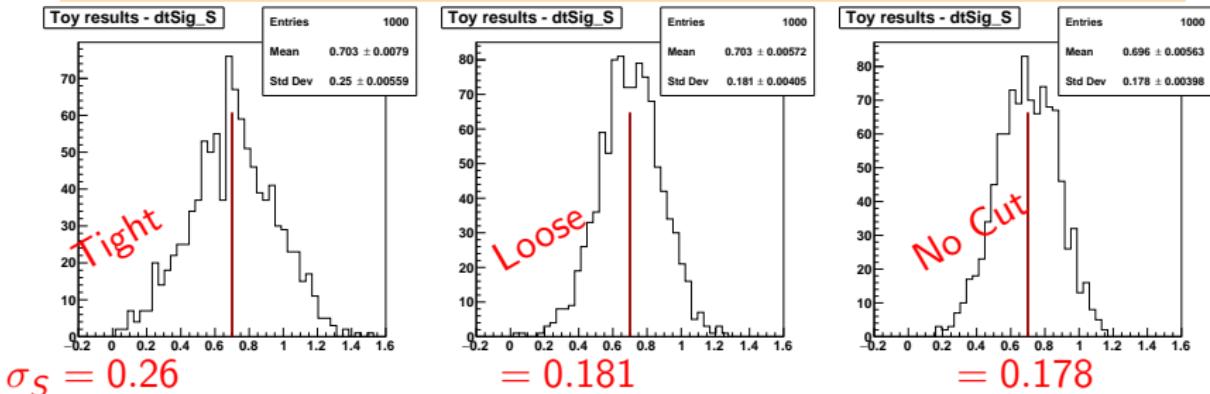
M_{bc}

ΔE

CS variable

- Testing fit machinery with Toy MC;
- Yield estimated for $L = 300 \text{ fb}^{-1}$: $N(B\bar{B}) \sim 330 \cdot 10^6$
 - ▶ width of distribution related to the expected statistical uncertainty;
 - ▶ check also for bias;
 - ▶ input CP asymmetry parameter: $S=0.7$ $C=0.0$
 - ▶ testing two different CS scenarios:
 - ★ Tight
 - ★ Loose
 - ★ No cut
 - ▶ Partially embedded toys
 - ★ Signal and SXF from MC;
 - ★ Continuum and Peaking background from pdf;

$L = 300 \text{ fb}^{-1}$: $N_{sig} = 390$, $N_{sxf} = 15$, $N_{cont} = 3300$, $N_{peak} = 30$



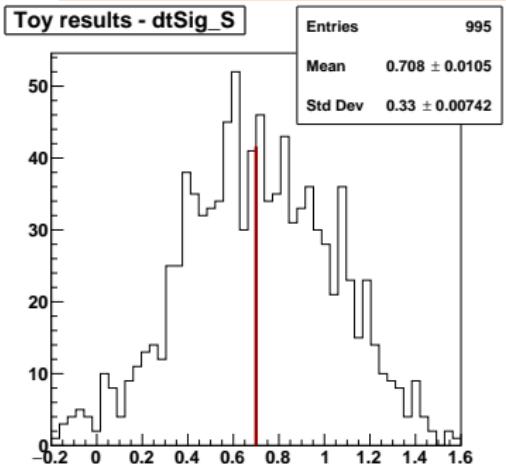
Preliminary results

Par	Bias	RMS
S (0.7)	0.696 ± 0.005	0.178
C (0.0)	0.005 ± 0.004	0.13
nSig	390.7 ± 0.8	24.7

Belle ($772 \cdot 10^6$ $B\bar{B}$): $N_{sig} = 648$, $\sigma_S = 0.15$, $\sigma_C = 0.10$

BaBar ($467 \cdot 10^6$ $B\bar{B}$): $N_{sig} = 472$, $\sigma_S = 0.17$, $\sigma_C = 0.11$

$L = 300 \text{ fb}^{-1}$: $N_{sig} = 106$, $N_{sxf} = 25$, $N_{cont} = 360$, $N_{peak} = 27$



Preliminary results:

Par	Bias	RMS
S (0.7)	0.708 ± 0.010	0.330
C (0.0)	-0.013 ± 0.008	0.246
nSig	110.2 ± 0.6	18.5

Less events due to lower BR
and reduced efficiency

Belle¹ ($772 \cdot 10^6 \text{ BB}$): $N_{sig} = 104$, $\sigma_S = 0.21$, $\sigma_C = 0.18$
 BaBar ($467 \cdot 10^6 \text{ BB}$): $N_{sig} = 105$, $\sigma_S = 0.26$, $\sigma_C = 0.20$

¹including also $\eta' \rightarrow \rho^0 \gamma$

- Almost a complete analysis chain for sensitivity study for \mathcal{CP} in $B^0 \rightarrow \eta' K_S^0$ channel;
- Presente at last B2TIP workshop;
- preliminary results are encouraging;
 - ▶ comparison with Belle and BaBar results looks fine;
- many thing to do:
 - ▶ include machine background (in progress)
 - ▶ complete $K_S^0 \rightarrow \pi^+ \pi^-$ channels;
 - ▶ study $K_S^0 \rightarrow \pi^0 \pi^0$ final states;
 - ▶ add $\eta' \rightarrow \rho^0 \gamma K_S^{0+-} / K_S^{000}$ channel;
 - ▶ systematics uncertainties evaluation;
 - ▶ documentation
 - ▶ ...
- manpower: a new postDoc student from Padova, **Alessandro Mordà**, is joining me for this work at $\sim 50\%$

Additional or backup slides

good candidate selection $B^0 \rightarrow \eta'(\rightarrow \eta_{\gamma\gamma}\pi^+\pi^-)K_S^{0+-}$:

- Reconstruct decay chain with mass constrains for η , η' , K_S^0 ,
 - vertex only (w/o mass) for B^0

■ $\eta \rightarrow \gamma\gamma$:

▶ gamma:all: $0.06 < E_\gamma < 6$ GeV,
 $-150 < \text{clus}_{time} < 0$, $E_9/E_{25} > 0.75$

▶ $M(\eta_{\gamma\gamma}) \in [0.52, 0.57]$ GeV;

■ $\eta' \rightarrow \eta_{\gamma\gamma}\pi^+\pi^-$:

▶ pi:all

▶ $\Delta \log \mathcal{L}(\pi, K) > -10$; new

▶ $d_0(\pi^\pm) < 0.08$ mm;

▶ $z_0(\pi^\pm) < 0.1$ mm;

▶ N hits_{PXD}(π^\pm) > 1

▶ $M(\eta') \in [0.93, 0.98]$ GeV;

if $N_{cands} > 1$, select candidate with highest $P\text{-value}_{vtx}(B_0, \eta', K_S^0)$

■ $K^0 \rightarrow \pi^+\pi^-$:

▶ K_S0:mdst

▶ $M(K_S^0 \rightarrow \pi^+\pi^-) \in [0.48, 0.52]$ GeV;

■ $B^0 \rightarrow \eta'(\rightarrow \eta_{\gamma\gamma}\pi^+\pi^-)K_S^{0+-}$

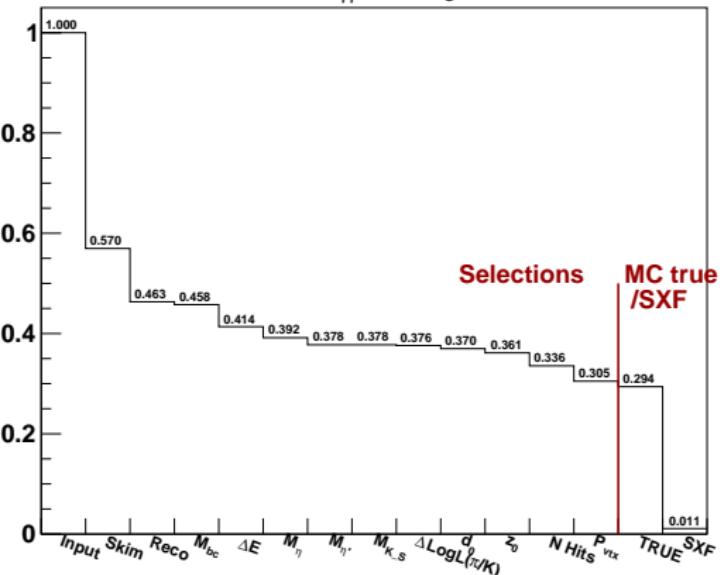
▶ $M_{bc} > 5.25$ GeV;

▶ $|\Delta E| < 0.1$ GeV;

▶ $P\text{-value}_{vtx}(B_0, \eta', K_S^0) > 1 \cdot 10^{-5}$

Events statistics

$B^0 \rightarrow \eta'(\eta_{\gamma\gamma} \pi^+\pi^-) K_s^0(\pi^+\pi^-)$



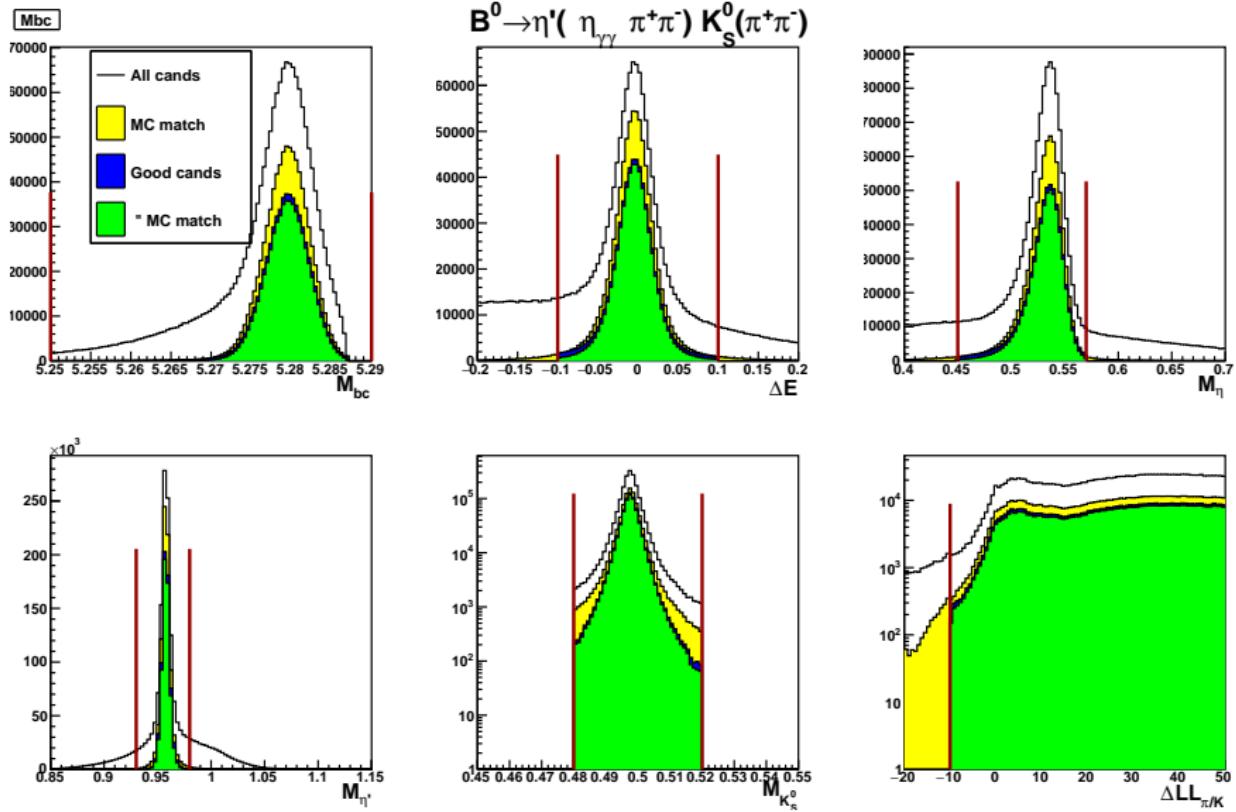
Combinatorics

Cands mult.: 1.88

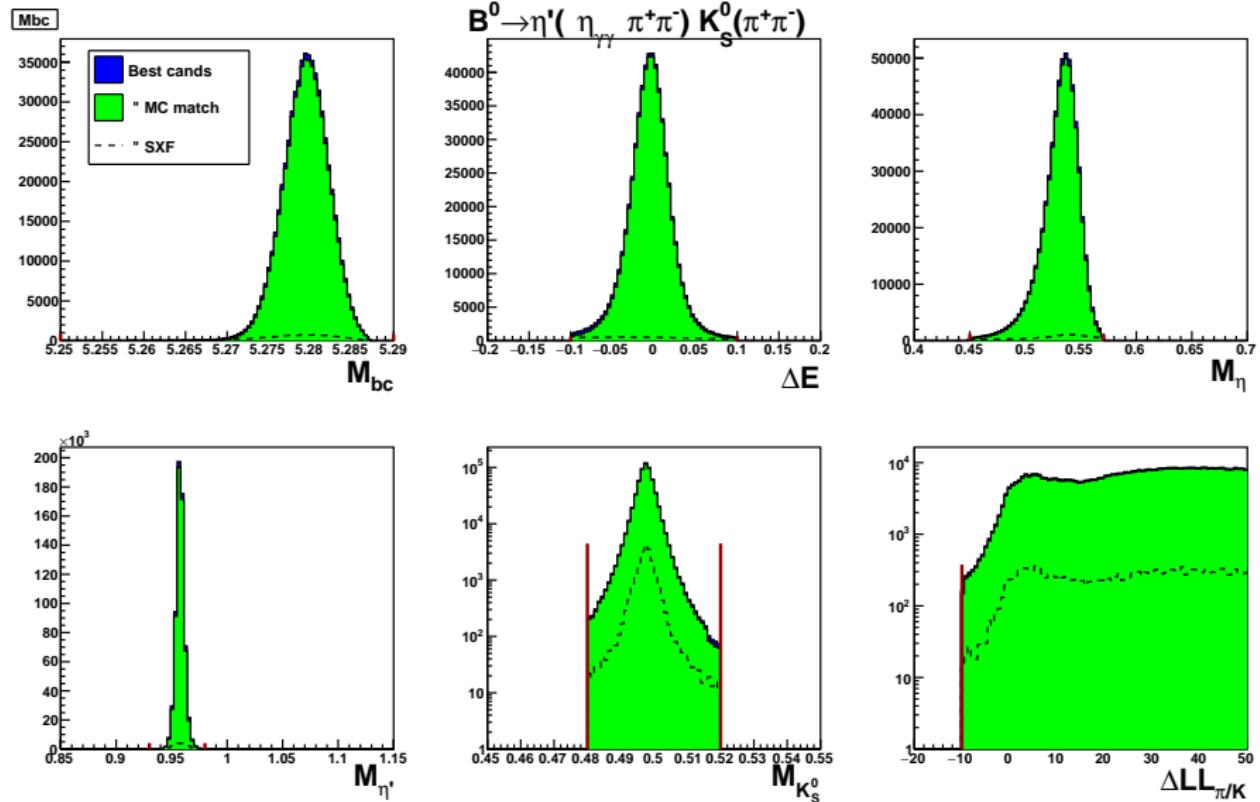
Good cands mult.: 1.06

Efficiency %

skim	57.0
preselection	46.1
good cands	30.5
MC true	29.4
SXF	1.1



Best candidates, after selections



good candidate selection $B^0 \rightarrow \eta'(\rightarrow \eta_{3\pi}\pi^+\pi^-)K_S^{0+-}$:

- Reconstruct decay chain with mass constraints for η , η' , K_S^0 ,
 - vertex only (w/o mass) for B^0

■ π^0 :

- gamma:all: $0.06 < E_\gamma < 6$ GeV,
 $-150 < \text{clus}_{time} < 0$, $E_9/E_{25} > 0.75$

- $M(\pi^0) \in [100, 150]$ MeV

■ $\eta \rightarrow \pi^+\pi^-\pi^0$:

- pi:all

- $\Delta \log \mathcal{L}(\pi, K) > -10$; new

- $M(\eta_{3\pi}) \in [0.52, 0.57]$ GeV;

- $d_0(\pi^\pm) < 0.08$ mm;

- $z_0(\pi^\pm) < 0.1$ mm;

- $N \text{ hits}_{PXD}(\pi^\pm) > 1$

■ $\eta' \rightarrow \eta_{3\pi}\pi^+\pi^-$:

- $M(\eta') \in [0.93, 0.98]$ GeV;

■ $K^0 \rightarrow \pi^+\pi^-$:

- K_S0:mdst

- $M(K_S^0 \rightarrow \pi^+\pi^-) \in [0.48, 0.52]$ GeV;

■ $B^0 \rightarrow \eta'(\rightarrow \eta_{3\pi}\pi^+\pi^-)K_S^{0+-}$

- $M_{bc} > 5.25$ GeV;

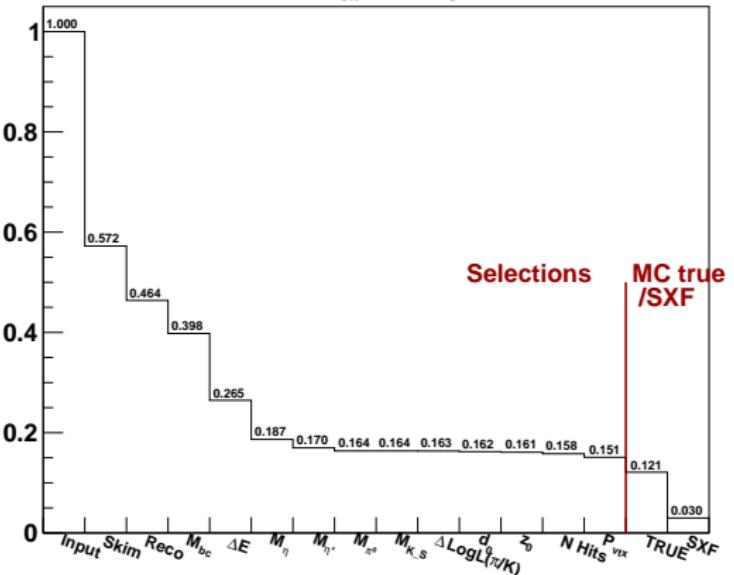
- $|\Delta E| < 0.15$ GeV;

- P-value_{vtx}(B_0, η', K_S^0) $> 1 \cdot 10^{-5}$

if $N_{cands} > 1$, select candidate with highest P-value_{vtx}(B_0, η', η, K_S^0)

Events statistics

$$B^0 \rightarrow \eta'(\eta_{3\pi} \pi^+ \pi^-) K_s^0(\pi^+ \pi^-)$$



Combinatorics

Cands mult.: 21.5

Good cands mult.: 1.45

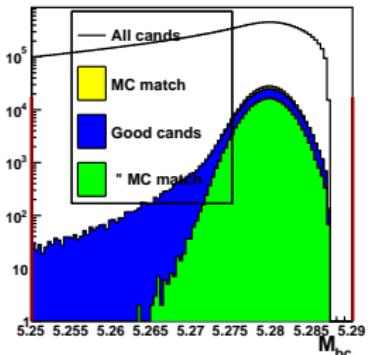
Efficiency %

skim	57.2
preselection	46.2
good cands	15.1
MC true	12.1
SXF	3.0

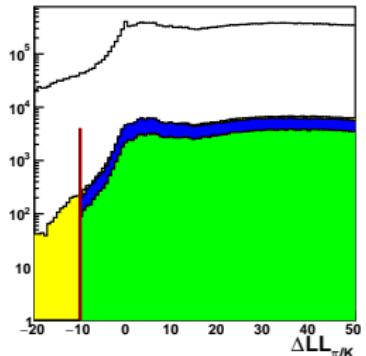
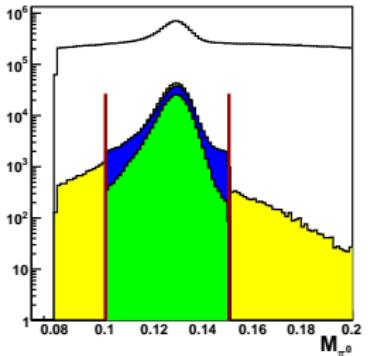
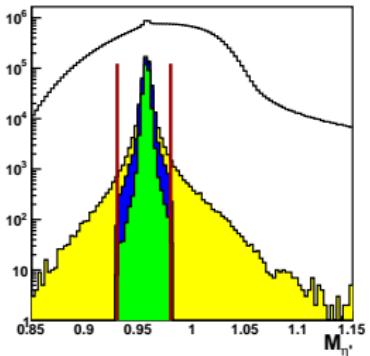
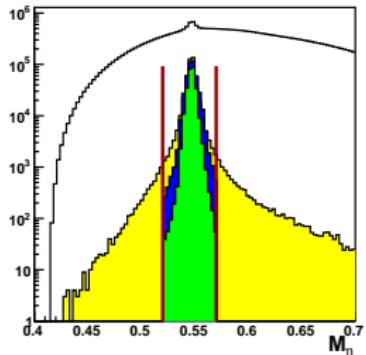
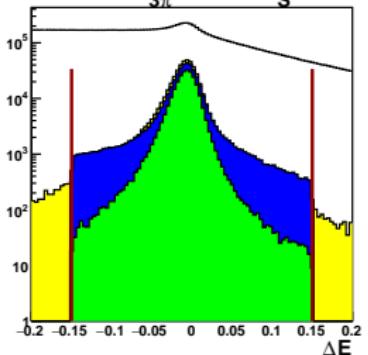
Reco eff is as good as $\eta_{\gamma\gamma}$ channel.

50% eff drop due to poor resolution on M_{bc} , ΔE , M_η all coming from π^0 reconstruction in $\eta \rightarrow \pi^+ \pi^- \pi^0$ decay

Mbc

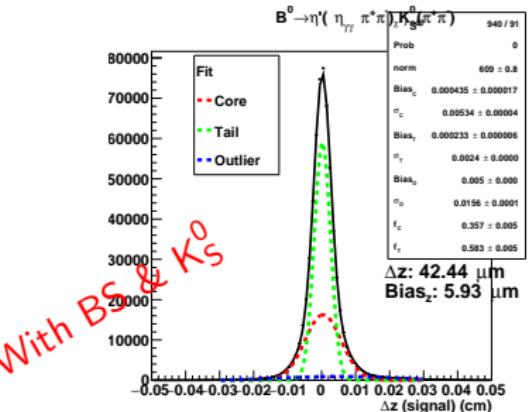
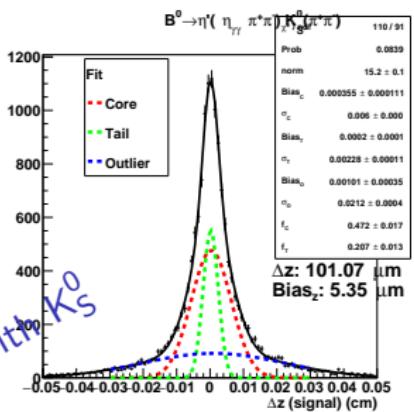
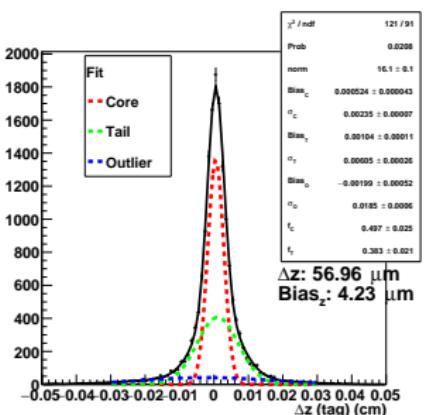
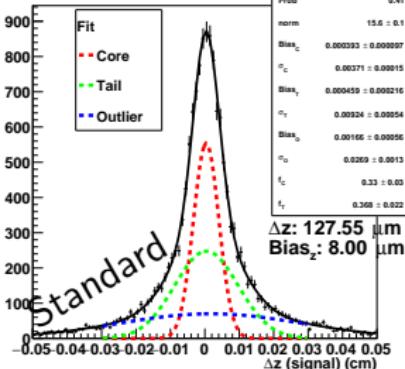


$B^0 \rightarrow \eta'(\eta_{3\pi} \pi^+ \pi^-) K_S^0(\pi^+ \pi^-)$



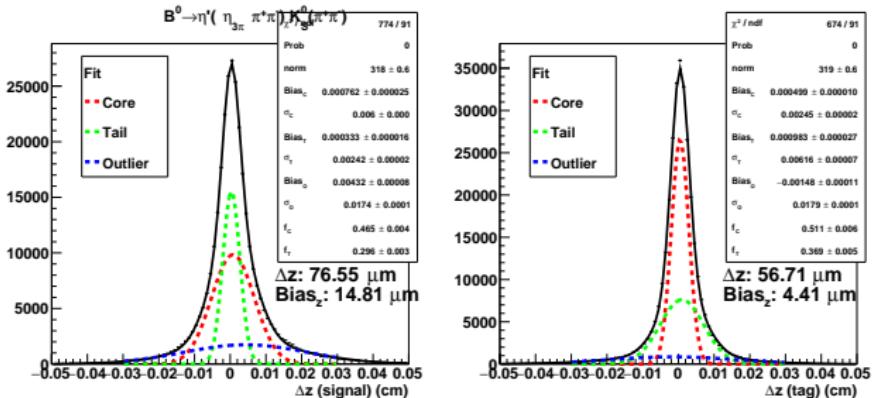
$$B^0 \rightarrow \eta'(\rightarrow \eta_{\gamma\gamma} \pi^+ \pi^-) K_S^{0+}$$

$$B^0 \rightarrow \eta'(\eta_{\gamma\gamma} \pi^+ \pi^-) K_S^{0+}$$

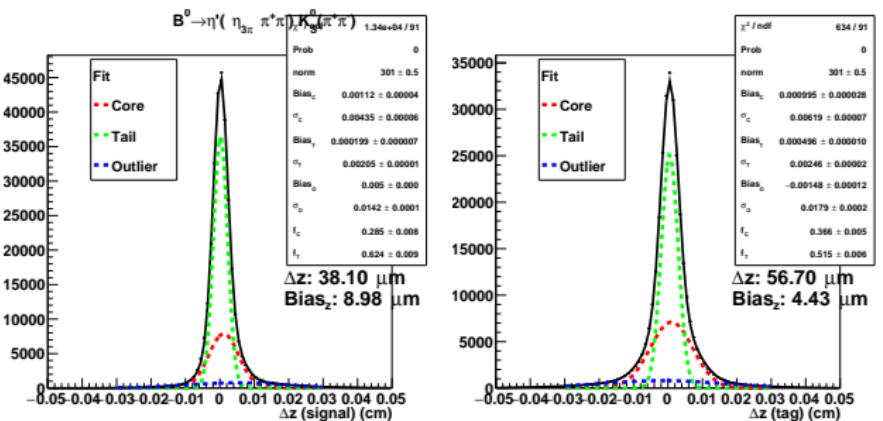


$$B^0 \rightarrow \eta'(\rightarrow \eta_3 \pi^+ \pi^-) K_S^{0+-}$$

Standard

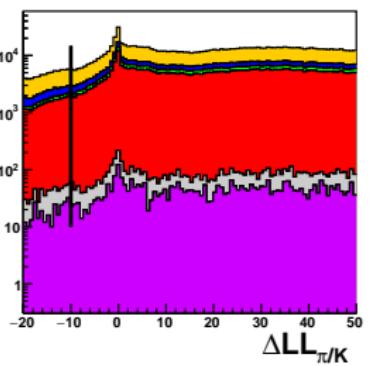
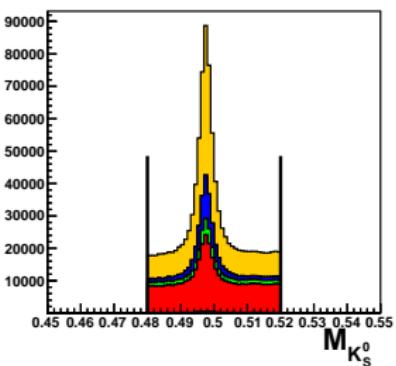
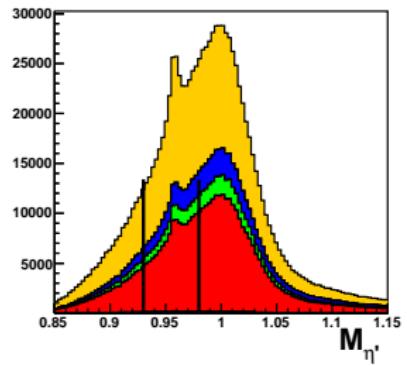
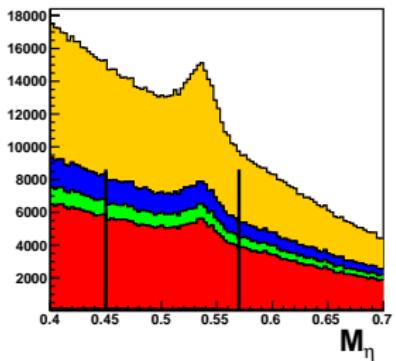
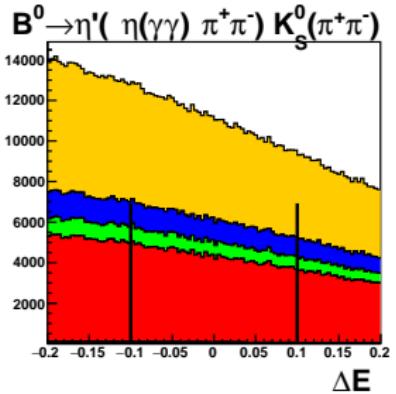
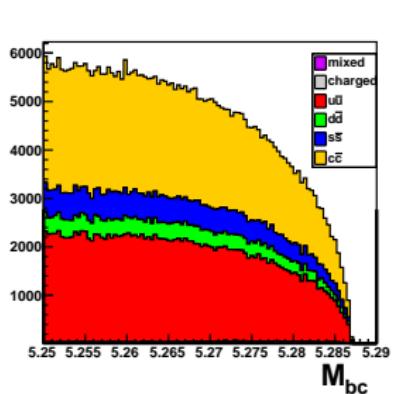


With BS & K_S^0



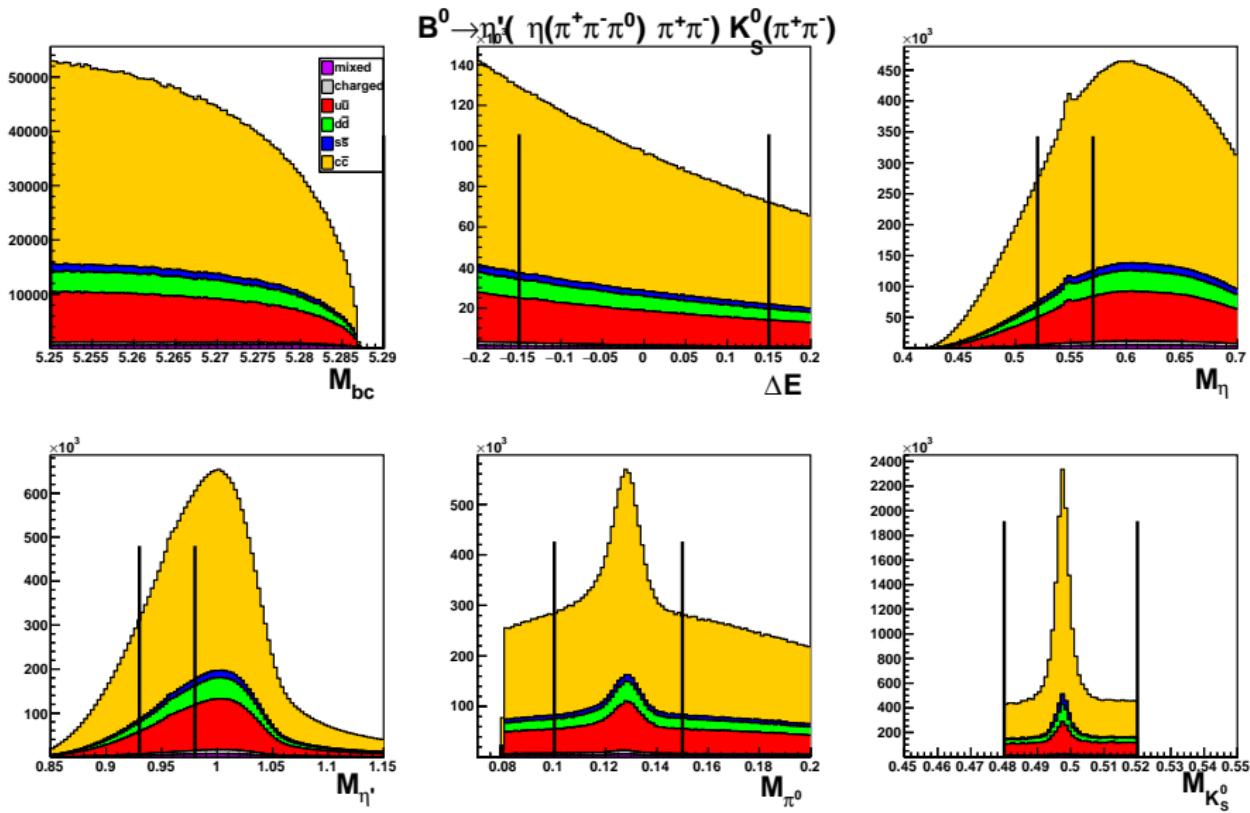
Background distribution

All candidates



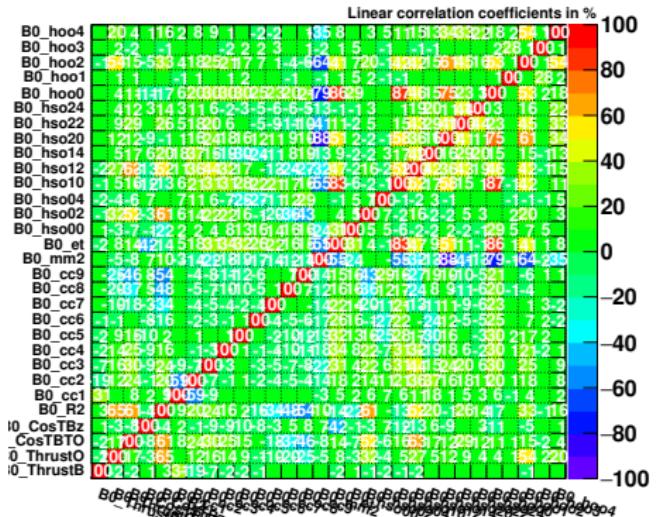
Background distribution

All candidates

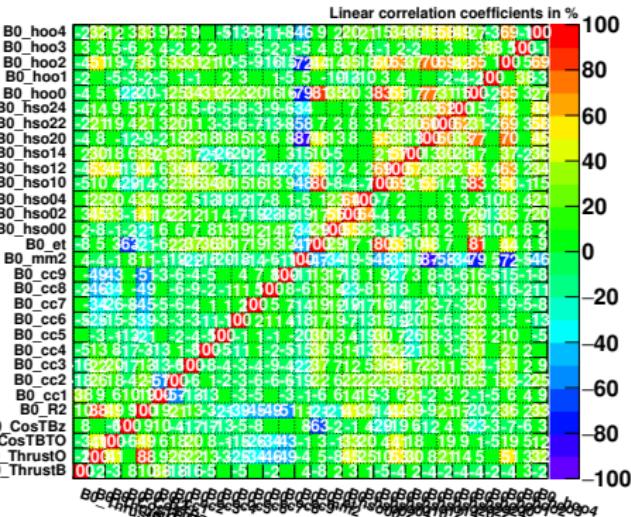


Continuum Suppression correlation matrix

Correlation Matrix (signal)

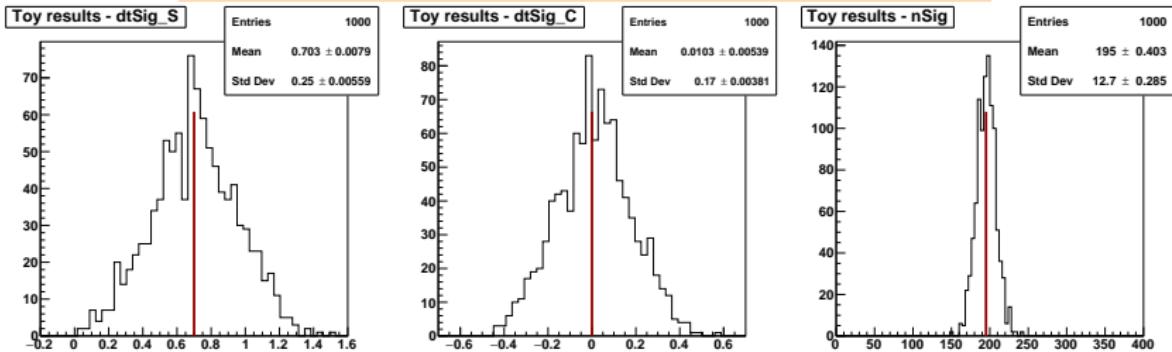


Correlation Matrix (background)



Tight: $\epsilon_{sig,sxf,peaking} = 50\%$, $\epsilon_{continuum} = 2.5\%$

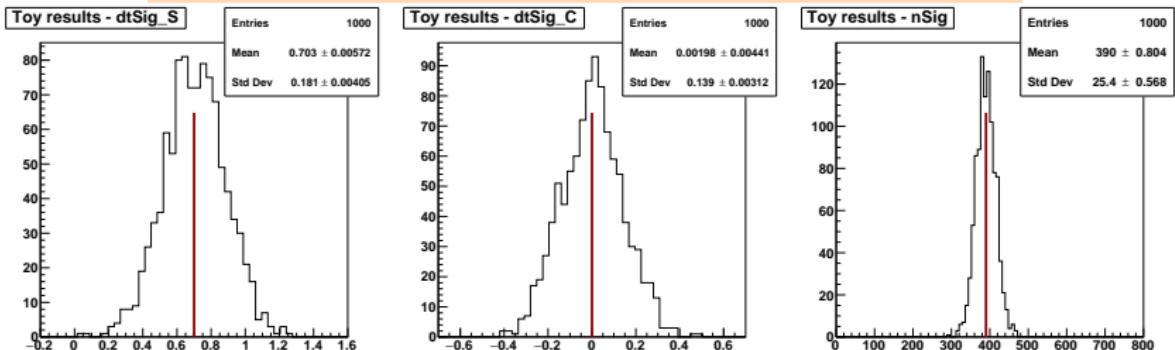
$N_{sig} = 195$, $N_{sxf} = 8$, $N_{cont} = 83$, $N_{peak} = 15$



Par	Bias	RMS
S (0.7)	0.703 ± 0.008	0.25
C (0.0)	0.010 ± 0.005	0.17
nSig	195.4 ± 0.4	12.7

Loose: $\epsilon_{sig,sxf,peaking} = 95\%$, $\epsilon_{continuum} = 42\%$

$N_{sig} = 390$, $N_{sxf} = 14$, $N_{cont} = 1400$, $N_{peak} = 28$



Par	Bias	RMS
S (0.7)	0.703 ± 0.005	0.18
C (0.0)	0.002 ± 0.004	0.14
nSig	389.8 ± 0.8	25.4

mode $\eta' \rightarrow \pi^\pm \eta$	This analysis*			Belle ^[Belle(2014)]			BaBar ^[BABAR(2009)]		
	N_{sig}	σ_S	σ_C	N_{sig}	σ_S	σ_C	N_{sig}	σ_C	σ_S
$\eta_{\gamma\gamma} K_S^{0+-}$	390	0.19	0.11	648	0.15	0.098	472	0.17	0.11
$\eta_{\gamma\gamma} K_S^{000}$	Just started			104	0.21 [†]	0.18 [†]	105	0.34	0.30
$\eta_{3\pi} K_S^{0+-}$	106	0.33	0.25	174	0.26	0.18	171	0.26	0.20
$\eta_{3\pi} K_S^{000}$	Will try			Not used					
$\eta' \rightarrow \rho^0 \gamma K_S^{0+-}$	Not yet			1411	0.098	0.069	1005	0.12	0.09
$\eta' \rightarrow \rho^0 \gamma K_S^{000}$	Not yet			162	0.21 [†]	0.18 [†]	206	0.33	0.26

*Very preliminary estimate based on toy MC, $L = 300 \text{ fb}^{-1}$

Warning: no machine background yet

[†]Results combining $\eta' \rightarrow \pi^\pm \eta_{\gamma\gamma}$ and $\eta' \rightarrow \rho^0 \gamma$

Bibliography I

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