

Something

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some meeting,
somewhere, sometime

- 1 AOD vs MiniAOD (Paolo)
- 2 B-mixing in $t\bar{t}$ events (Martino *et al.*)
- 3 P'_5 measurement in $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ (Stefano Alessio)

AOD vs MiniAOD (Paolo)

Issue

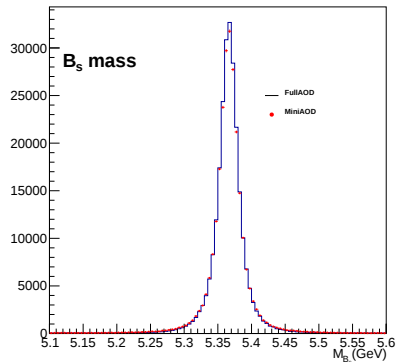
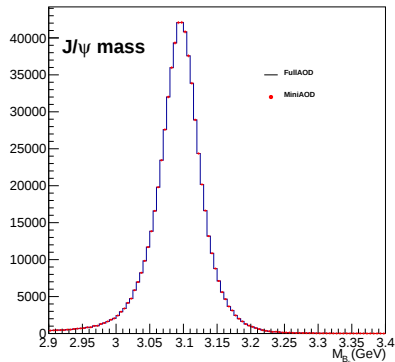
- AOD production and storage probably discontinued in 2017:
- MiniAOD only choice left?
- Any difference between AOD and MiniAOD for B reconstruction and analysis?
- $B_S^0 \rightarrow J/\psi \phi$, $J/\psi \rightarrow \mu^- \mu^+$, $\phi \rightarrow K^+ K^-$
- Comparing same dataset 1 M events, same reconstruction, from AOD and from MiniAOD
BsToJpsiPhi_BMuonFilter_TuneCUEP8M1_13TeV-pythia8-evtgen
- A newer version of MiniAOD already available but not yet used

- $p_{T,\mu} > 3.0$ GeV
- $p_{T,K} > 0.7$ GeV
- $2.8 \text{ GeV} < m_{J/\psi} < 3.4 \text{ GeV}$
- $1.005 \text{ GeV} < m_K < 1.035 \text{ GeV}$
- $P(\chi_{\text{vtx}}^2) > 0.02$

B_S^0 mass reconstructed with J/ψ mass constraint

Invariant masses distributions

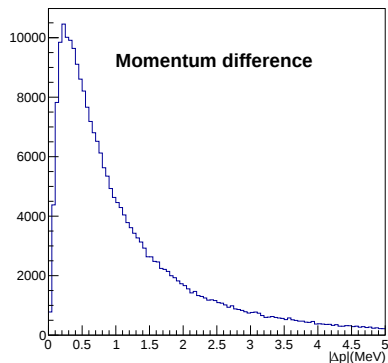
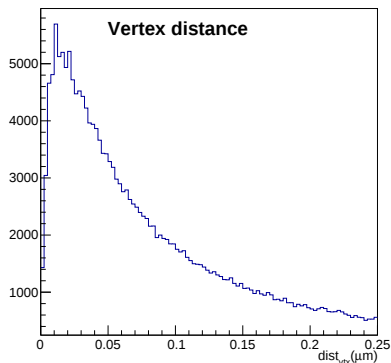
	SIM	AOD	AOD&MiniAOD
J/ψ	1018280	662731	662731
B_s^0	528069	297150	255448



Event-by-event comparison

Compare each B_s^0 reconstructed in AOD with the same reconstructed in MiniAOD:

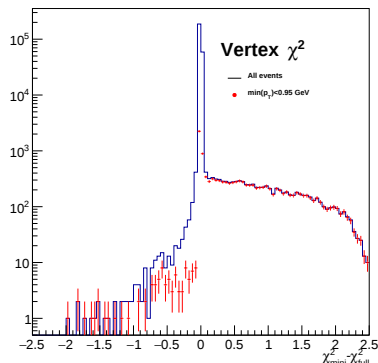
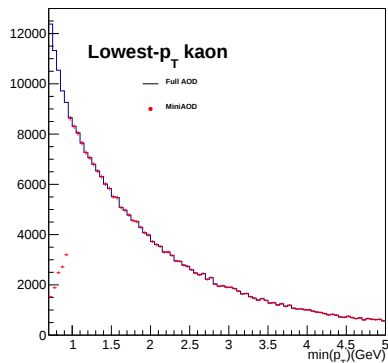
- compute vertex distance (3D)
- compute modulus of 3-momentum difference (sum of momenta extrapolated to vertex)



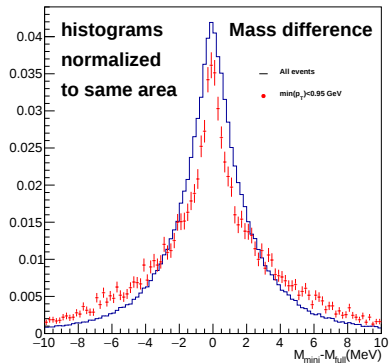
Tracking information in MiniAOD:

- tracks with $p_T > 0.95$ GeV: momentum from PF candidates, approximate covariance matrix
- tracks from Inclusive Vertex Finder (“whitelist”, no p_T cut: other tracks can be added)

Efficiency difference concentrated at low- p_T



Event-by-event mass difference



Update on B-mixing in tt events

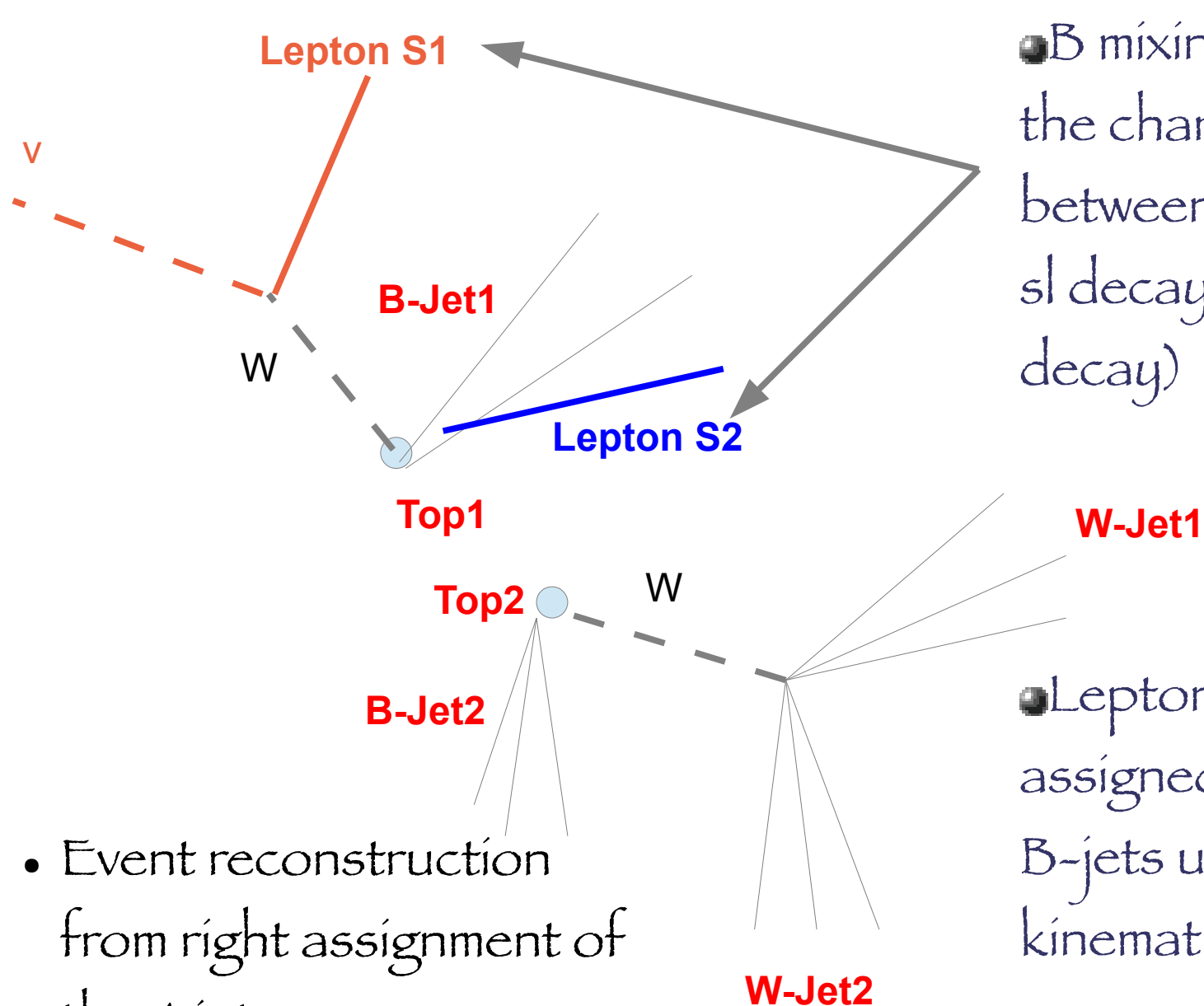
Martino Margoni
9/3/2017

- Motivation
- Analysis Strategy:
 - Event Reconstruction
 - B flavor tagging at the production
- Caveats:
 - Work from Paolo (selection optimization) and Alessio (separation of $b \rightarrow l$ vs $b \rightarrow c \rightarrow l$) still to be included
 - Only Run 1 MC analyzed
- Analysis will be performed on Run 2

Motivation

- Semileptonic top decays $t\bar{t}$, $t \rightarrow lb\nu$, $\bar{t} \rightarrow \bar{b}X$
 - ✦ lepton tags the flavor of both the B-jets at the production time
- Arxiv 1212.4611 [Gedalia, Isidori et al.]: 3σ test of the D0 anomaly with 50 fb^{-1} at 14 TeV ($\delta A_{sl} \sim 0.15\%$)
- Interests of the integrated B mixing measurements:
 - ✦ Original Analysis
 - ✦ Compare $\chi(m_t)$ with $\chi(m_Z)$: test QCD factorization
 - ✦ First step towards CPV in B mixing

Analysis Strategy



● B mixing obtained exploiting the charge correlation between leptons **S1** (from top sl decay) and **S2** (from B sl decay)

● Lepton **S2** has to be assigned to one of the two B-jets using topological and kinematic quantities

- Event reconstruction from right assignment of the 4 jets

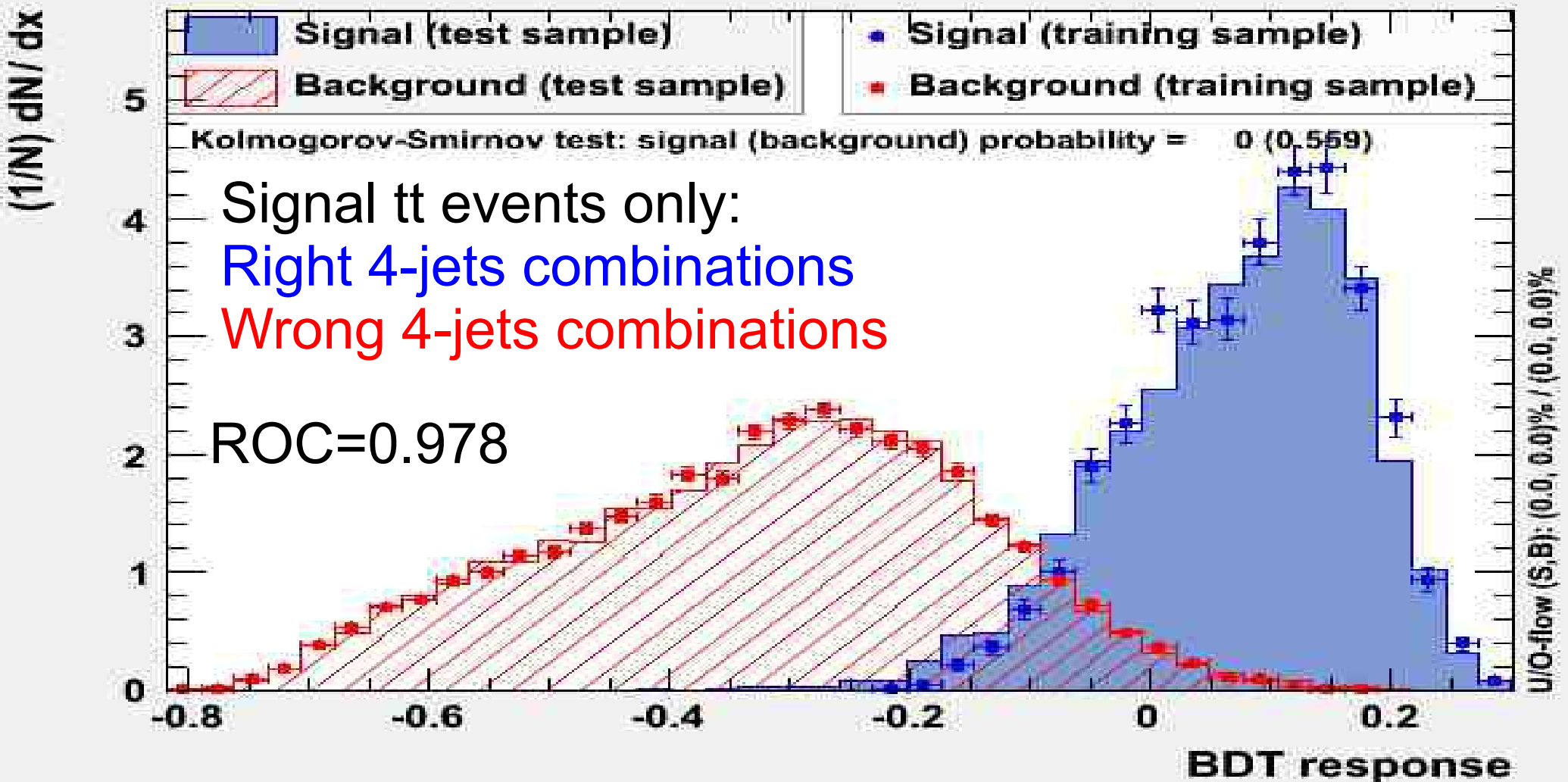
Event reconstruction

Goals:

- Right topological assignment of the 4-jets in the event
- B Flavor Tagging at the production for $t \rightarrow b \rightarrow (c) \rightarrow l$ events

TMVA Variables include:

- 4 jets spectra
- Angles between jets,
- $m(W \rightarrow jj)$
- $m(t \rightarrow \text{hadrons})$, $m(t \rightarrow Wb)$
- Btag info (only for jet with no leptons to avoid bias on χ)
- Lepton P_t wrt jet axis



By considering the 4-jets combination having maximum BDT:

Prob(4 jets right assignment)	=	$37.8 \pm 0.7\%$
Prob(2 B-jets right assignment)	=	$53.2 \pm 0.7\%$
Prob(at least 1 B-jet right assignment)	=	$75.7 \pm 0.6\%$

Event Selection + Reconstruction

	Initial	Reco	Effi	Final Fraction
tt Semi Lep	1888	1028	54%	68.8± 1.2 %
tt Full Lep	1830	180	9.8%	12.0± 0.8 %
DY	179793	81	4 10 ⁻⁴	5.1 ± 0.6 %
QCD	360095	80	2 10 ⁻⁴	5.4 ± 0.6 %
W+jets	11947	74	6 10 ⁻³	4.9 ± 0.6 %
WW+ZZ+WZ	619	4	6 10 ⁻³	0.3 ± 0.1 %
Singletop	612	48	8%	3.2 ± 0.5 %

To be optimized

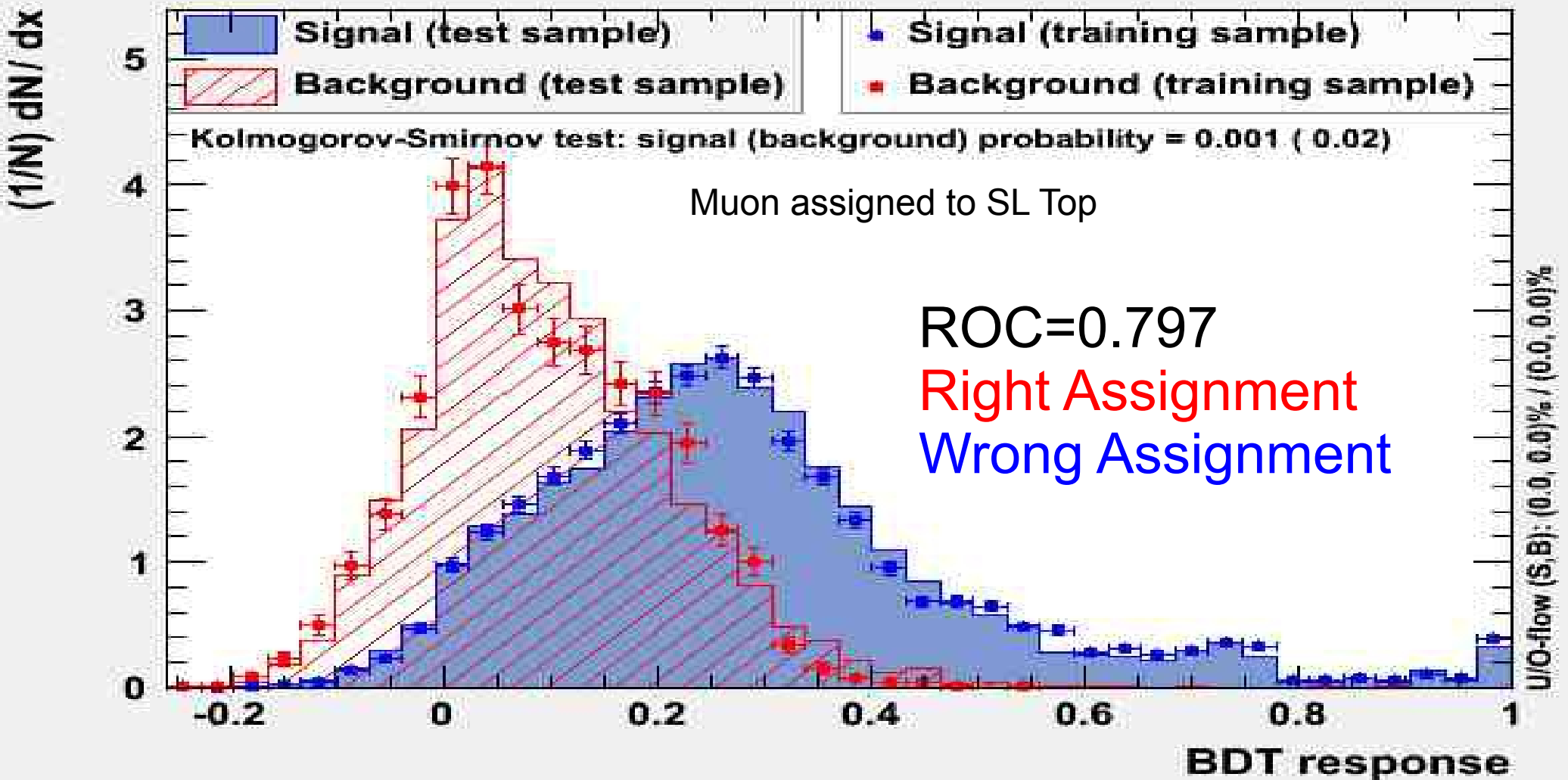
tt Full Lep and Singletop are mostly populated by signal events → Signal ~ 80%

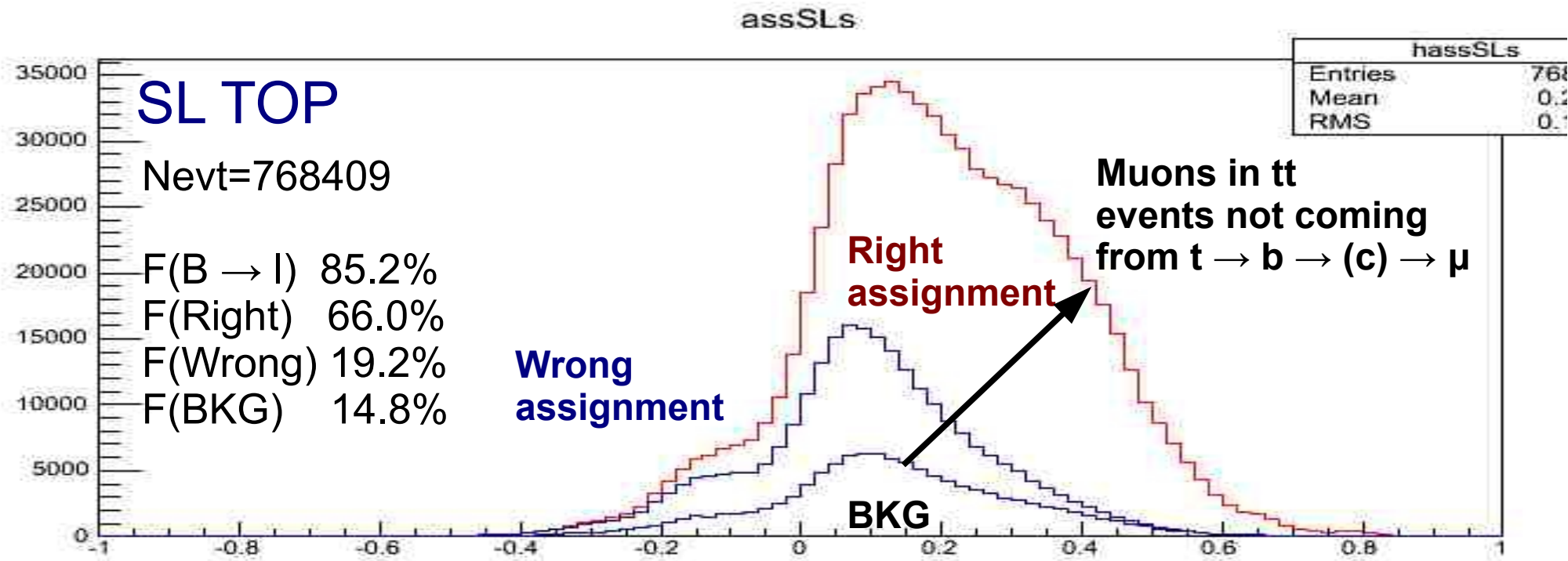
B flavor tagging

- After the event reconstruction, the 4-jets combinations are ordered according to their BDT value
- For every muon from $t \rightarrow b \rightarrow (c) \rightarrow l$, we choose the highest BDT 4-jets combination in which the muon jet has been classified as a B-jet
- We compare the top assigned to the muon by the algorithm with the right top from MC truth
 - Fraction of right assignment if muon assigned to SL top:
 $F=75.04 \pm 0.19\% \rightarrow \text{mistag} \sim 25\%$
 - Fraction of right assignment if muon assigned to Had top:
 $F=79.47 \pm 0.19\% \rightarrow \text{mistag} \sim 20\%$

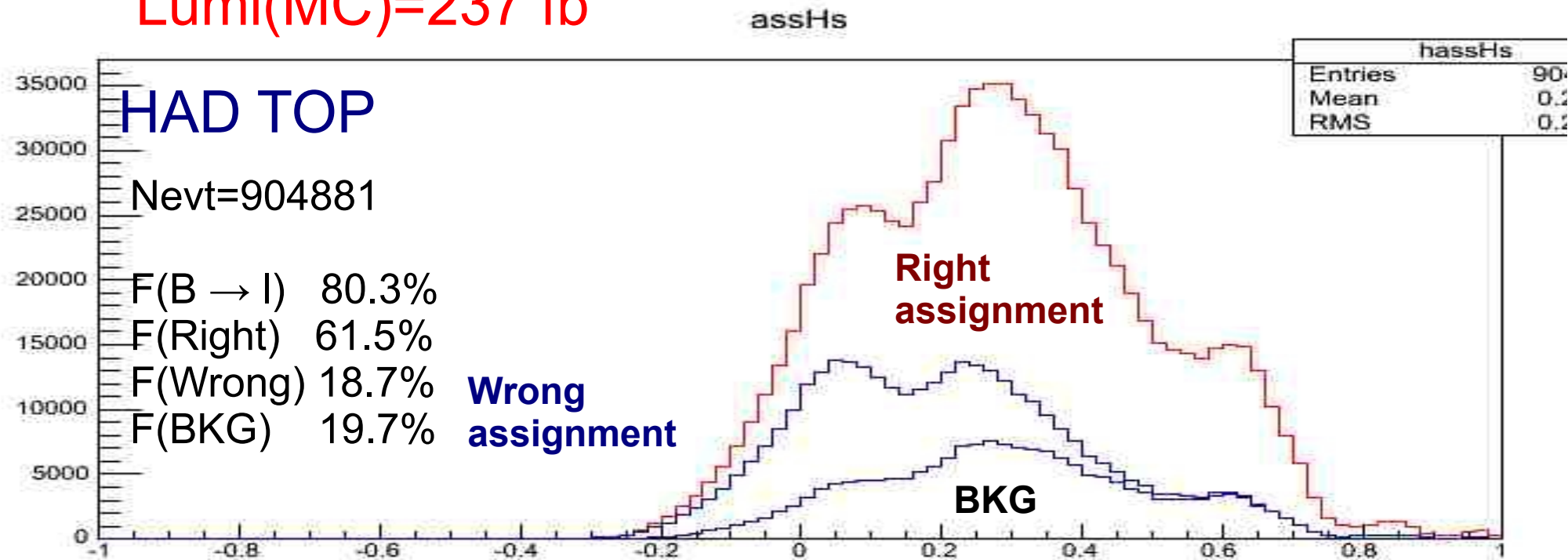
Define an additional BDT using angular variables to improve the performance

TMVA overtraining check for classifier: BDT

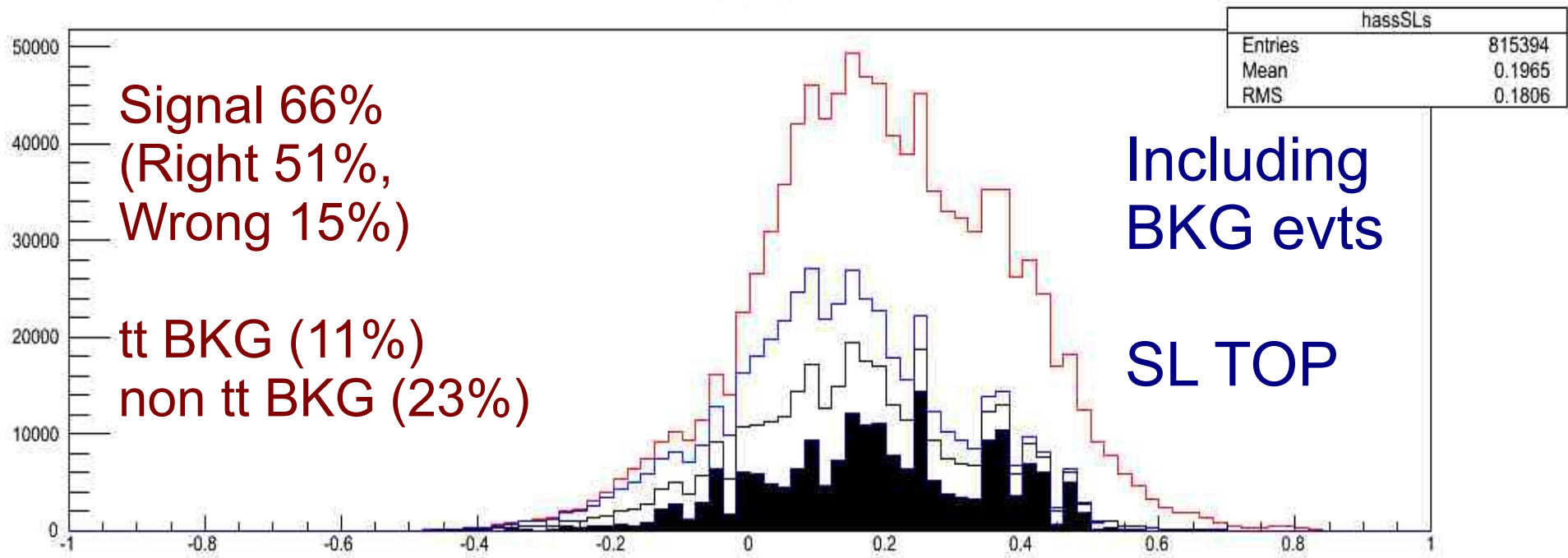




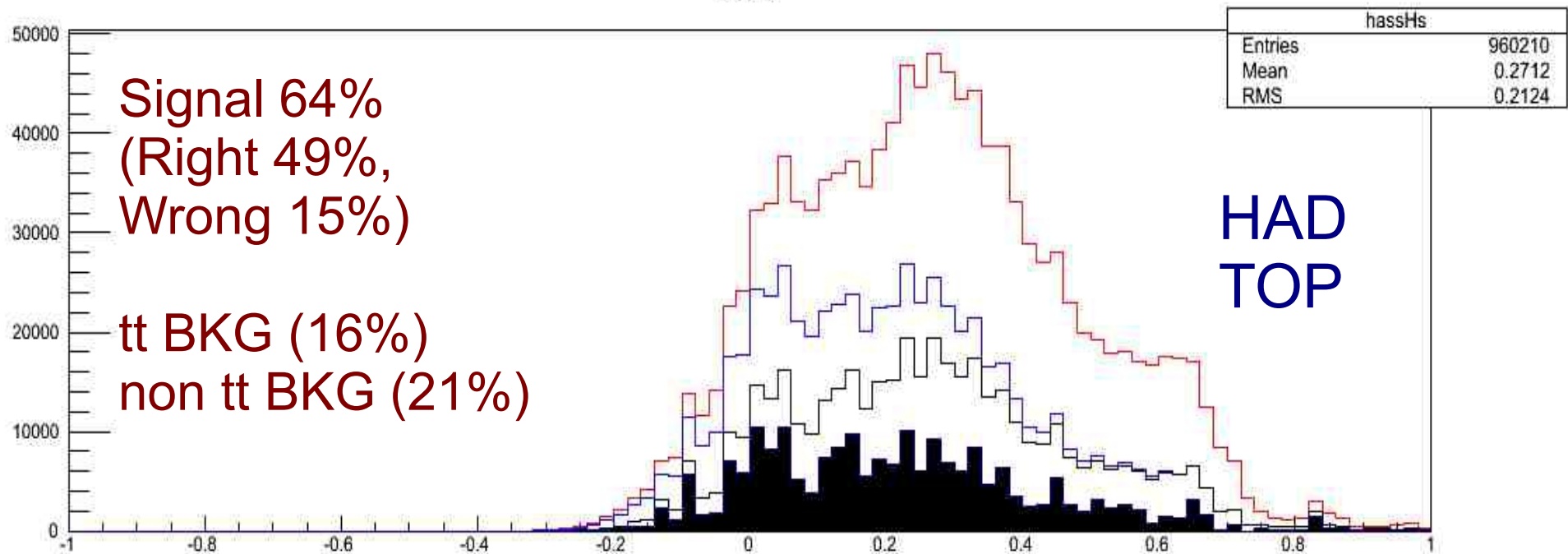
Lumi(MC)=237 fb⁻¹



assSLs



assHs



Mixing in top decays: projections

“Fixed” flavour at creation:

$$N_{\text{same}} = \bar{\chi} N_{\text{tot}} \quad ; \quad N_{\text{oppo}} = (1 - \bar{\chi}) N_{\text{tot}}$$

Run-1 analysis (muon only)

- Expected statistical error on mixing: $\sigma_{\chi} \sim 2 \cdot 10^{-3}$
- Expected statistical error on asymmetry: $\sigma_A \sim 2 \cdot 10^{-2}$

Run-2 analysis

- $\mathcal{L}_2 \sim 100 \text{ fb}^{-1} \sim 5\mathcal{L}_1$
 - $\sigma_{t\bar{t},2} \sim 4\sigma_{t\bar{t},1}$
 - same trigger thresholds for muons,
slightly higher for electrons ($p_T > 17, 12 \text{ GeV}$)
- } 20 times higher statistics

$$\sigma_{\chi(\text{stat})} \sim 0.5 \cdot 10^{-3} \quad ; \quad \sigma_{A(\text{stat})} \sim 0.5 \cdot 10^{-2}$$

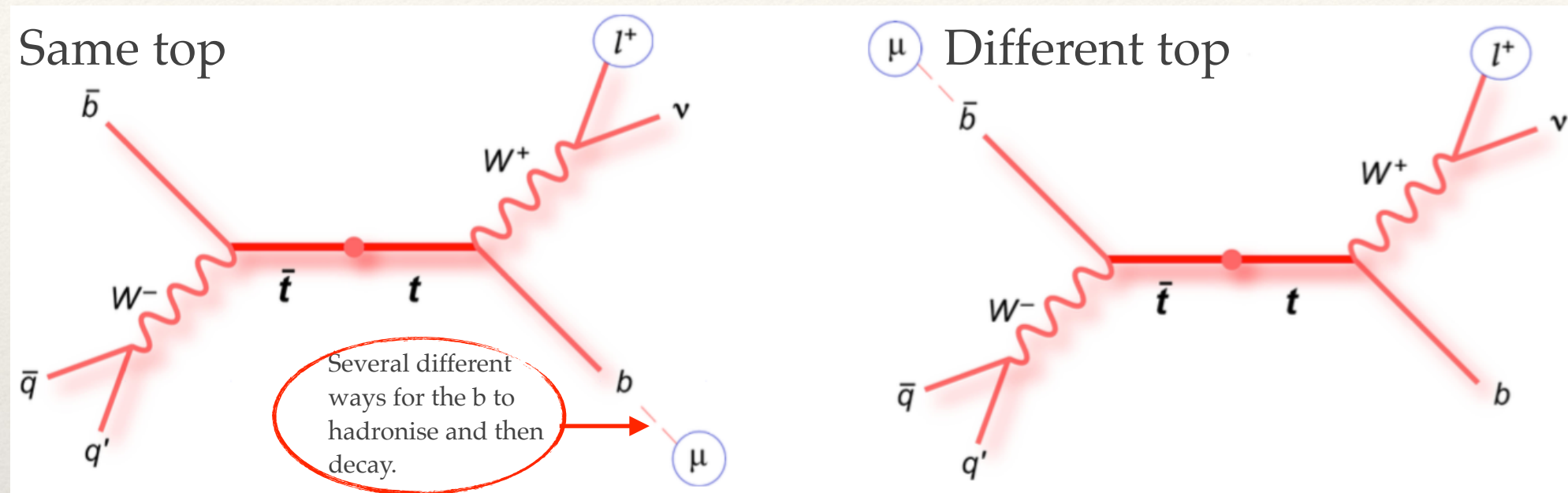
Not competitive with LHCb, but a measurement with a new technique

Next Steps

- Use DATA/MC comparison of the variables used in the BDTs (Student+Stefano)
- Merge with Paolo selection. Optimization of TMVA
- $b \rightarrow \mu$ vs $b \rightarrow c \rightarrow \mu$ separation using Alessio code
- Definition of PDF and fit on MC (closure test) and Data

CP violation in b decays using top quark pairs

- ❖ 20.3 fb⁻¹ of 8TeV data (pp collisions)



- ❖ Measure same and opposite sign lepton pairs to compute mixing and direct CP asymmetries from observed N^{++} , N^{--} , N^{+-} and N^{-+} rates:

$$N^{ij} = N^{q_\mu q_W}$$

- ❖ Mistag probability is 21%:

	N_j^{++}	N_j^{--}	N_j^{+-}	N_j^{-+}
N_i^{++}	0.79	0.00	0.00	0.21
N_i^{--}	0.00	0.79	0.21	0.00
N_i^{+-}	0.00	0.21	0.79	0.00
N_i^{-+}	0.21	0.00	0.00	0.79

$$A_{\text{mix}}^{b\ell} = \frac{\Gamma(b \rightarrow \bar{b} \rightarrow \ell^+ X) - \Gamma(\bar{b} \rightarrow b \rightarrow \ell^- X)}{\Gamma(b \rightarrow \bar{b} \rightarrow \ell^+ X) + \Gamma(\bar{b} \rightarrow b \rightarrow \ell^- X)},$$

$$A_{\text{mix}}^{bc} = \frac{\Gamma(b \rightarrow \bar{b} \rightarrow \bar{c} X) - \Gamma(\bar{b} \rightarrow b \rightarrow c X)}{\Gamma(b \rightarrow \bar{b} \rightarrow \bar{c} X) + \Gamma(\bar{b} \rightarrow b \rightarrow c X)},$$

$$A_{\text{dir}}^{b\ell} = \frac{\Gamma(b \rightarrow \ell^- X) - \Gamma(\bar{b} \rightarrow \ell^+ X)}{\Gamma(b \rightarrow \ell^- X) + \Gamma(\bar{b} \rightarrow \ell^+ X)},$$

$$A_{\text{dir}}^{c\ell} = \frac{\Gamma(\bar{c} \rightarrow \ell^- X_L) - \Gamma(c \rightarrow \ell^+ X_L)}{\Gamma(\bar{c} \rightarrow \ell^- X_L) + \Gamma(c \rightarrow \ell^+ X_L)},$$

$$A_{\text{dir}}^{bc} = \frac{\Gamma(b \rightarrow c X_L) - \Gamma(\bar{b} \rightarrow \bar{c} X_L)}{\Gamma(b \rightarrow c X_L) + \Gamma(\bar{b} \rightarrow \bar{c} X_L)},$$

CP violation in b decays using top quark pairs

- ❖ Hard lepton from W-boson tags b quark via $t \rightarrow bW^+ \rightarrow b\ell^+\nu$
- ❖ Soft muon (SMT algorithm*) from $b \rightarrow X\mu\nu$ probes the decay chain.
- ❖ Require 2 leptons in an event:

Same sign leptons:

$$\begin{aligned} t \rightarrow \ell^+\nu \quad (b \rightarrow \bar{b}) &\rightarrow \ell^+\ell^+X, \\ t \rightarrow \ell^+\nu \quad (b \rightarrow c) &\rightarrow \ell^+\ell^+X, \\ t \rightarrow \ell^+\nu \quad (b \rightarrow \bar{b} \rightarrow c\bar{c}) &\rightarrow \ell^+\ell^+X, \end{aligned}$$

Opposite sign leptons:

$$\begin{aligned} t \rightarrow \ell^+\nu \quad b &\rightarrow \ell^+\ell^-X, \\ t \rightarrow \ell^+\nu \quad (b \rightarrow \bar{b} \rightarrow \bar{c}) &\rightarrow \ell^+\ell^-X, \\ t \rightarrow \ell^+\nu \quad (b \rightarrow c\bar{c}) &\rightarrow \ell^+\ell^-X, \end{aligned}$$

- ❖ Use standard top reconstruction for a $t\bar{t} \ell + jets$ event.
- ❖ Require a displaced vertex (b candidate) tagged with SMT algorithm.
- ❖ Fully reconstruct $t\bar{t}$ candidate with KLFitter#.

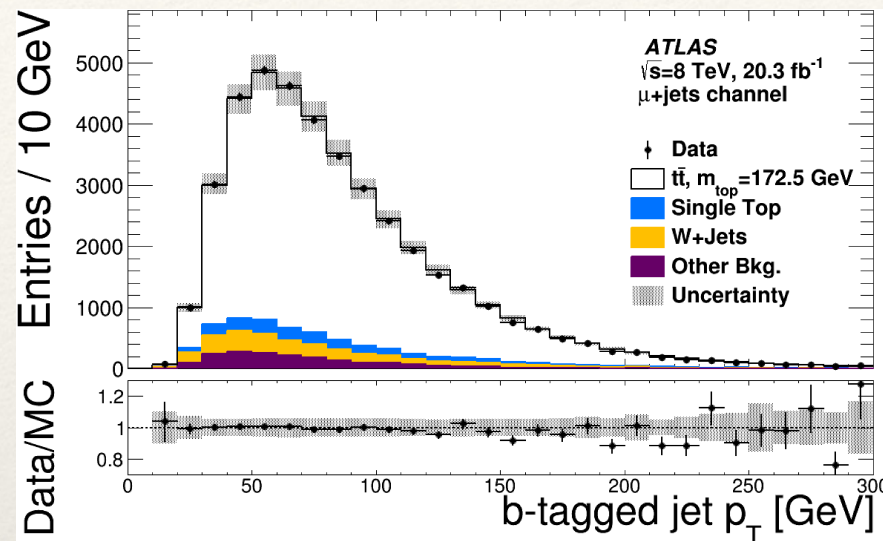
$$\begin{aligned} P(b \rightarrow \ell^+) &= \frac{N(b \rightarrow \ell^+)}{N(b \rightarrow \ell^-) + N(b \rightarrow \ell^+)} = \frac{N^{++}}{N^{+-} + N^{++}} = \frac{N^{++}}{N^+}, \\ P(\bar{b} \rightarrow \ell^-) &= \frac{N(\bar{b} \rightarrow \ell^-)}{N(\bar{b} \rightarrow \ell^-) + N(\bar{b} \rightarrow \ell^+)} = \frac{N^{--}}{N^{--} + N^{-+}} = \frac{N^{--}}{N^-}, \\ P(b \rightarrow \ell^-) &= \frac{N(b \rightarrow \ell^-)}{N(b \rightarrow \ell^-) + N(b \rightarrow \ell^+)} = \frac{N^{+-}}{N^{+-} + N^{++}} = \frac{N^{+-}}{N^+}, \\ P(\bar{b} \rightarrow \ell^+) &= \frac{N(\bar{b} \rightarrow \ell^+)}{N(\bar{b} \rightarrow \ell^-) + N(\bar{b} \rightarrow \ell^+)} = \frac{N^{-+}}{N^{--} + N^{-+}} = \frac{N^{-+}}{N^-}, \end{aligned}$$

$$A^{\text{ss}} = \frac{P(b \rightarrow \ell^+) - P(\bar{b} \rightarrow \ell^-)}{P(b \rightarrow \ell^+) + P(\bar{b} \rightarrow \ell^-)}, \quad A^{\text{os}} = \frac{P(b \rightarrow \ell^-) - P(\bar{b} \rightarrow \ell^+)}{P(b \rightarrow \ell^-) + P(\bar{b} \rightarrow \ell^+)},$$

$$\begin{aligned} A^{\text{ss}} &= r_b A_{\text{mix}}^{b\ell} + r_c (A_{\text{dir}}^{bc} - A_{\text{dir}}^{c\ell}) + r_{c\bar{c}} (A_{\text{mix}}^{bc} - A_{\text{dir}}^{c\ell}) \\ A^{\text{os}} &= \tilde{r}_b A_{\text{dir}}^{b\ell} + \tilde{r}_c (A_{\text{mix}}^{bc} + A_{\text{dir}}^{c\ell}) + \tilde{r}_{c\bar{c}} A_{\text{dir}}^{c\ell} \end{aligned}$$

- ❖ The r 's are decay rate fractions in fiducial region

CP violation in b decays using top quark pairs



	$e+jets$		$\mu+jets$	
WW, WZ, WW	50	± 7	45	± 5
$Z+jets$	800	± 80	450	± 60
Multijet	1 800	$\pm 1 400$	1 500	± 330
Single top	1 800	± 150	2 000	± 150
$W+jets$	2 500	± 160	2 800	± 150
$t\bar{t}$	30 000	$\pm 1 900$	34 000	$\pm 2 000$
Expected	37 000	$\pm 2 600$	41 000	$\pm 2 300$
Data	36 796		40 807	

- ❖ Good agreement between observed and expected yields.

	Data (10^{-2})		MC (10^{-2})		Existing limits (2σ) (10^{-2})		SM prediction (10^{-2})	
A^{ss}	-0.7	± 0.8	0.05	± 0.23	-		$< 10^{-2}$	[19]
A^{os}	0.4	± 0.5	-0.03	± 0.13	-		$< 10^{-2}$	[19]
A_{mix}^b	-2.5	± 2.8	0.2	± 0.7	< 0.1	[95]	$< 10^{-3}$	[96] [95]
A_{dir}^{bl}	0.5	± 0.5	-0.03	± 0.14	< 1.2	[94]	$< 10^{-5}$	[19] [94]
A_{dir}^{cl}	1.0	± 1.0	-0.06	± 0.25	< 6.0	[94]	$< 10^{-9}$	[19] [94]
A_{dir}^{bc}	-1.0	± 1.1	0.07	± 0.29	-		$< 10^{-7}$	[97]

- ❖ Competitive results ($\sigma \sim \%$ -level) obtained for mixing and direct CP asymmetries through this measurement
- ❖ Also measured A_{dir}^{bc} .

Existing constraints/SM predictions from:

- [19] O. Gedalia et al., Phys. Rev. Lett. **110** (2013) 232002,
- [94] Decotes-Genon et al., Phys. Rev. D **87** (2015).
- [95] HFAG, arXiv:1412.7515.
- [97] S. Bar-Shalom et al., Phys. Lett. B **694** (2011) 374–379

New CMS results on $B^0 \rightarrow K^{*0} \mu^+ \mu^-$ decay studies

- Introduction
- Event selection
- Decay rate and total p.d.f.
- An interesting statistical problem ...
- Signal evidence & fit validation
- Systematic uncertainties
- Preliminary results
- Summary



Mauro Dinardo

Università degli Studi di Milano Bicocca and INFN - Italy
On behalf of the CMS collaboration

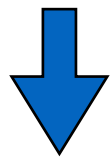
Moriond 2017 EW Session

22/3/2017

$B^0 \rightarrow K^{*0} \mu^+ \mu^-$ described within Standard Model (SM) as flavour-changing neutral-current process

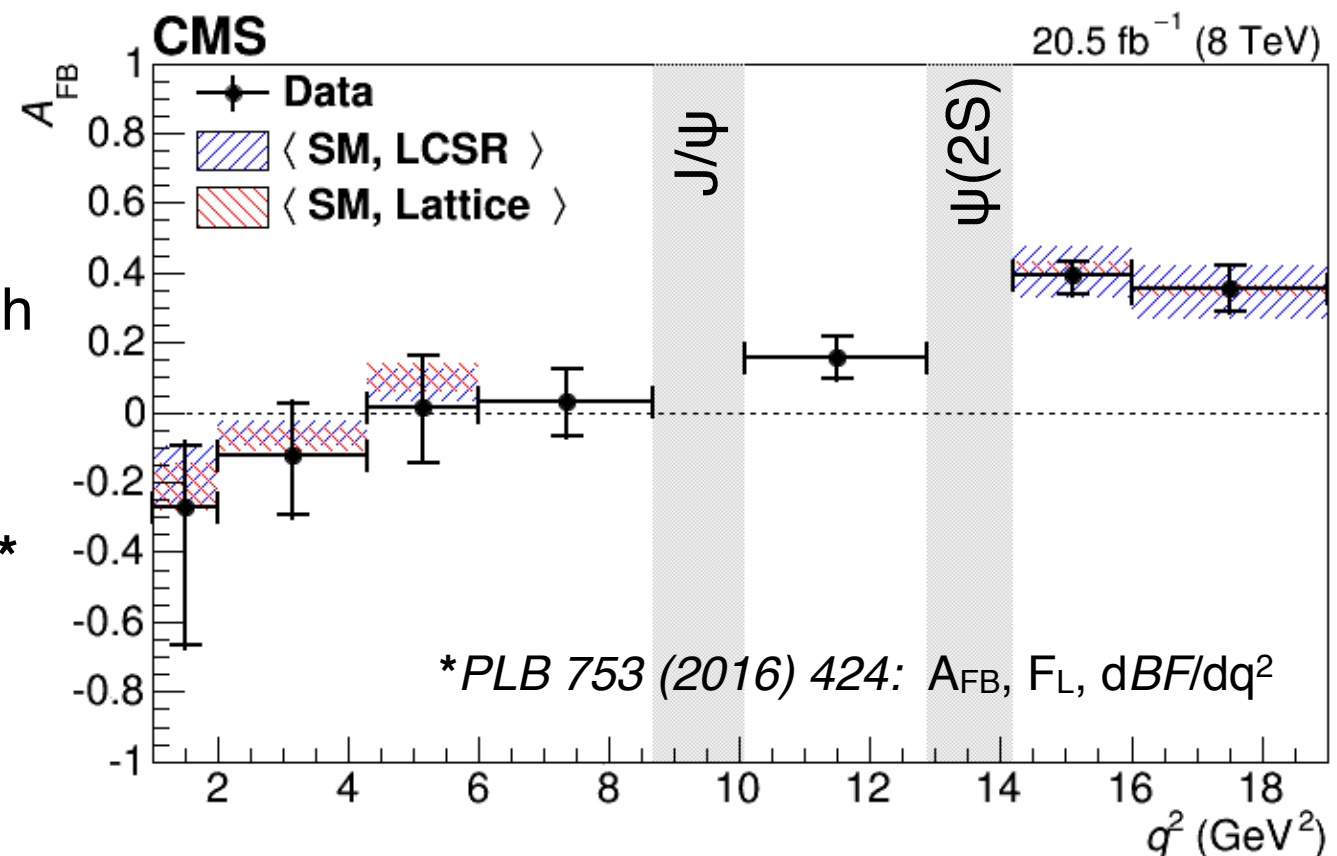
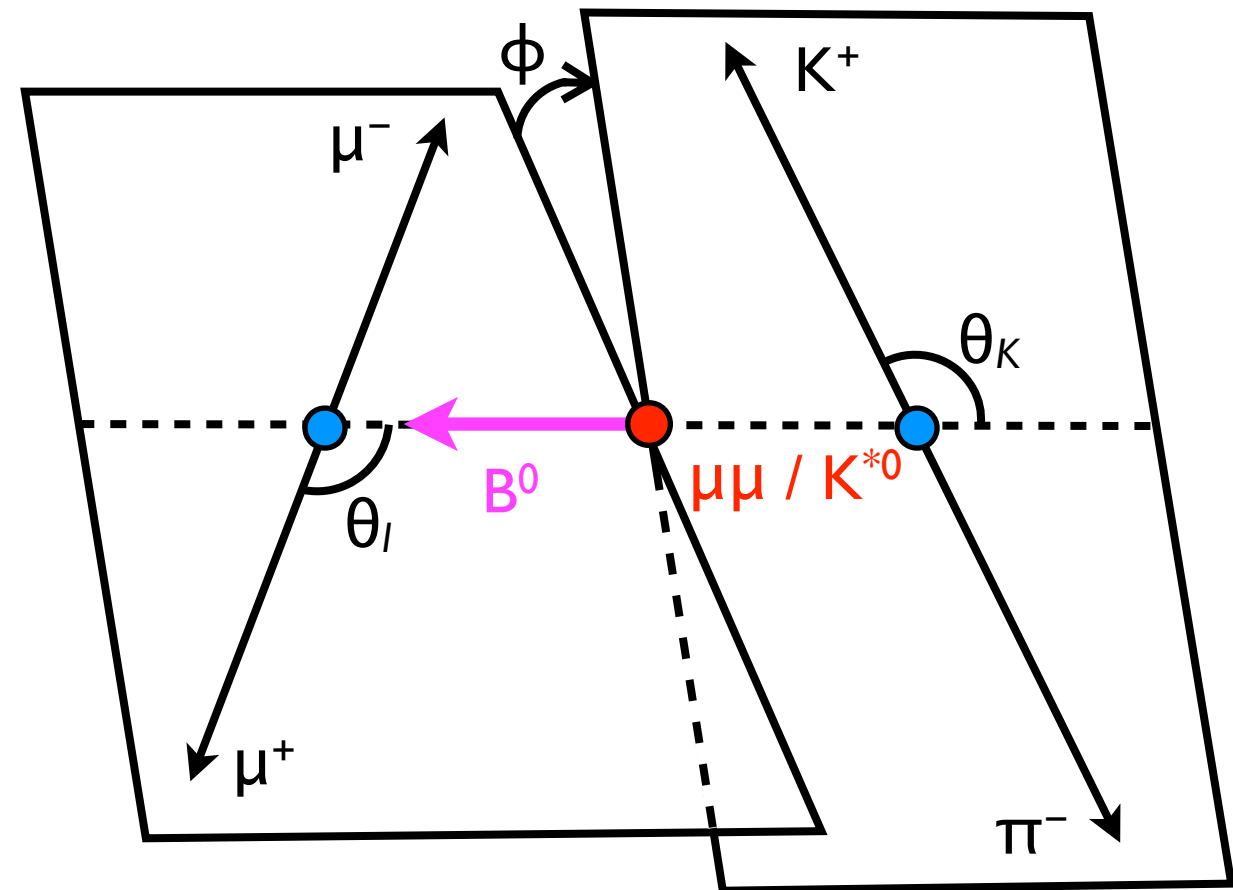
Decay fully described as a function of three angles (θ_l , θ_K , Φ) and dimuon invariant mass squared, q^2

Robust SM calculations of several angular parameters, *e.g.* forward-backward asymmetry of the muons, A_{FB} , longitudinal polarisation fraction of the K^{*0} , F_L , P_5' (see next slides) are available for much of the phase space



Discrepancy of the angular parameters vs q^2 with respect to SM indicates new physics

This talk is about extension of previous analysis* (same 2012 data set, 20.5 fb^{-1} (8 TeV)): new angular parameters, P_1 and P_5'



Dedicated **low mass displaced dimuon trigger** during **2012** data taking

Most important selections to discriminate signal and reduce trigger rate:

- single muon $p_T > 3.5$ GeV
- dimuon $p_T > 6.9$ GeV
- $1 < m(\mu\mu) = q < 4.8$ GeV
- $L / \sigma > 3$ w.r.t. beamspot
- Vtx CL $> 10\%$

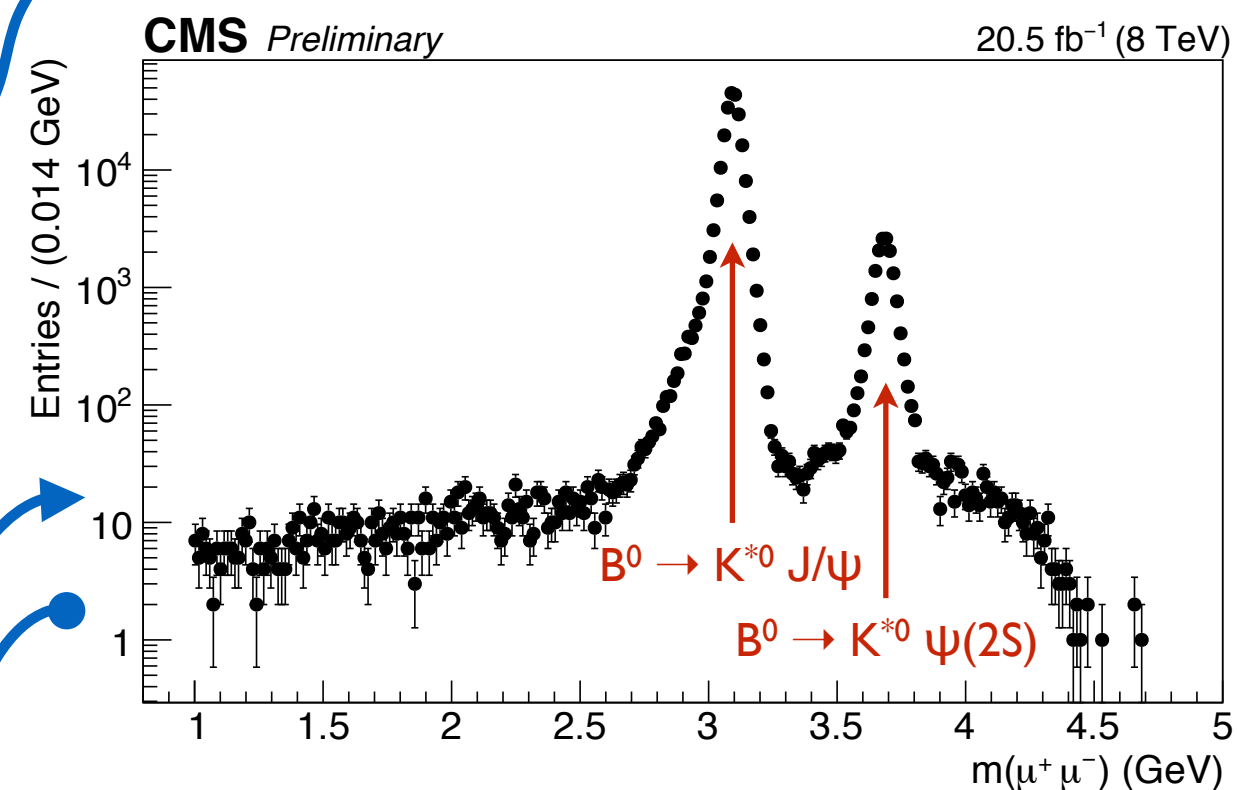
Both $K^+\pi^-$ and $K^-\pi^+$ mass hypothesis are computed

- $p_T > 0.8$ GeV
- $DCA / \sigma > 2$ w.r.t. beamspot
- $|\text{Im}(K\pi) - m(K^{*0}_{\text{PDG}})| < 90$ MeV at least one of the two mass hypothesis must lie in the window
- $m(KK) > 1.035$ ($\Phi(1020)$ particle rejection)

Two CP-states, $B^0 \rightarrow K^{*0} (K^+ \pi^-) \mu^+ \mu^-$ and $B^0_{\text{bar}} \rightarrow K^{*0}_{\text{bar}} (K^- \pi^+) \mu^+ \mu^-$, difficult to disentangle (no particle ID) $\rightarrow$ **CP-state assignment based on mass hypothesis closer to K^{*0} PDG mass (mistag rate $\sim 14\%$)**

Both B^0 and B^0_{bar} mass hypothesis are computed:

- $p_T > 8$ GeV
- $|\eta| < 2.2$
- $|\text{Im}(K\pi\mu\mu) - m(B^0)_{\text{PDG}}| < 280$ MeV for at least one of the two mass hypothesis
- Vtx. CL $> 10\%$
- $L / \sigma > 12$ w.r.t. beamspot
- $\cos(\alpha) > 0.9994$ angle in transverse plane between B^0 momentum and B^0 line of flight (w.r.t. beamspot)
- If more than one candidate $\rightarrow$ choose best B^0 vtx CL



Signal and control samples are treated identically
Signal candidates obtained by **J/ψ and ψ(2S) rejections**

Two channels can contribute to the final state $K^+ \pi^- \mu^+ \mu^-$:

- **P-wave** resonant channel, $K^+ \pi^-$ from the meson vector resonance K^{*0} decay
- **S-wave** non-resonant channel, $K^+ \pi^-$ don't come from any resonance

We have to parametrise both decay rates $\rightarrow$ **14** parameters $\rightarrow$ given the number events in **2012 data set**, we need to reduce number of free angular parameters to allow the fit to converge $\rightarrow$ exploit the odd symmetry of trigonometric functions, *i.e.* **fold** decay rate around $\Phi = 0$ and $\theta_l = \pi/2$

S-wave and S&P-wave interference

$$\frac{1}{d\Gamma/dq^2} \frac{d^4\Gamma}{dq^2 d\cos\theta_l d\cos\theta_K d\phi} = \frac{9}{8\pi} \left\{ \frac{2}{3} \left[(F_S + A_S \cos\theta_K) (1 - \cos^2\theta_l) + A_S^5 \sqrt{1 - \cos^2\theta_K} \sqrt{1 - \cos^2\theta_l} \cos\phi \right] + (1 - F_S) \left[2F_L \cos^2\theta_K (1 - \cos^2\theta_l) + \frac{1}{2} (1 - F_L) (1 - \cos^2\theta_K) (1 + \cos^2\theta_l) + \frac{1}{2} P_1 (1 - F_L) (1 - \cos^2\theta_K) (1 - \cos^2\theta_l) \cos 2\phi + 2P_5' \cos\theta_K \sqrt{F_L (1 - F_L)} \sqrt{1 - \cos^2\theta_K} \sqrt{1 - \cos^2\theta_l} \cos\phi \right] \right\}$$

P-wave

Decay rate depends upon **6** angular parameters:

- F_S, A_S, F_L : fixed to published CMS measurements on same data set (Φ integrated out)
- P_1, P_5' : measured parameters in this analysis (Φ dependance)
- A_S^5 : nuisance parameter

The probability density function

$$\begin{aligned}
 \text{p.d.f.}(m, \theta_K, \theta_l, \Phi) = & \boxed{Y_S^C} \left[\boxed{S^C(m)} \boxed{S^a(\theta_K, \theta_l, \phi)} \boxed{\epsilon^C(\theta_K, \theta_l, \phi)} \right. \\
 & \xrightarrow{\text{Mistag fraction}} + \frac{\boxed{f^M}}{1 - f^M} \boxed{S^M(m)} \boxed{S^a(-\theta_K, -\theta_l, \phi)} \boxed{\epsilon^M(\theta_K, \theta_l, \phi)} \left. \right] \\
 & + \boxed{Y_B B^m(m) B^{\theta_K}(\theta_K) B^{\theta_l}(\theta_l) B^\phi(\phi)},
 \end{aligned}$$

Correctly tagged events
Mistagged events
Background

- **Signal** contribution: **mass shape (double gaussian)**, **decay rate**, and **3D efficiency function**
- **Background** contribution: mass shape (exponential) and factorised polynomial functions for each angular variable

- Fit performed in two steps:
 1. Fit sidebands to determine background shape
 2. Fit whole mass spectrum, 5 free parameters:
 - signal (**Y_S**) and background (**Y_B**) yields
 - **P₁**, **P₅'**, and **A⁵_s** angular parameters

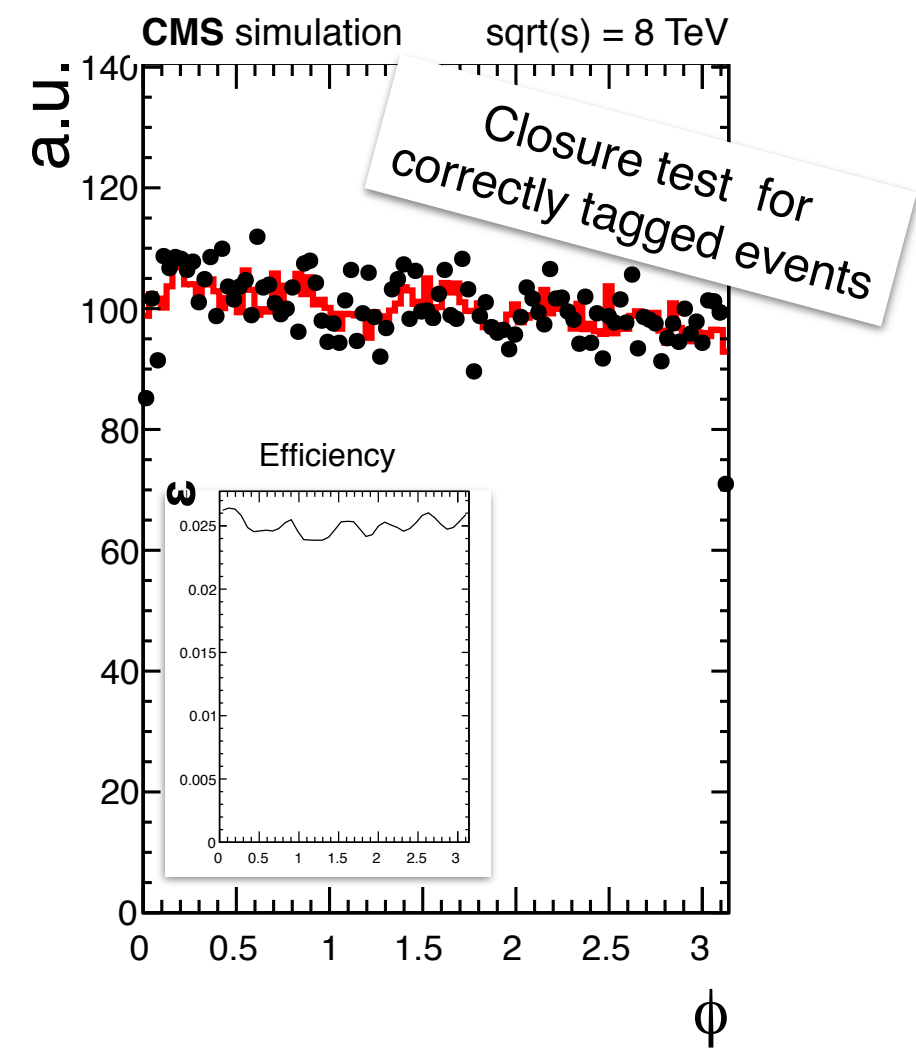
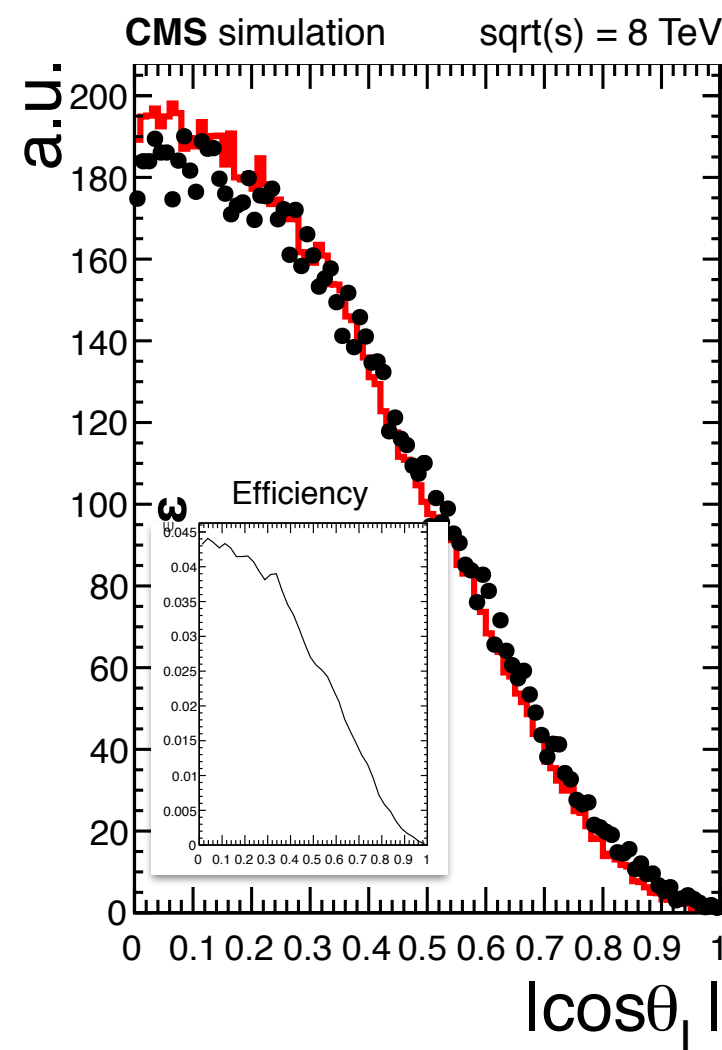
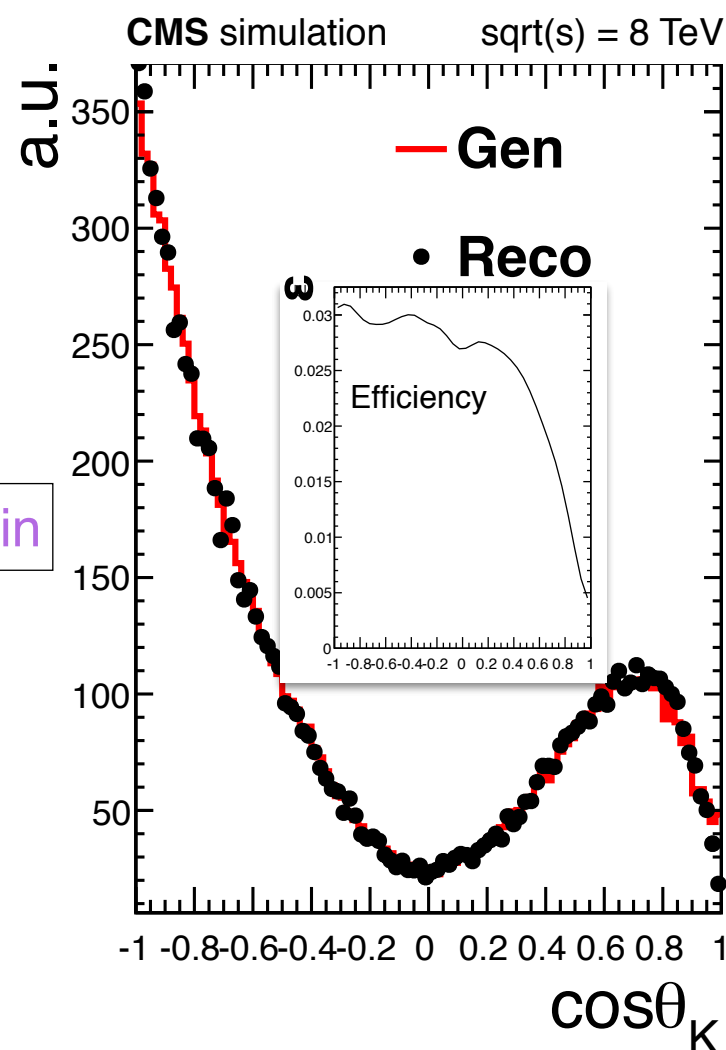
- Use unbinned extended maximum likelihood estimator
- Measurement performed 7 times (one in each q^2 bin)

q^2 bin index	$m^2(\mu\mu)$ (GeV ²)
1	1 – 2
2	2 – 4.3
3	4.3 – 6
4	6 – 8.68
5	10.9 – 12.86
6	14.18 – 16
7	16 – 19

- Numerator and denominator of efficiency are separately described with nonparametric technique implemented with a kernel density estimator on unbinned distributions
- Final efficiency distributions in the p.d.f. obtained from the ratio of 3D histograms derived from the sampling of the kernel density estimators

Closure test:

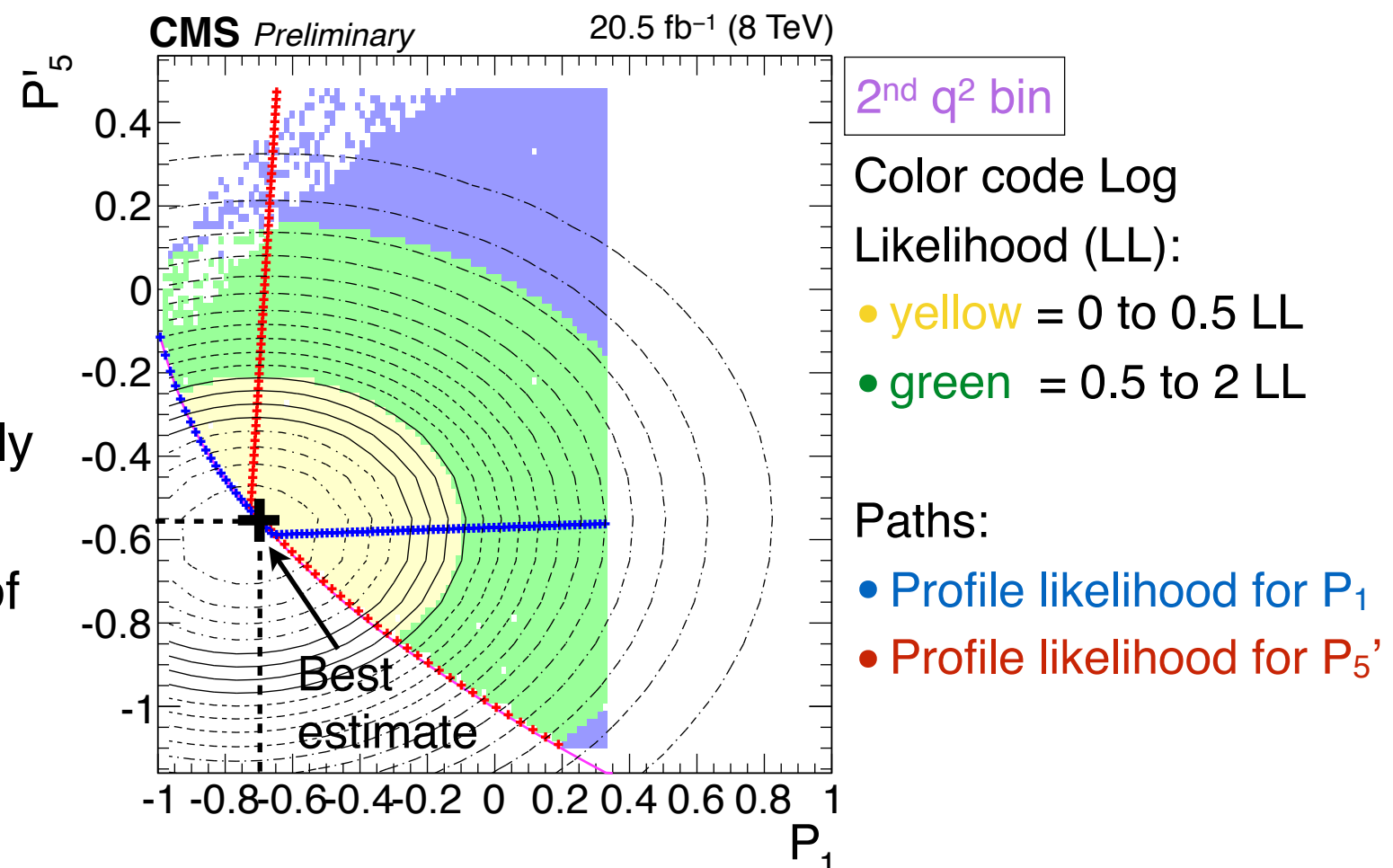
- compute efficiency with half of the MC simulation and use it to correct the other half
- same test performed both for correctly and mistagged events independently



An interesting statistical problem ...

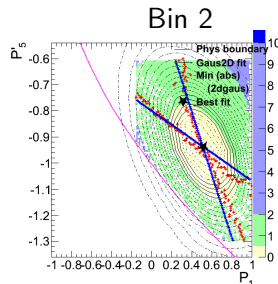
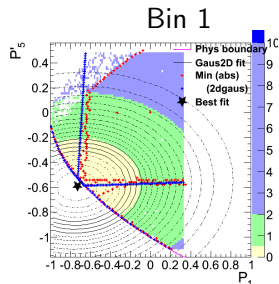
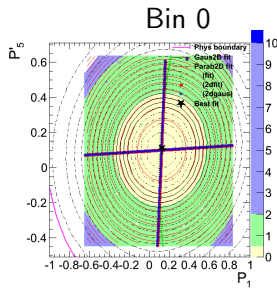
- The decay rate can become negative for certain values of the angular parameters (P_1 , P_5' , A_5^5)
- The presence of such a physically allowed region greatly complicates the numerical maximisation process of the likelihood by MINUIT and especially the error determination by MINOS, in particular next to the boundary between physical and unphysical regions
- The **best estimate** of P_1 and P_5' is computed by:
 - discretise the bi-dimensional space P_1 - P_5'
 - maximise the likelihood as a function of Y_S , Y_B , and A_5^5 at fixed values of P_1 , P_5'
 - fit the likelihood distribution with a 2D-gaussian function
 - the maximum of this function inside the physically allowed region is the best estimate

- To ensure correct coverage for the **uncertainties** of P_1 and P_5' , the Feldman-Cousins method is used in a simplified form: the confidence interval's construction is performed only along two 1D paths determined by profiling the 2D-gaussian description of the likelihood inside the physically allowed region



Procedure description

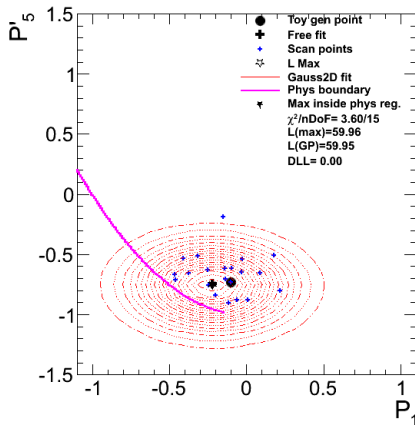
- start from the 2D $\mathcal{L}(P_1, P'_5)$ computed on data, taking into account the physical boundaries
- Then we fit it with a bivariate gaussian function and profile it vs P_1 and P'_5 , respectively, looking for maximum along the profile;
 - ▶ more robust than consider just the absolute maximum of the $\mathcal{L}$ along the profile.
 - ▶ if we hit a physical boundary, the minimum can be along the boundary itself
- Then we generate 100 (data-like size) toys using as input parameters P_1 and P'_5 .
 - ▶ To save CPU time not for all points, but we start around $\Delta \log \mathcal{L} = 0.5$



Procedure description (cont'ed)

Each toy is fitted with the full pdf as done for data

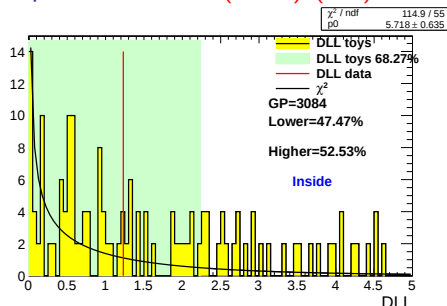
- we repeat the fit with 20 different set of 20 initial values of P_1 and P'_5
 - ▶ to find the absolute max, we fit the 20 values with a 2D gauss function
 - ▶ the max must be inside the physical region
- Eventually, we have 100 toys, and 100 values for the likelihood.



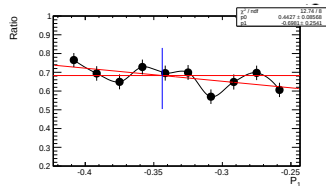
Procedure description (cont'ed)

- We compute $\Delta \log \mathcal{L}$ for each toy
 - ▶ compared with the min along the profile [black/yellow histo]→
 - ▶
- and $\Delta \log \mathcal{L}$ for data for that gen point
 - ▶ [red line]→
- **ratio** = (# toys with $\text{DLL}(\text{toy}) < \text{DLL}(\text{Data})$) / (#toys)
- If **ratio** < 68.27%
 - ▶ [green area]→
- then generation point is **inside** the 1σ boundary for data, otherwise it's **outside**.
- repeat for $P_1(P'_5)$ upper(lower) bound: 4 "directions"

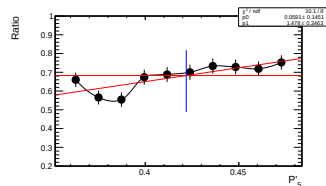
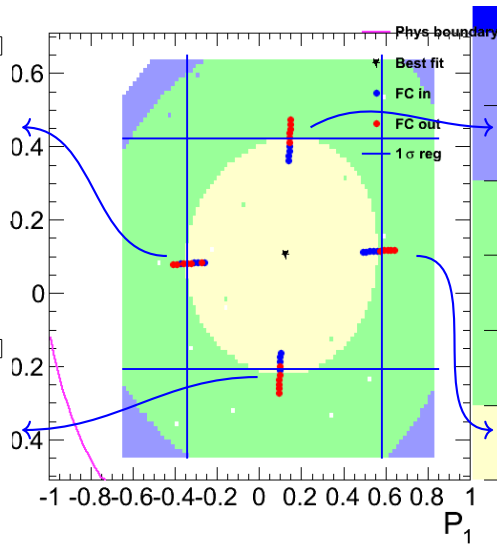
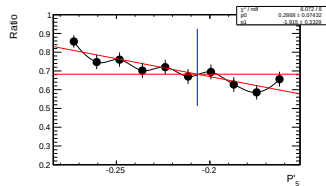
An example of DLL toys distribution compared with DLL(Data) (red)



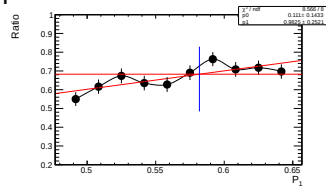
Bin 0 NEW



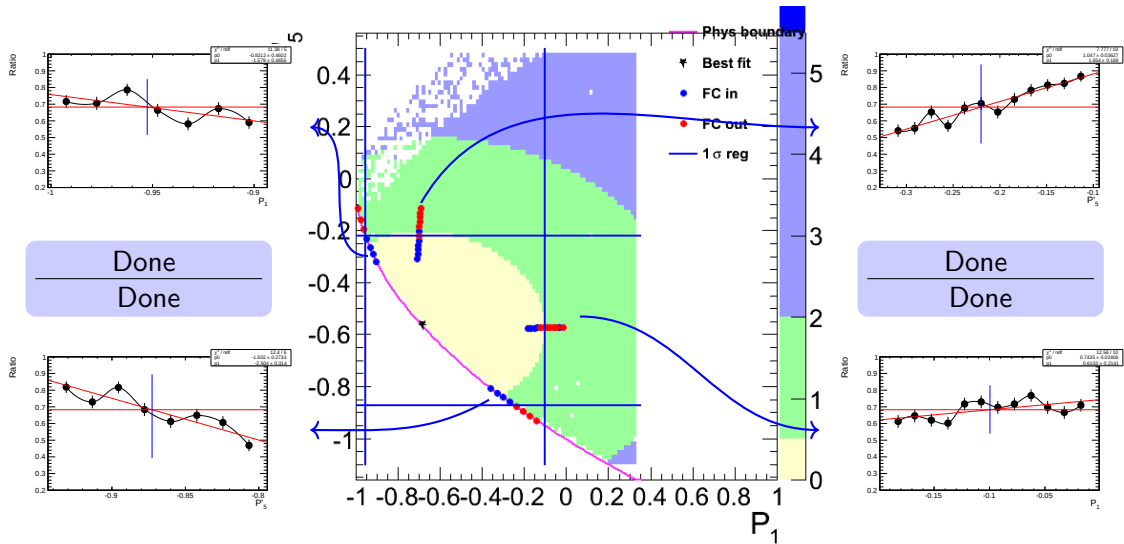
Done
Done



Done
Done



Bin 1 NEW



- Number of points in the P_1, P'_5 space investigated: 903
- Number of toys generated: 90 300
- Number of UML fit performed in total: 1 900 000
- Number of jobs submitted: $\sim 90\,000$
- Maximum number of jobs running at once: 750
- Average wall clock time for a job: $\sim 1.6\ h$
- Total wall clock time by all jobs: $\sim 5.2 \cdot 10^8\ s = 15\,000\ h = 6\,000\ d = 1.65\ y$
- Actual time spent so far ~ 2.5 month, not counting the two months spent by Alessio with his coverage study to try and demonstrate that this effort was not needed.
- and counting **STOP** ...

Comparison with $\Delta \log \mathcal{L} = 0.5$ Results and confidence level $\Delta \log \mathcal{L} = 0.5$

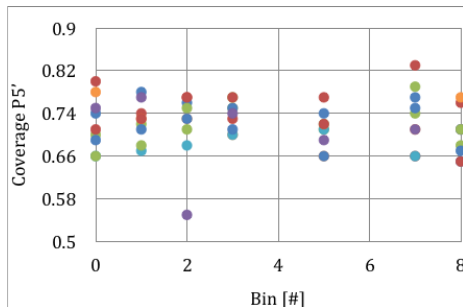
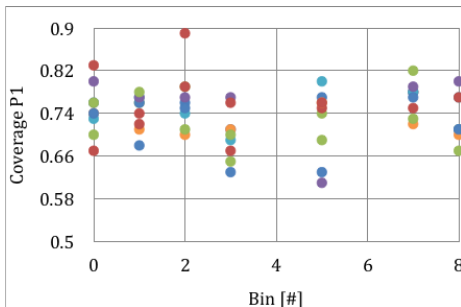
Bin		P_1				P'_5		
		FC	CM	Hyb		FC	CM	Hyb
0	0.12	+0.46 −0.47	+0.44 −0.463	+0.42 −0.447	0.10	+0.32 −0.31	+0.313 −0.333	+0.313 −0.333
1	−0.69	+0.58 −0.27	+0.59 −0.267	+0.537 −0.25	−0.57	+0.34 −0.31	+0.35 −0.29	+0.35 −0.29
2	0.53	+0.24 −0.33	+0.333 −0.36	+0.297 −0.32	−0.96	+0.22 −0.21	+0.23 −0.163	+0.23 −0.163
3	−0.47	+0.27 −0.23	+0.307 −0.25	+0.283 −0.23	−0.64	+0.15 −0.19	+0.18 −0.183	+0.18 −0.183
5	−0.53	+0.2 −0.14	+0.153 −0.137	+0.16 −0.14	−0.69	+0.11 −0.14	+0.097 −0.12	+0.107 −0.123
7	−0.33	+0.24 −0.23	+0.257 −0.23	+0.25 −0.227	−0.66	+0.13 −0.2	+0.143 −0.17	+0.143 −0.17
8	−0.53	+0.19 −0.19	+0.217 −0.21	+0.207 −0.2	−0.56	+0.12 −0.12	+0.137 −0.143	+0.137 −0.143

FC: Feldman-Cousins — CM: $DLL < 0.5$ — Hyb: bayesian approach on profiled $\mathcal{L}$

In red the most significant (?) differences

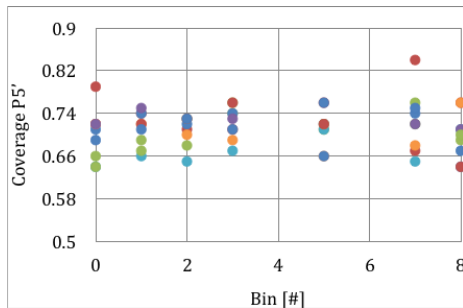
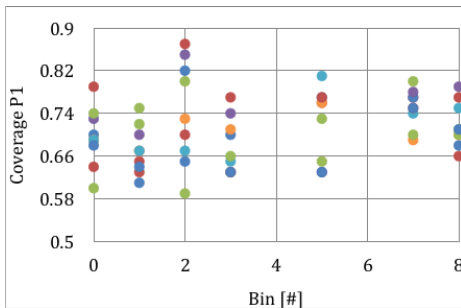
Custom-MINOS method

- The same idea as MINOS, but computed *by-hand* on the likelihood grid
- Looking for the outermost points in the scan with $\Delta NLL \leq 0.5$
- The boundary could affect the validity of this method
- The coverage was tested to be compatible with the expectations

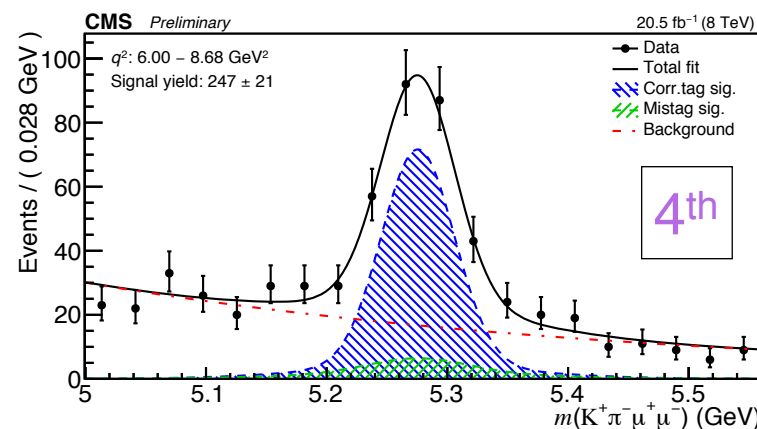
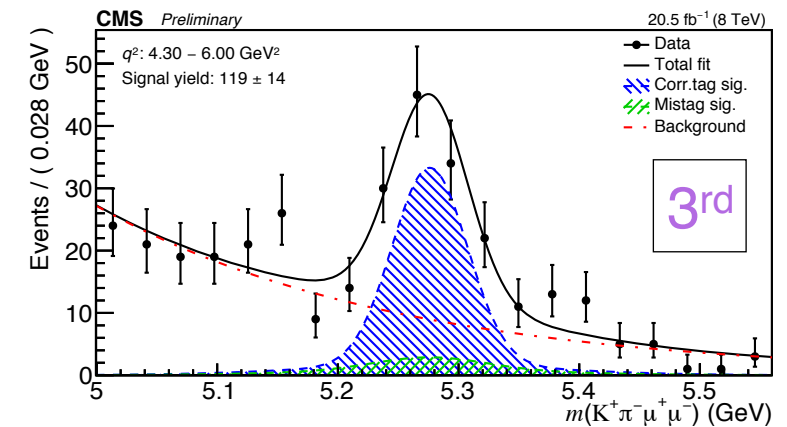
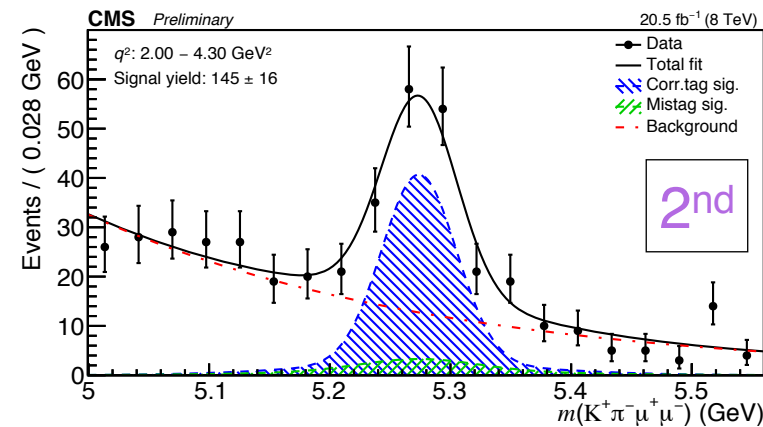
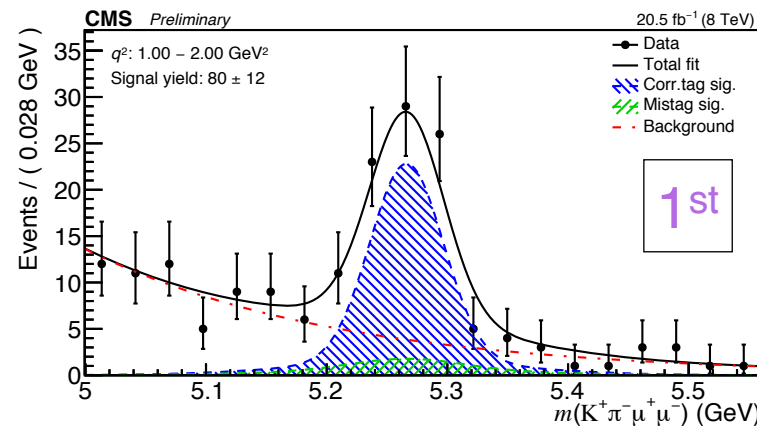


Hybrid-bayesian method

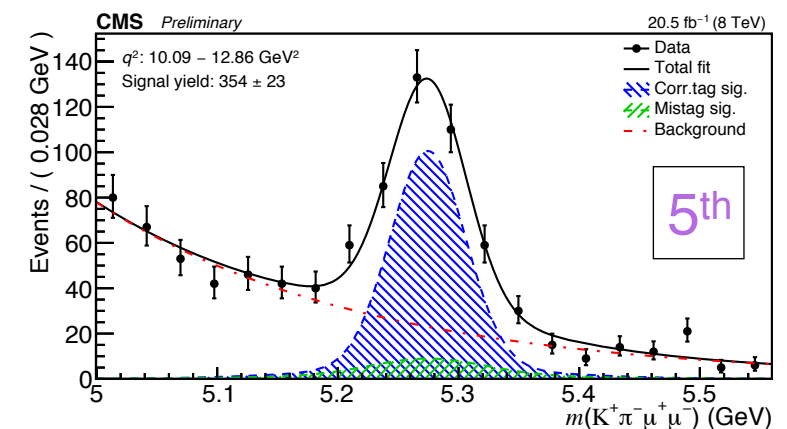
- For each parameter, the 2D likelihood scan is profiled to get a 1D function
- The Bayes theorem is applied to it, with a prior uniform inside the range of validity
- The confidence interval is defined to contain the 68% of the posterior distribution integral
- The coverage was tested to be compatible with the expectations



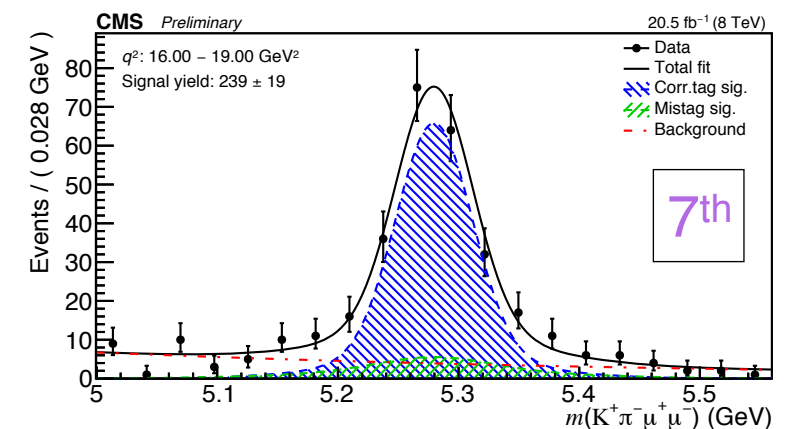
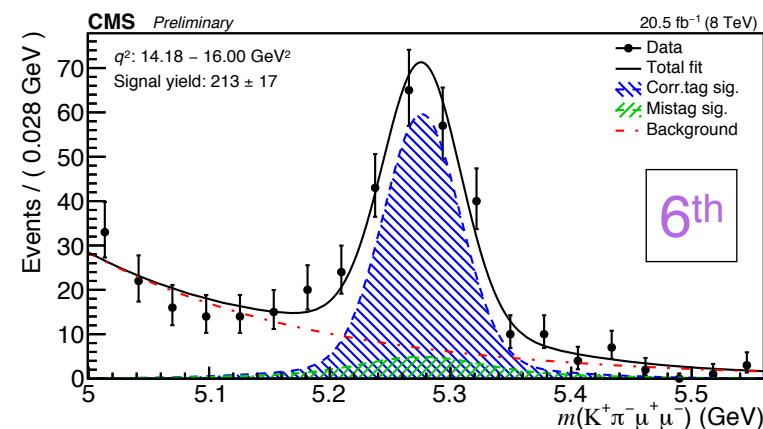
Signal evidence



$B^0 \rightarrow K^{*0} J/\psi$

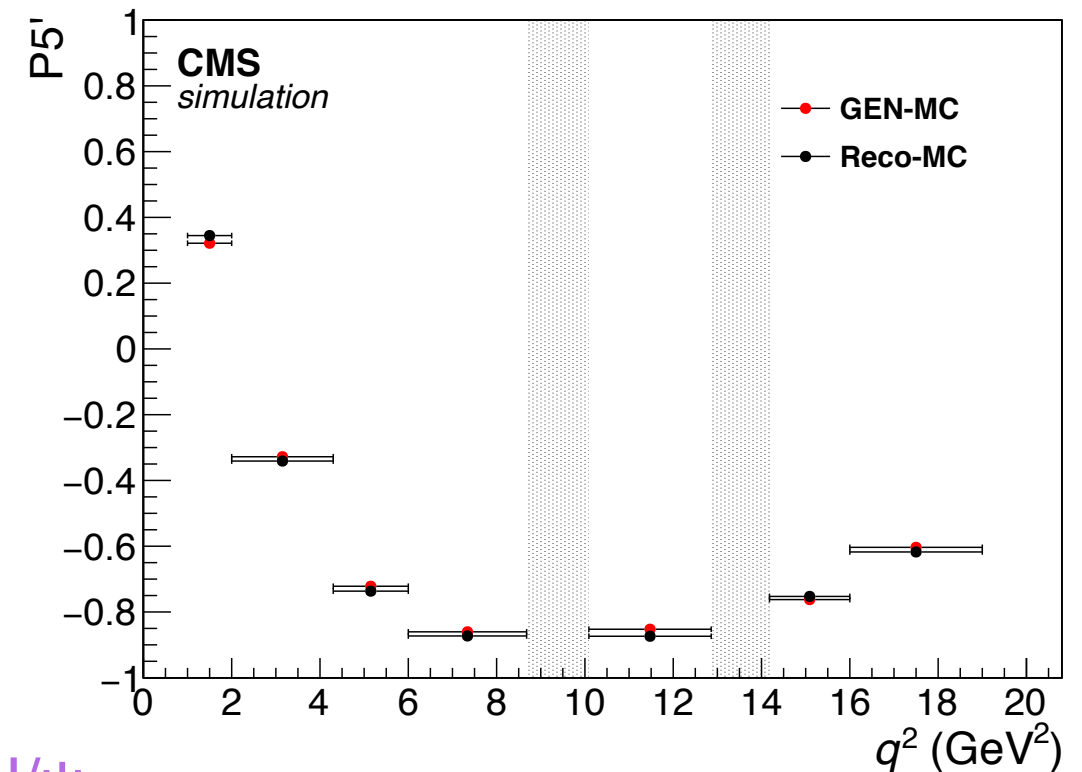
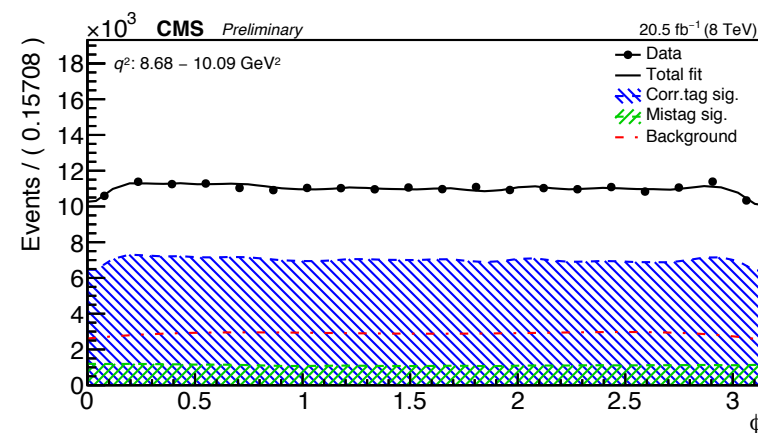
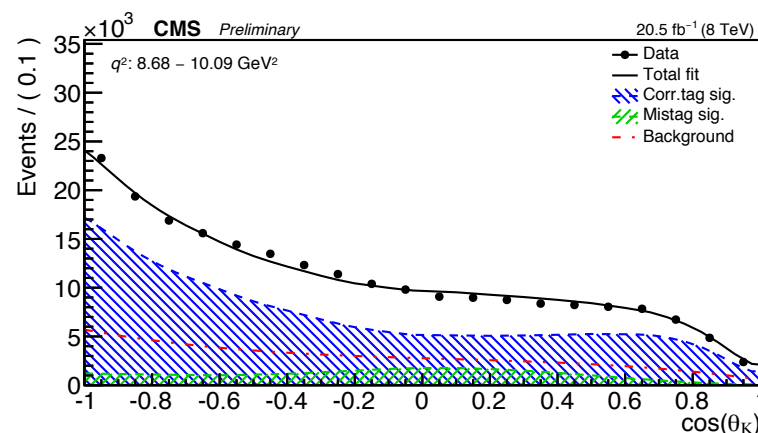
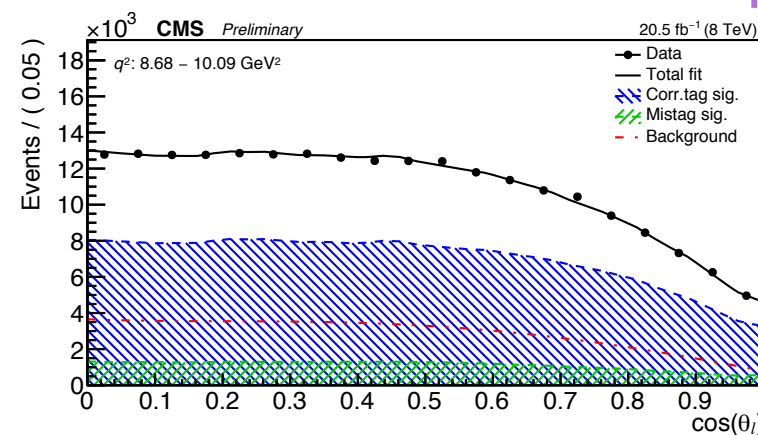
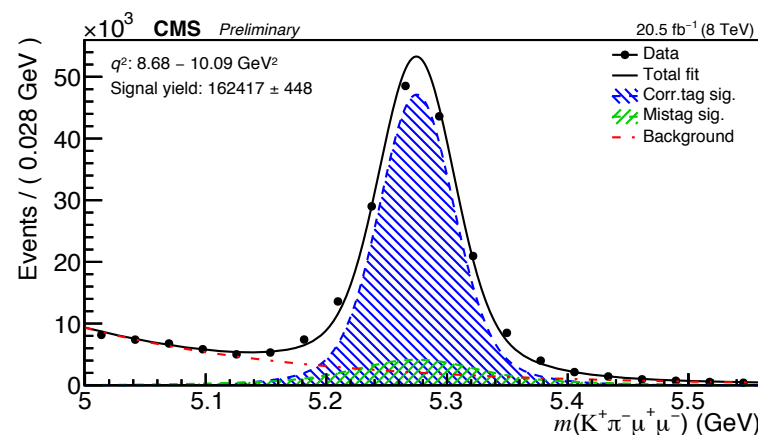


$B^0 \rightarrow K^{*0} \psi(2S)$



- Legend →
- Total fit
 - Signal, correctly tagged events
 - Signal, mistagged events
 - Background

- Several validation steps are performed with [simulation](#):
- with statistically precise MC signal sample: compare fit results with input values to the simulation
(**simulation mismodeling**)
 - with 200 data-like MC signal+background samples: compare average fit results with fit to the statistically precise MC signal sample (**fit bias**)
 - with pseudo-experiments


 $B^0 \rightarrow K^{*0} J/\psi$


Validation with [data](#) control channels:

- Fit performed with F_L free to vary
- The difference of F_L with respect to PDG value is propagated to the signal q^2 bins as systematic uncertainty (**efficiency**)

Systematic uncertainty	$P_1(10^{-3})$	$P'_5(10^{-3})$
Simulation mismodeling	1–33	10–23
Fit bias	5–78	10–119
MC statistical uncertainty	29–73	31–112
Efficiency	17–100	5–65
$K\pi$ mistagging	8–110	6–66
Background distribution	12–70	10–51
Mass distribution	12	19
Feed-through background	4–12	3–24
F_L, F_S, A_S uncertainty propagation	0–126	0–200
Angular resolution	2–68	0.1–12
Total systematic uncertainty	60–220	70–230

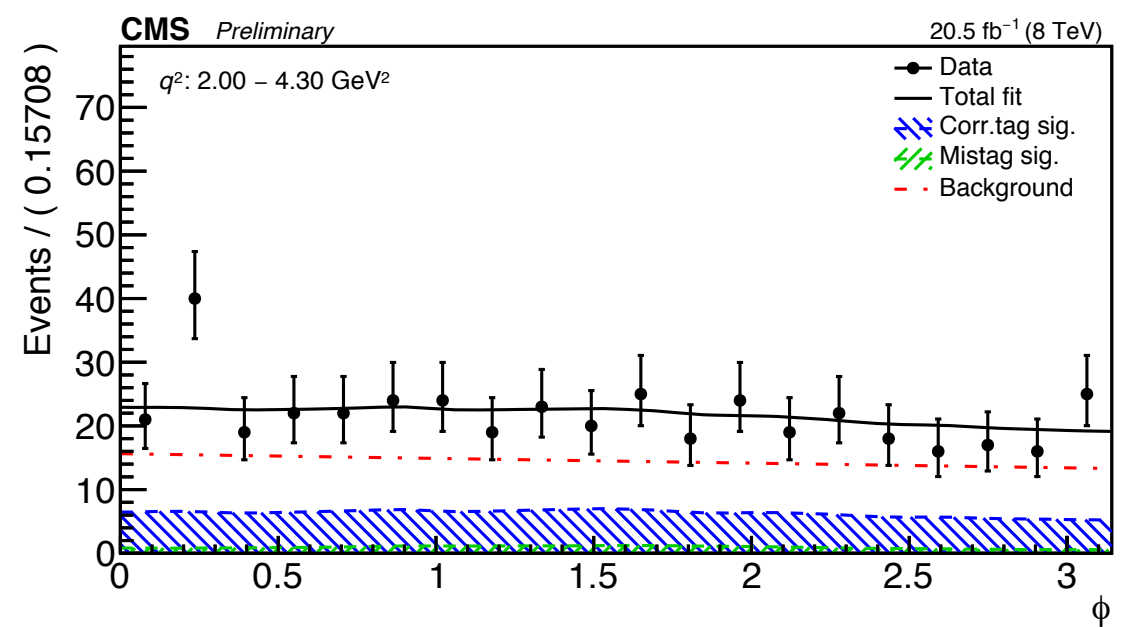
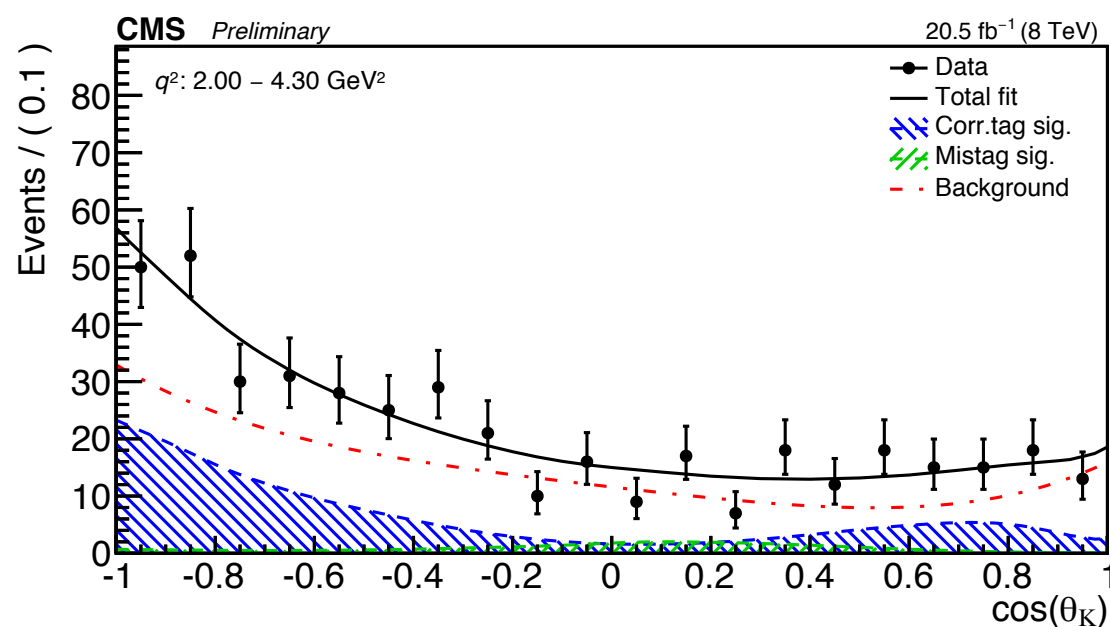
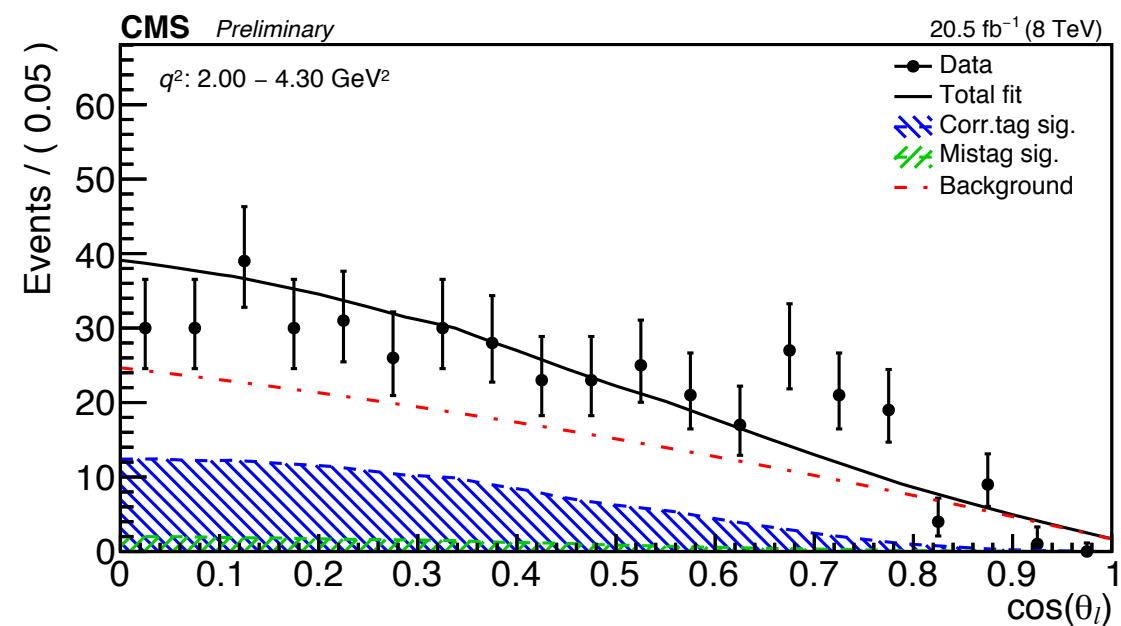
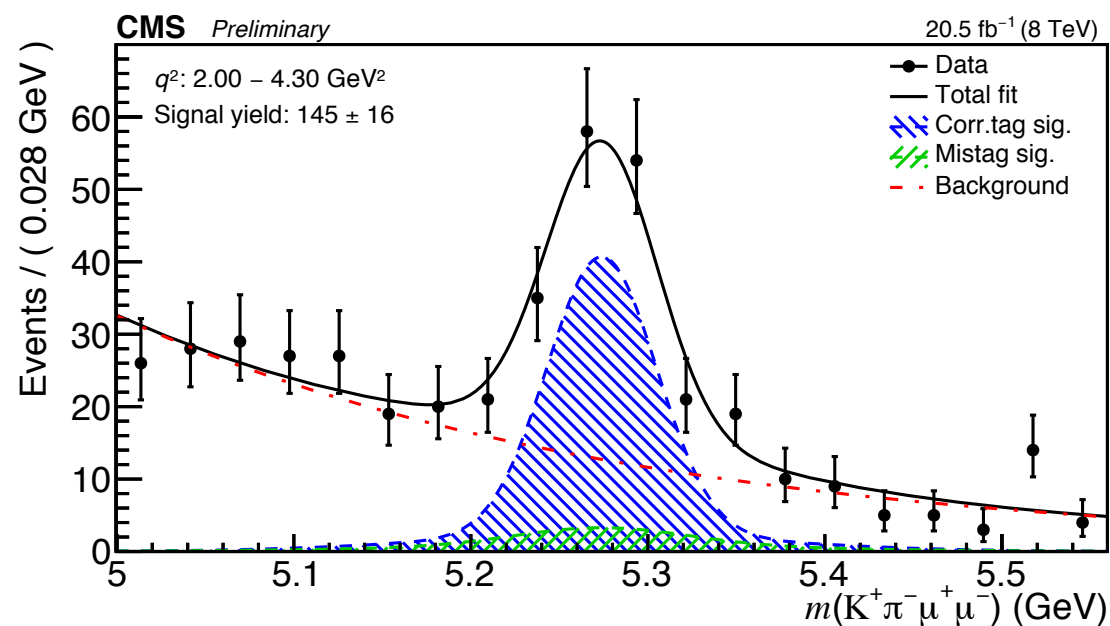
MC statistical uncertainty: fit data with 100 new efficiency distributions generated according to the simulation statistical uncertainty → effect of the different efficiency functions on final result is used to estimate the systematic uncertainty

$K\pi$ mistagging: mistag fraction free to vary in control channel $B^0 \rightarrow K^{*0} J/\psi \rightarrow$ discrepancy with respect to simulation is propagated to angular parameters

F_L, F_S , and A_S uncertainty propagation:

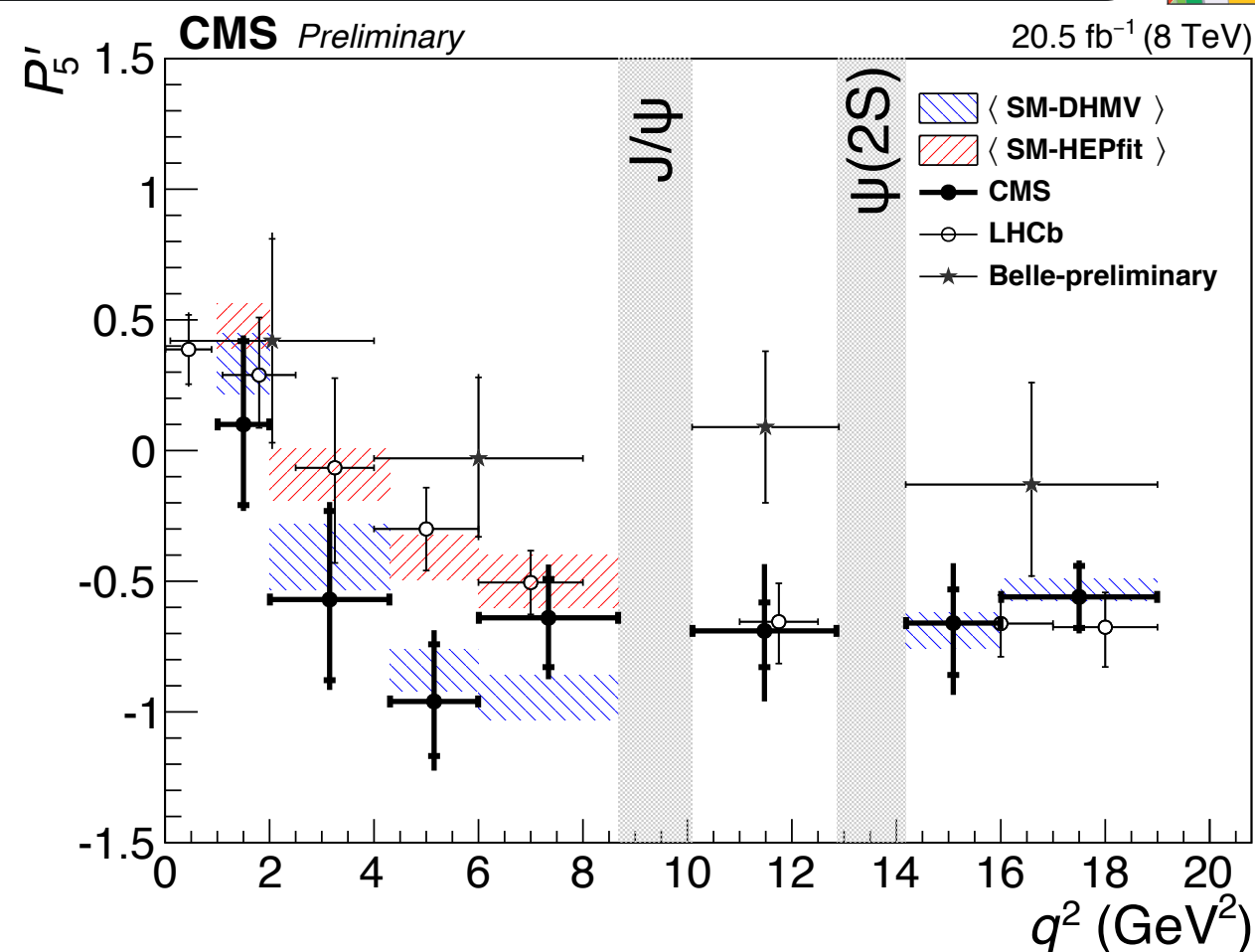
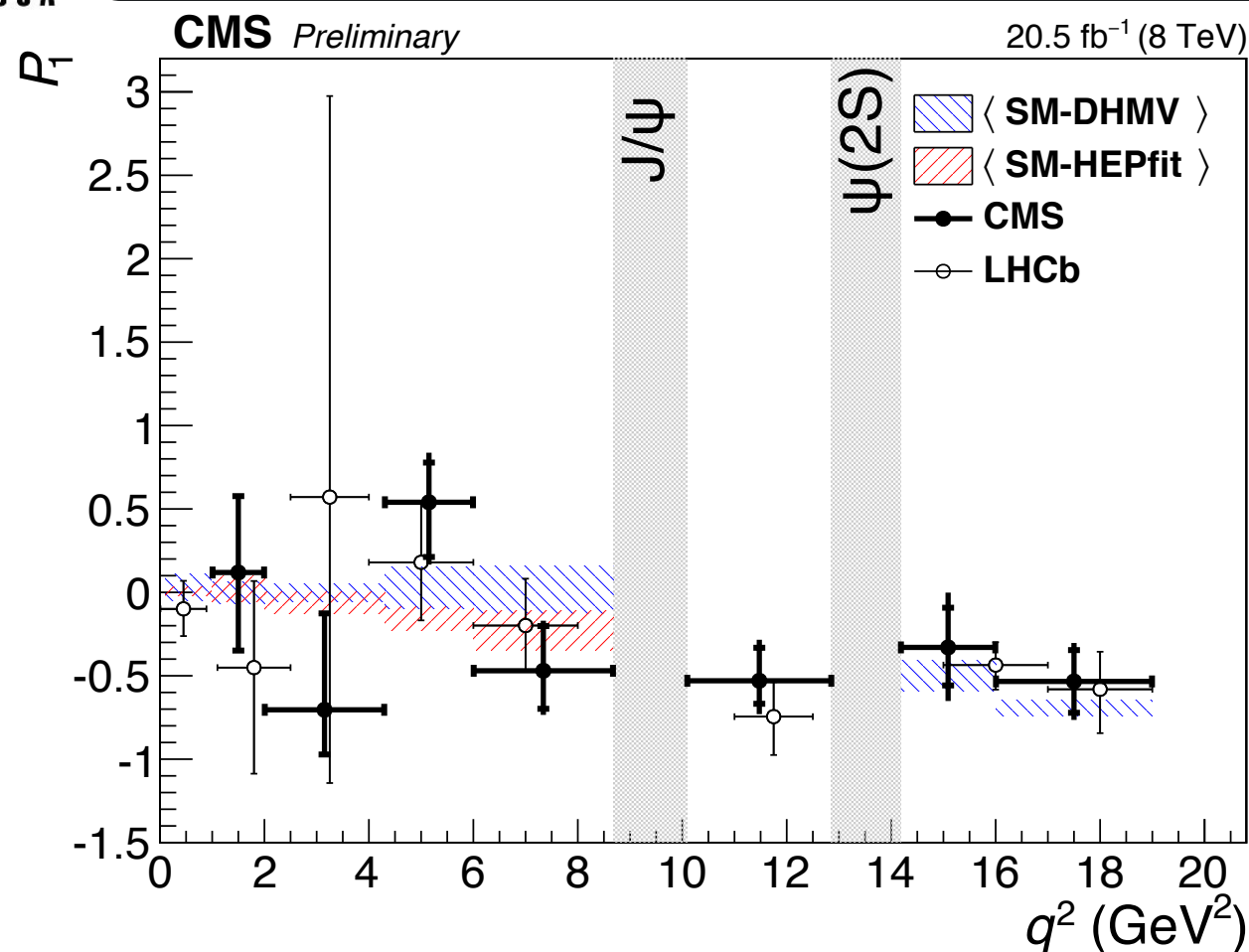
- Generate a statistically precise, $O(100 \times \text{data})$, pseudo-experiments (one per q^2 bin)
- Fit with all 6 angular parameters free to vary
- Fit with F_L, F_S , and A_S fixed
- Ratio of uncertainties between free and partially-fixed fit is used to compute the systematic uncertainty

Preliminary results: 2nd q^2 bin



Representative fit results: vertical bars give the statistical uncertainties, horizontal bars the bin width (fits to all other q^2 bins are in backup slides)

Preliminary results



- Inner vertical bars → statistical uncertainty
- Outer vertical bars → total uncertainty
- Horizontal bars → bin widths
- Statistical uncertainty is the dominant contribution but in 5th and 6th q^2 bins were it is comparable to systematic uncertainty

- **SM-DHNV** is computed using soft form factors in conjunction with parametrized power corrections, and with the hadronic charm-loop contribution derived from calculations
- **SM-HEPfit** uses full QCD computation of the form factors and derives the hadronic contribution from LHCb data

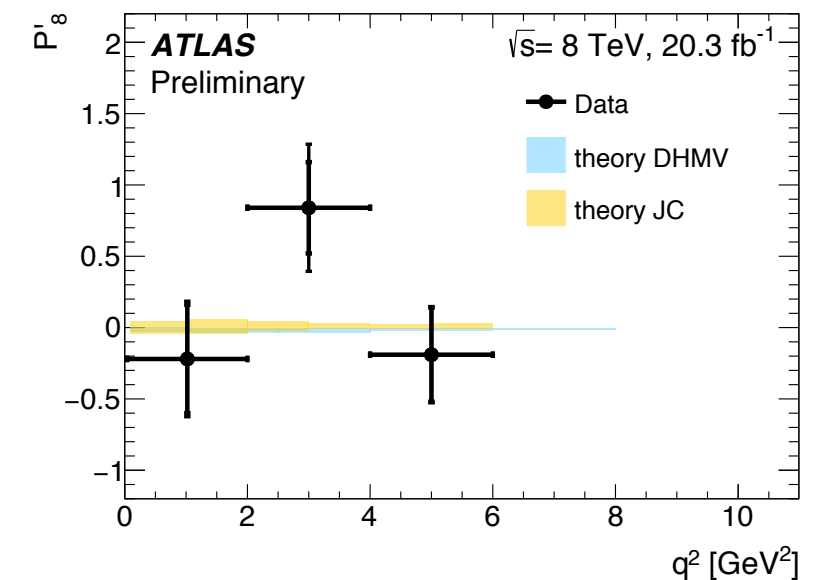
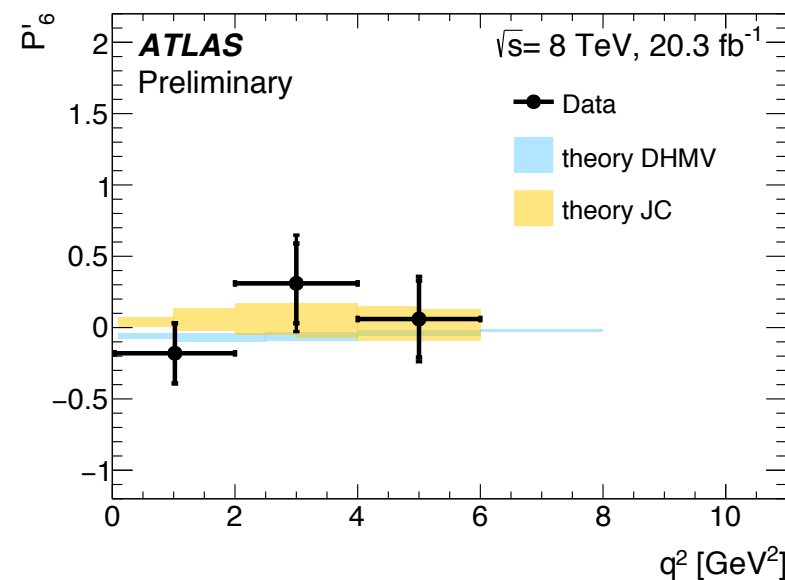
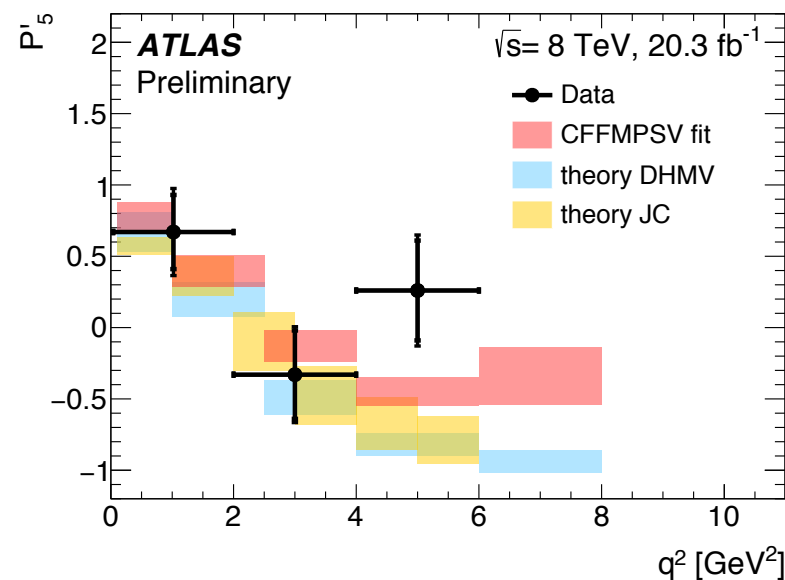
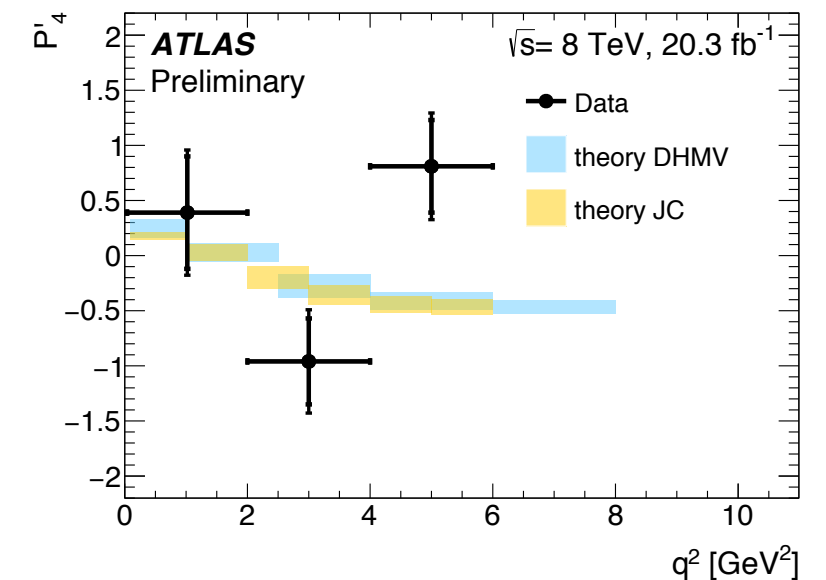
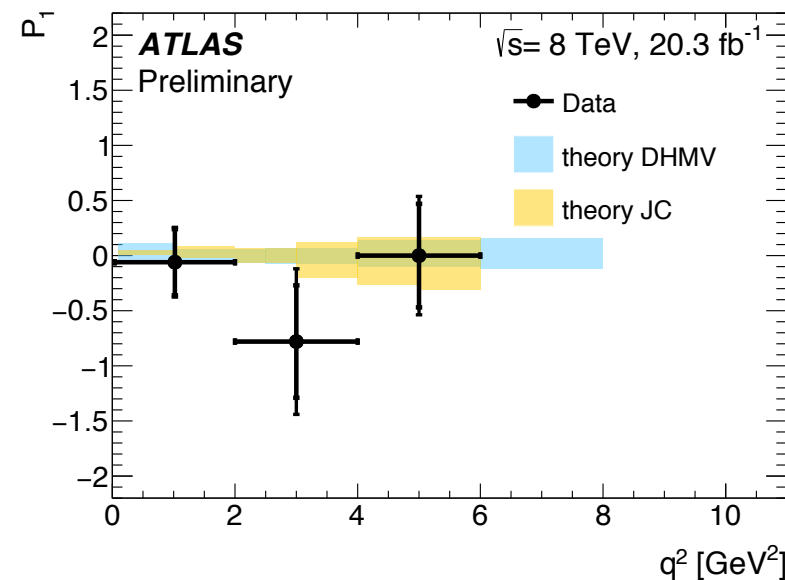
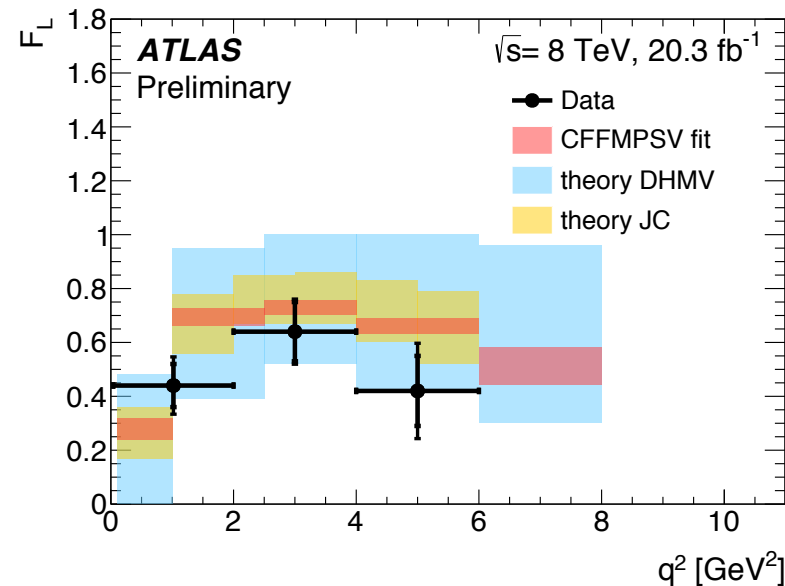
- LHCb: *JHEP* 02 (2016) 104
- Belle-preliminary: *arXiv:1612.05014*

- SM-DHNV: *JHEP* 01 (2013) 048, *JHEP* 05 (2013) 137
- SM-HEPfit: *JHEP* 06 (2016) 116, *arXiv:1611.04338*

Angular analysis results on $B_d \rightarrow K^* \mu^+ \mu^-$



❖ Results are compatible with theoretical calculations & fits:



CFFMPSV: Ciuchini et al.; JHEP **06** (2016) 116; arXiv:1611.04338.

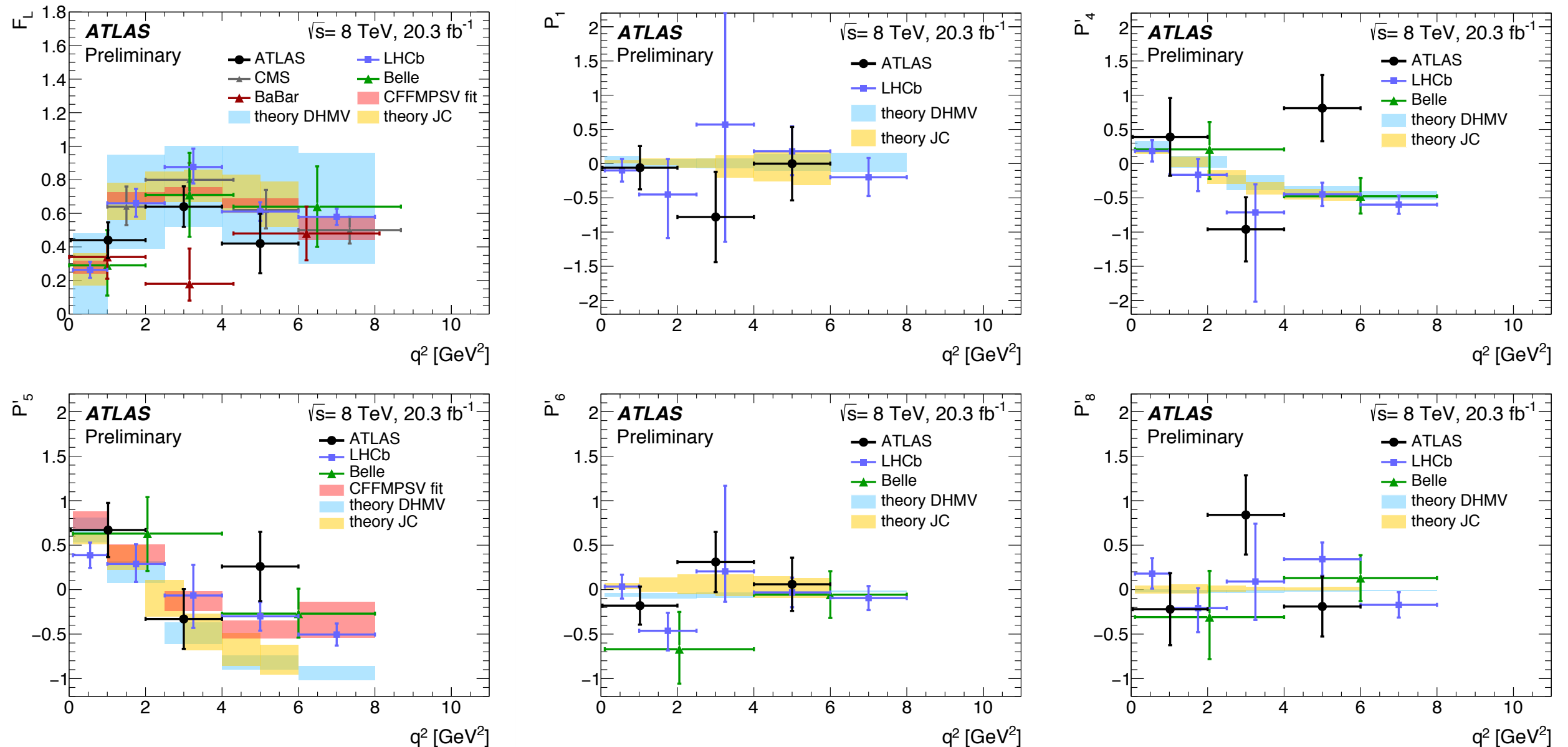
DMVH: Decotes-Genon et al.; JHEP **01** (2013) 048; JHEP **05** (2013) 137; JHEP **12** (2014) 125.

JC: Jäger-Camalich; JHEP **05** (2013) 043; Phys. Rev. **D93** (2016) 014028.

Angular analysis results on $B_d \rightarrow K^* \mu^+ \mu^-$



❖ Results are compatible with theoretical calculations & fits:



CFFMPSV: Ciuchini et al.; JHEP **06** (2016) 116; arXiv:1611.04338.

DMVH: Decotes-Genon et al.; JHEP **01** (2013) 048; JHEP **05** (2013) 137; JHEP **12** (2014) 125.

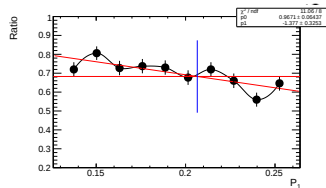
JC: Jäger-Camalich; JHEP **05** (2013) 043; Phys. Rev. **D93** (2016) 014028.



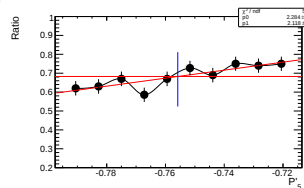
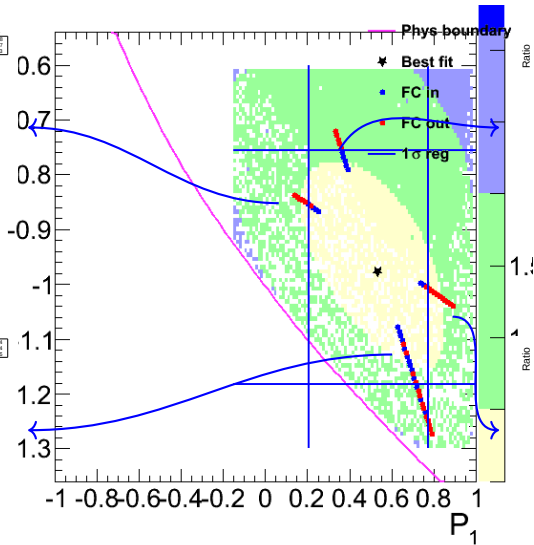
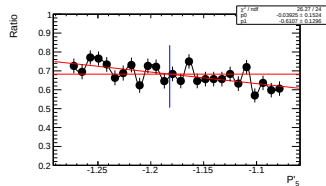
Additional stuff

Additional or backup slides

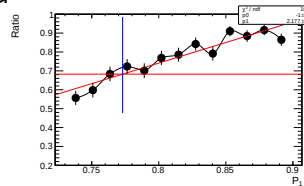
Bin 2 NEW



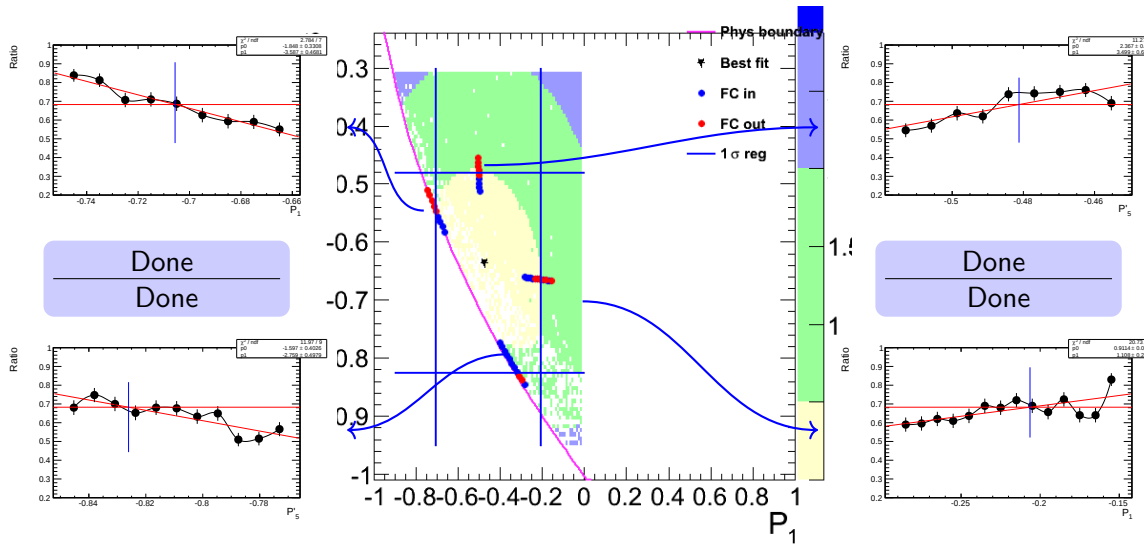
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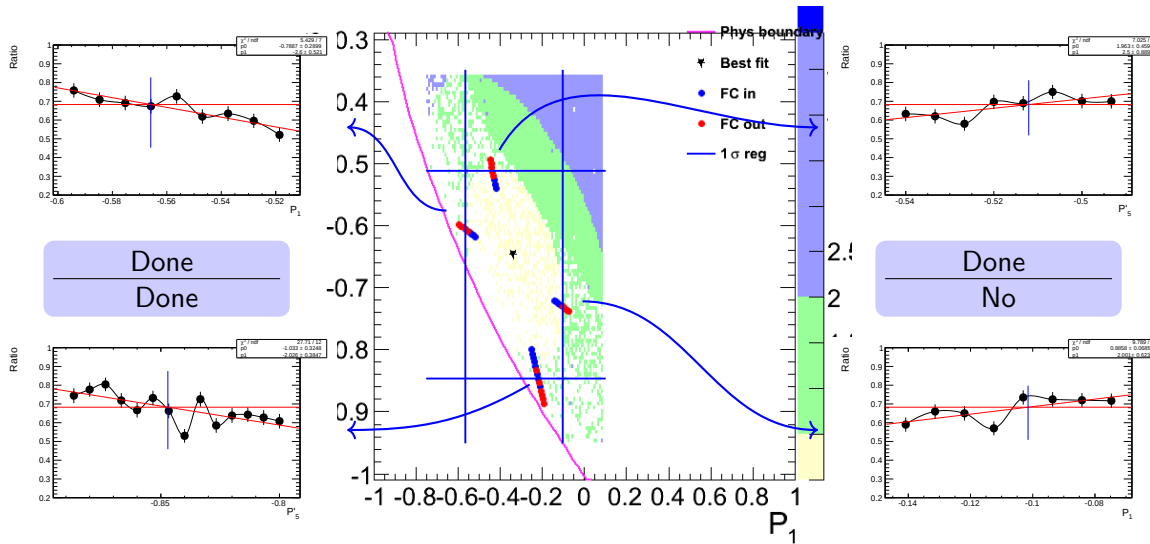
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Bin 3 NEW



Bin 7 NEW



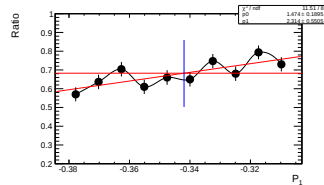
Done

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No



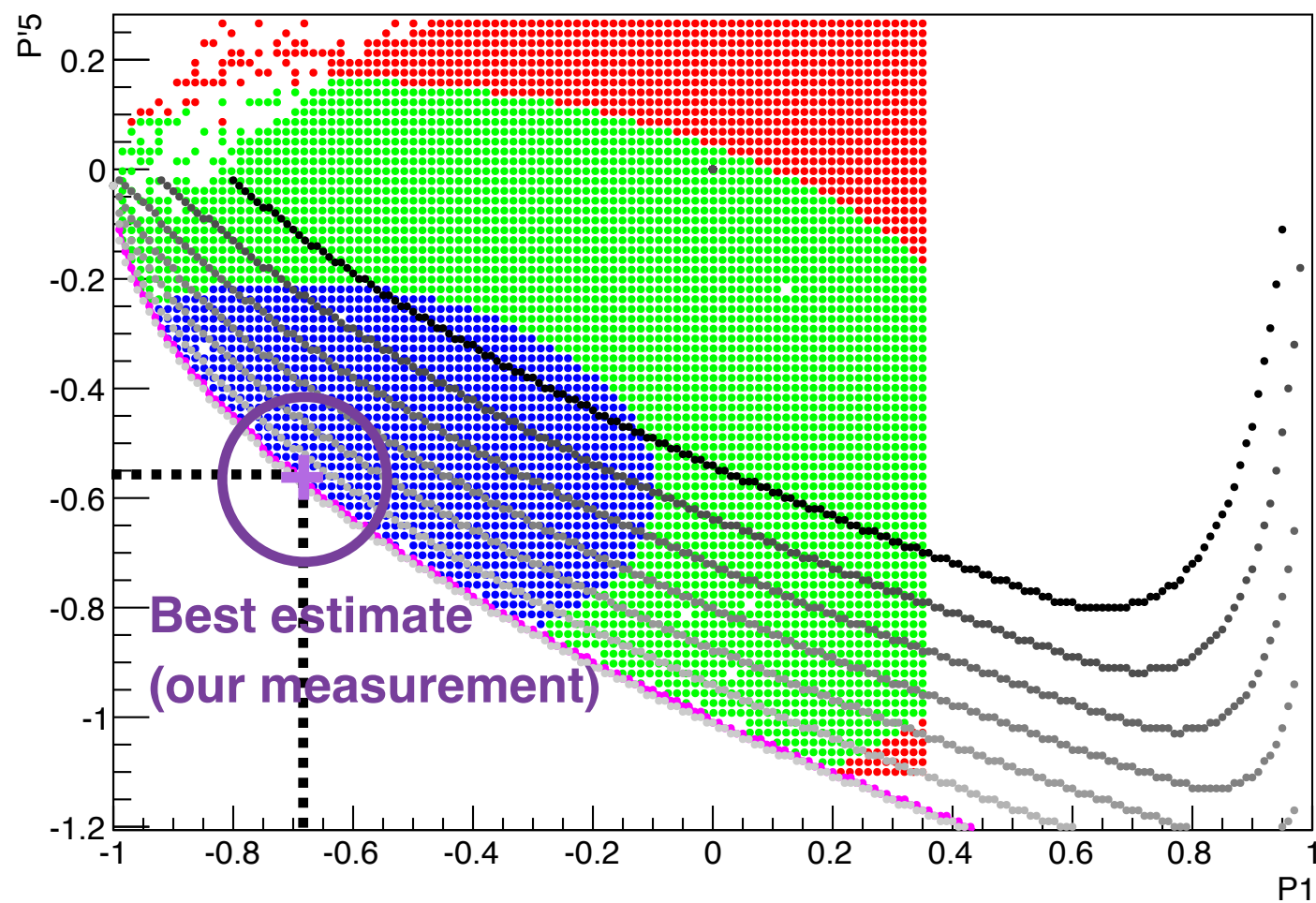


Proposed solution (“Custom MINOS”)

1. Discretise the P_1 - P_5 ' domain
2. Maximise the likelihood for $\mathbf{Y}_S$, $\mathbf{Y}_B$ and $\mathbf{A}^5_S$ at each point of the P_1 - P_5 ' domain
3. Best estimate of P_1 and P_5 ': point in the P_1 - P_5 ' domain with maximal likelihood
4. Fit likelihood distribution on the P_1 - P_5 ' domain at point **2.** with a 2D gaussian
5. Find the contour at $\Delta\text{NLL} = 0.5$ of the 2D gaussian in the physical domain
6. Statistical uncertainties: projection of the contour on the P_1 and P_5 ' axis

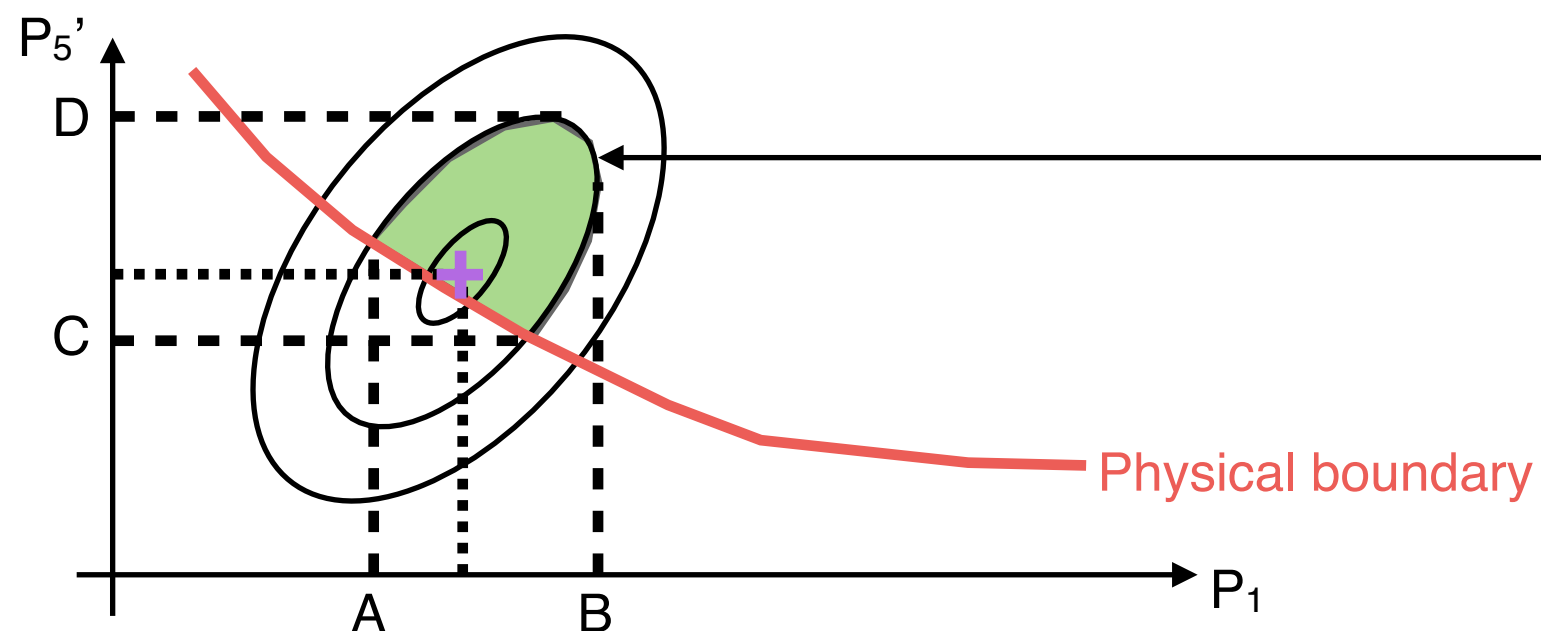
Justification for this method: it is well known that for a “well behaving” likelihood (e.g. not too skewed) the projection of $\Delta\text{NLL} = 0.5$ contour on both axis defines 68% confidence intervals

Alternative proposed solution: bin 1



Coloured region only meant to give a feeling about negative log likelihood (NLL) gradient

- blue = span 0 to $1/2 \Delta\text{NLL}$
- green = span 0.5 to $2 \Delta\text{NLL}$



- Fit coloured region with 2D gaussian
- Find contour at $0.5 \Delta\text{NLL}$ of 2D gaussian in physical domain
- Project the contour on the P_1 and P_5' axis to find statistical uncertainty

Proposed solution: “Hybrid frequentist-bayesian”

1. Discretise the P_1 - P_5 ' domain
2. Maximise the likelihood for $\mathbf{Y}_S$, $\mathbf{Y}_B$ and $\mathbf{A}^5_S$ at each point of the P_1 - P_5 ' domain
3. Best estimate of P_1 and P_5 ': point in the P_1 - P_5 ' domain with maximal likelihood
4. Fit likelihood distribution on the P_1 - P_5 ' domain at point **2.** with a 2D gaussian
5. Normalise the 2D gaussian to 1 in the physical domain
6. Statistical uncertainties: define intervals in which the profiled distributions, independently for P_1 and P_5 ', contain 68% of probability

Justification for this method: we apply the bayesian theorem to both the 1D profiled likelihood

Alternative proposed solution: bin 1

