

# Light Sterile Neutrinos

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Neutrino Unbound: <http://www.nu.to.infn.it>

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# In Memory of Hai-Wei Long



- ▶ Born 28 January 1984 in Guandong, China.
- ▶ PhD in October 2013 at the University of Science and Technology of China in Hefei.
- ▶ Postdoc in Torino from February 2014 to February 2015.
- ▶ Passed away 29 May 2015 in Guandong, China.

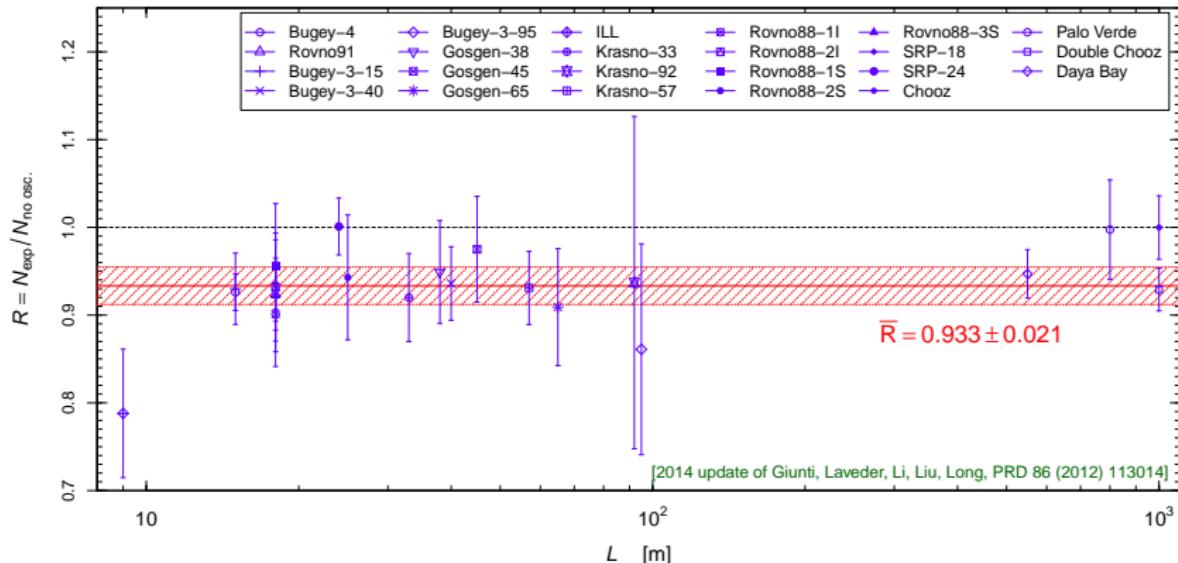
## Indications of SBL Oscillations Beyond $3\nu$

# Reactor Electron Antineutrino Anomaly

[Mention et al, PRD 83 (2011) 073006; update in White Paper, arXiv:1204.5379]

## New reactor $\bar{\nu}_e$ fluxes

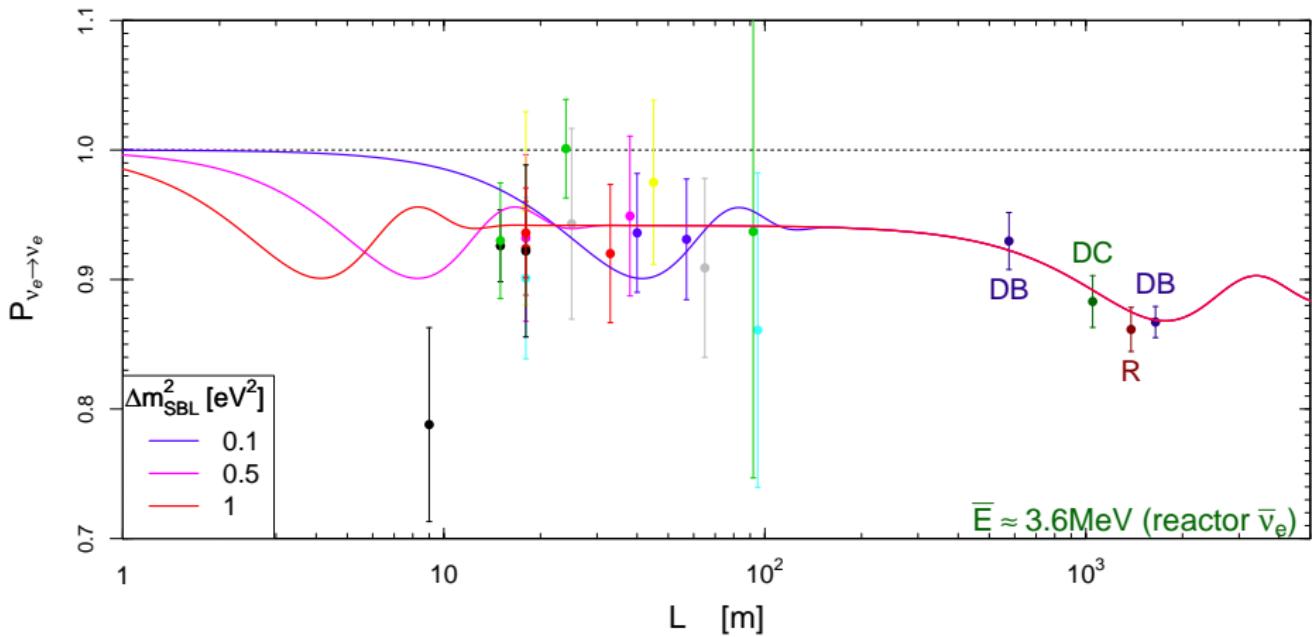
[Mueller et al, PRC 83 (2011) 054615; Huber, PRC 84 (2011) 024617]



[see also: Sinev, arXiv:1103.2452; Ciuffoli, Evslin, Li, JHEP 12 (2012) 110; Zhang, Qian, Vogel, PRD 87 (2013) 073018; Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050; Ivanov et al, PRC 88 (2013) 055501]

Problem: unknown  $\bar{\nu}_e$  flux uncertainties?

[Hayes, Friar, Garvey, Jonkmans, PRL 112 (2014) 202501; Dwyer, Langford, PRL 114 (2015) 012502]

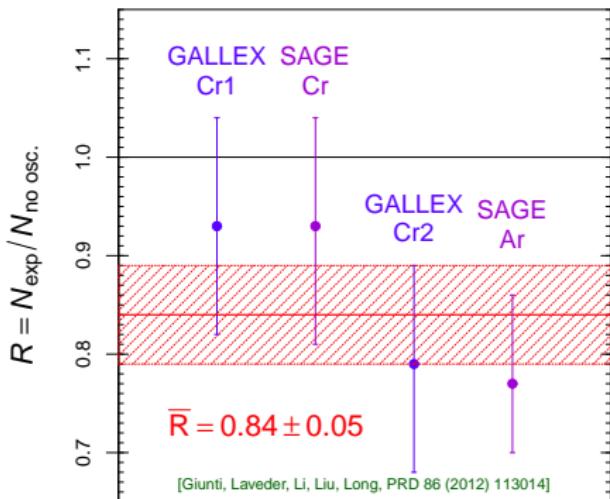


# Gallium Anomaly

## Gallium Radioactive Source Experiments: GALLEX and SAGE

Detection Process:  $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$

$\nu_e$  Sources:  $e^- + {}^{51}\text{Cr} \rightarrow {}^{51}\text{V} + \nu_e$        $e^- + {}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl} + \nu_e$



$\bar{\nu}_e \rightarrow \bar{\nu}_e$        $E \sim 0.7 \text{ MeV}$

$\langle L \rangle_{\text{GALLEX}} = 1.9 \text{ m}$

$\langle L \rangle_{\text{SAGE}} = 0.6 \text{ m}$

Nominal  $\approx 2.9\sigma$  anomaly

$\Delta m^2 \gtrsim 1 \text{ eV}^2$       ( $\gg \Delta m_A^2 \gg \Delta m_S^2$ )

[SAGE, PRC 73 (2006) 045805; PRC 80 (2009) 015807]

[Laveder et al, Nucl.Phys.Proc.Suppl. 168 (2007) 344;  
MPLA 22 (2007) 2499; PRD 78 (2008) 073009;  
PRC 83 (2011) 065504]

[Mention et al, PRD 83 (2011) 073006]

- ${}^3\text{He} + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + {}^3\text{H}$  cross section measurement [Frekers et al., PLB 706 (2011) 134]
- $E_{\text{th}}(\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-) = 233.5 \pm 1.2 \text{ keV}$  [Frekers et al., PLB 722 (2013) 233]

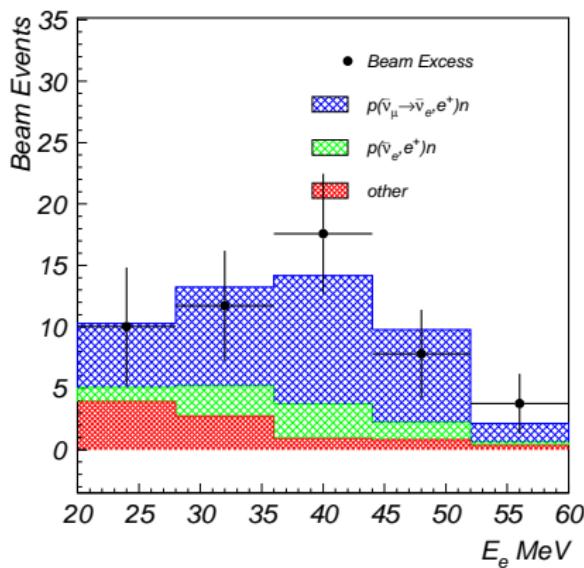
# LSND

[PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 30 \text{ m}$$

$$20 \text{ MeV} \leq E \leq 60 \text{ MeV}$$



Nominal  $\approx 3.8\sigma$  excess

$$\Delta m^2 \gtrsim 0.2 \text{ eV}^2 \quad (\gg \Delta m_A^2 \gg \Delta m_\zeta^2)$$

- ▶ Well known source of  $\bar{\nu}_\mu$ :  
 $\mu^+$  at rest  $\rightarrow e^+ + \nu_e + \bar{\nu}_\mu$
- ▶  $\bar{\nu}_\mu \xrightarrow[L \simeq 30 \text{ m}]{} \bar{\nu}_e$
- ▶ Well known detection process of  $\bar{\nu}_e$ :  
 $\bar{\nu}_e + p \rightarrow n + e^+$
- ▶ But signal not seen by KARMEN with same method at  $L \simeq 18 \text{ m}$

[PRD 65 (2002) 112001]

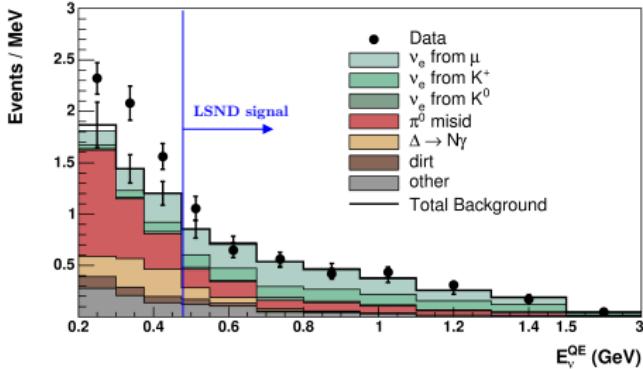
# MiniBooNE

$L \simeq 541 \text{ m}$

$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$

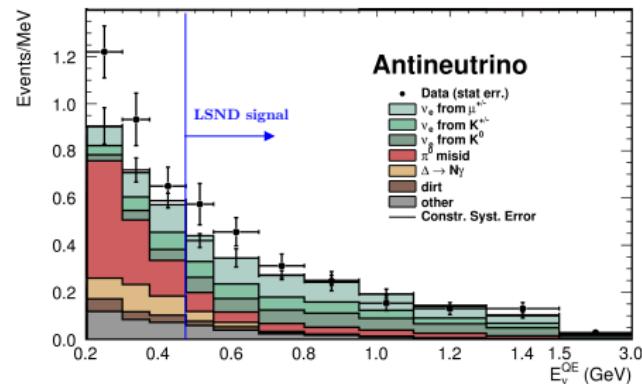
$$\nu_\mu \rightarrow \nu_e$$

[PRL 102 (2009) 101802]



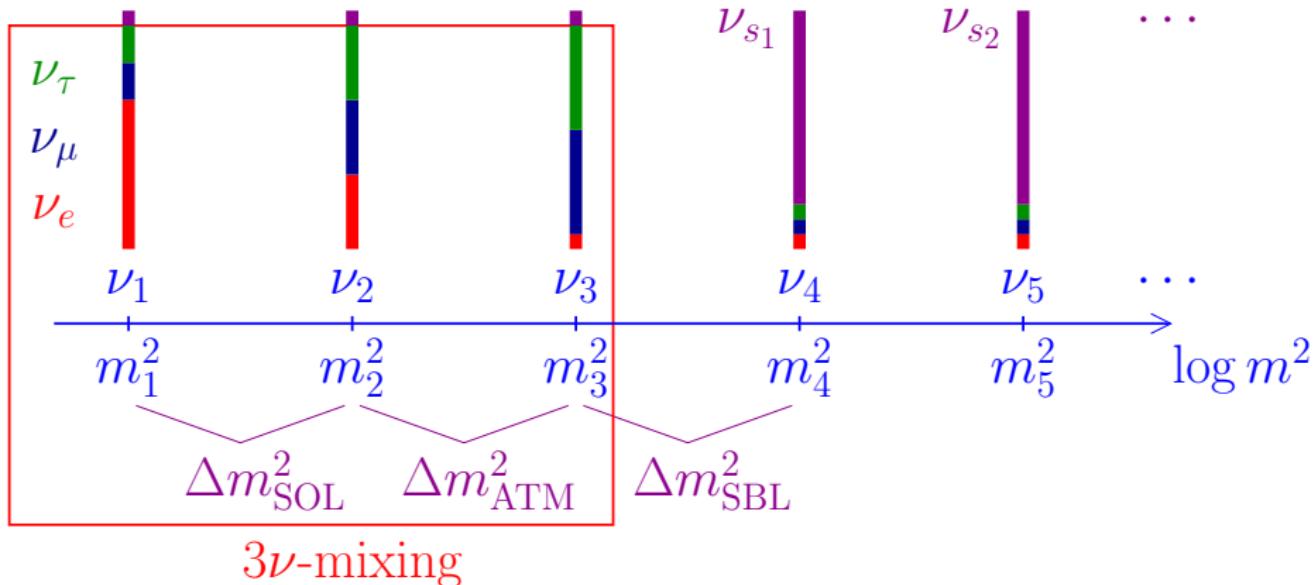
$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

[PRL 110 (2013) 161801]



- ▶ Purpose: check LSND signal.
- ▶ LSND signal:  $E > 475 \text{ MeV}$ .
- ▶ Different  $L$  and  $E$ .
- ▶ Agreement with LSND signal?
- ▶ Similar  $L/E$  (oscillations).
- ▶ CP violation?
- ▶ No money, no Near Detector.
- ▶ Low-energy anomaly!

# Beyond Three-Neutrino Mixing: Sterile Neutrinos



Terminology: a eV-scale sterile neutrino  
means: a eV-scale massive neutrino which is mainly sterile

# Sterile Neutrinos from Physics Beyond the SM

- ▶ Neutrinos are special in the Standard Model: the only **neutral fermions**
- ▶ Active left-handed neutrinos can mix with non-SM singlet fermions often called **right-handed neutrinos**      **Neutrino Portal** [A. Smirnov, arXiv:1502.04530]
- ▶ Light anti- $\nu_R$  are **light sterile neutrinos**

$$\nu_R^c \rightarrow \nu_{sL} \quad (\text{left-handed})$$

- ▶ Sterile means **no standard model interactions**

[Pontecorvo, Sov. Phys. JETP 26 (1968) 984]

- ▶ Active neutrinos ( $\nu_e, \nu_\mu, \nu_\tau$ ) can oscillate into light sterile neutrinos ( $\nu_s$ )
- ▶ Observables:
  - ▶ **Disappearance** of active neutrinos (neutral current deficit)
  - ▶ Indirect evidence through **combined fit of data** (current indication)
- ▶ Short-baseline anomalies +  $3\nu$ -mixing:

$$\Delta m_{21}^2 \ll |\Delta m_{31}^2| \ll |\Delta m_{41}^2| \leq \dots$$

$\nu_1$	$\nu_2$	$\nu_3$	$\nu_4$	$\dots$
$\nu_e$	$\nu_\mu$	$\nu_\tau$	$\nu_{s1}$	$\dots$

# Effective SBL Oscillation Probabilities in 3+1 Schemes

$$P_{\nu_\alpha \rightarrow \nu_\beta}^{\text{SBL}} \simeq \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

$$P_{\nu_\alpha \rightarrow \nu_\alpha}^{\text{SBL}} \simeq 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

Perturbation of 3ν Mixing:  $|U_{e4}|^2 \ll 1$ ,  $|U_{\mu 4}|^2 \ll 1$ ,  $|U_{\tau 4}|^2 \ll 1$ ,  $|U_{s4}|^2 \simeq 1$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

↑  
SBL

- ▶ 6 mixing angles
- ▶ 3 Dirac CP phases
- ▶ 3 Majorana CP phases
- ▶ But CP violation is not observable in current SBL experiments!
- ▶ Observable in LBL accelerator exp. sensitive to  $\Delta m_{\text{ATM}}^2$  [de Gouvea, Kelly, Kobach, PRD 91 (2015) 053005; Klop, Palazzo, PRD 91 (2015) 073017] and solar exp. sensitive to  $\Delta m_{\text{SOL}}^2$  [Long, Li, Giunti, PRD 87, 113004 (2013) 113004]

## 3+1: Appearance vs Disappearance

- ▶ Amplitude of  $\nu_e$  disappearance:

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2$$

- ▶ Amplitude of  $\nu_\mu$  disappearance:

$$\sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu 4}|^2 (1 - |U_{\mu 4}|^2) \simeq 4|U_{\mu 4}|^2$$

- ▶ Amplitude of  $\nu_\mu \rightarrow \nu_e$  transitions:

$$\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$$

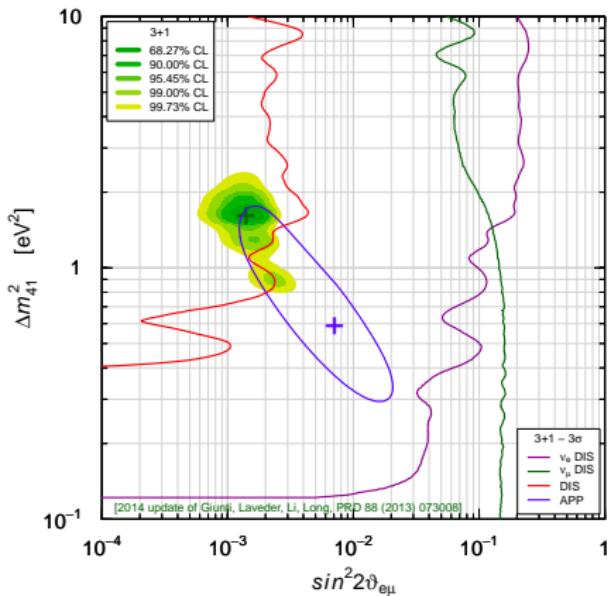
- ▶ Upper bounds on  $\nu_e$  and  $\nu_\mu$  disappearance  $\Rightarrow$  strong limit on  $\nu_\mu \rightarrow \nu_e$

[Okada, Yasuda, IJMPA 12 (1997) 3669; Bilenky, Giunti, Grimus, EPJC 1 (1998) 247]

- ▶ Similar constraint in 3+2, 3+3, ..., 3+N<sub>s</sub> !

# Global 3+1 Fit

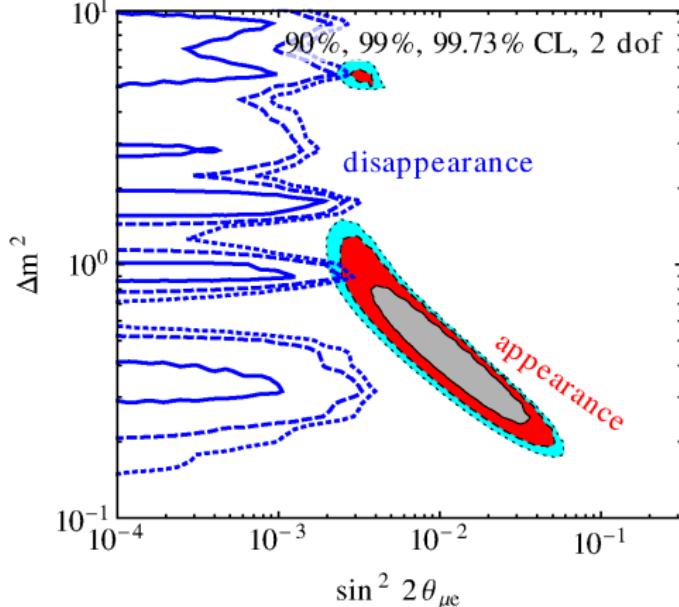
Our Fit



$$\text{GoF} = 5\%$$

$$\text{PGoF} = 0.1\%$$

Kopp, Machado, Maltoni, Schwetz

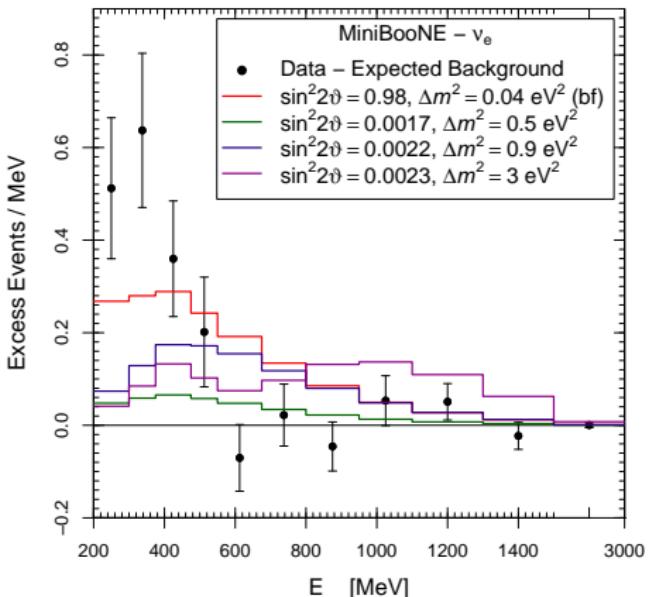
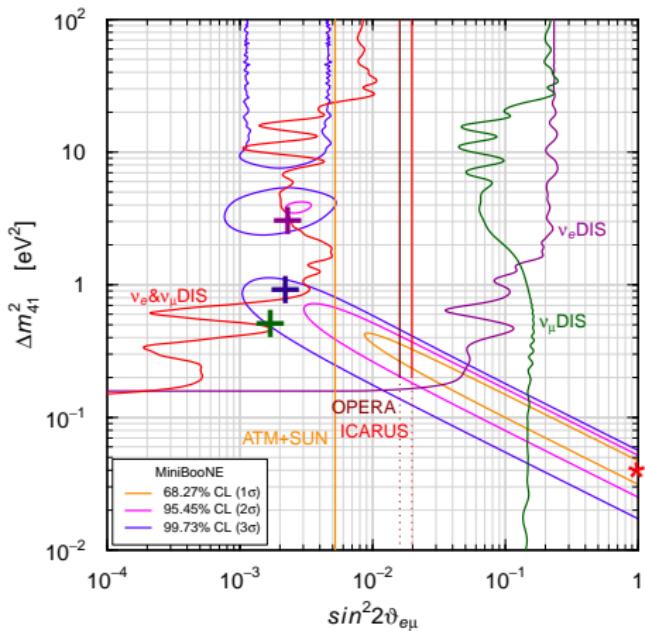


$$\text{GoF} = 19\%$$

$$\text{PGoF} = 0.01\%$$

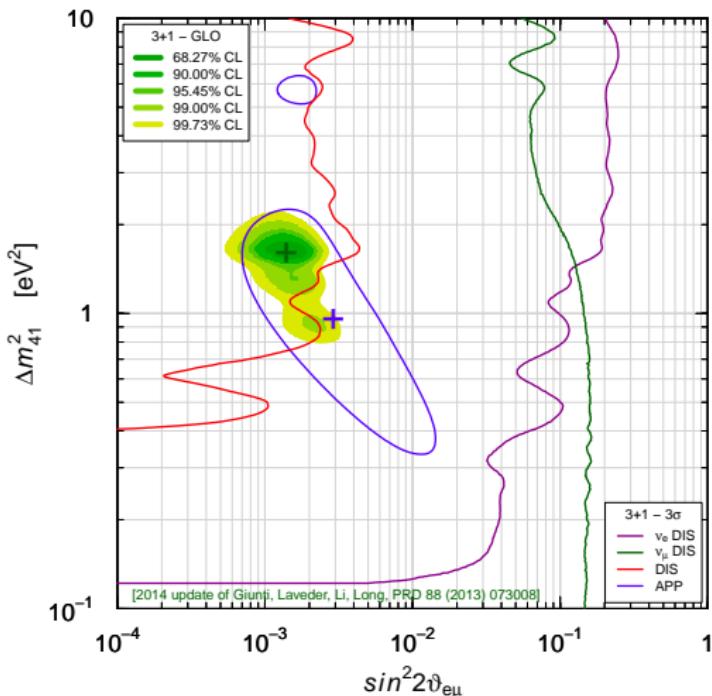
[Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050]

# MiniBooNE Low-Energy Excess?



- ▶ No fit of low-energy excess for realistic  $\sin^2 2\theta_{e\mu} \lesssim 3 \times 10^{-3}$
- ▶ Neutrino energy reconstruction problem? [Martini, Ericson, Chanfray, PRD 87 (2013) 013009]
- ▶ MB low-energy excess is the main cause of bad APP-DIS PGOf = 0.1%
- ▶ Pragmatic Approach: discard the Low-Energy Excess because it is very likely not due to oscillations

# Pragmatic 3+1 Fit



MiniBooNE  $E > 475$  MeV  
GoF = 26%      PGOF = 7%

- APP  $\nu_\mu \rightarrow \nu_e$  &  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ : LSND ( $\nu_s$ ), MiniBooNE (?), OPERA ( $\times_s$ ), ICARUS ( $\times_s$ ), KARMEN ( $\times_s$ ), NOMAD ( $\times_s$ ), BNL-E776 ( $\times_s$ )
- DIS  $\nu_e$  &  $\bar{\nu}_e$ : Reactors ( $\nu_s$ ), Gallium ( $\nu_s$ ),  $\nu_e C$  ( $\times_s$ ), Solar ( $\times_s$ )
- DIS  $\nu_\mu$  &  $\bar{\nu}_\mu$ : CDHSW ( $\times_s$ ), MINOS ( $\times_s$ ), Atmospheric ( $\times_s$ ), MiniBooNE/SciBooNE ( $\times_s$ )

No Osc. nominally disfavored  
at  $\approx 6.3\sigma$   
 $\Delta\chi^2/NDF = 47.7/3$

# Effective SBL Oscillation Probabilities in 3+2 Schemes

$$\Delta_{kj} = \Delta m_{kj}^2 L / 4E$$

$$\eta = \arg[U_{e4}^* U_{\mu 4} U_{e5} U_{\mu 5}^*]$$

$$P_{\substack{(-) \\ \nu_\mu \rightarrow \nu_e}}^{\text{SBL}} = 4|U_{e4}|^2|U_{\mu 4}|^2 \sin^2 \Delta_{41} + 4|U_{e5}|^2|U_{\mu 5}|^2 \sin^2 \Delta_{51} \\ + 8|U_{\mu 4} U_{e4} U_{\mu 5} U_{e5}| \sin \Delta_{41} \sin \Delta_{51} \cos(\Delta_{54} - \eta)$$

$$P_{\substack{(-) \\ \nu_\alpha \rightarrow \nu_\alpha}}^{\text{SBL}} = 1 - 4(1 - |U_{\alpha 4}|^2 - |U_{\alpha 5}|^2)(|U_{\alpha 4}|^2 \sin^2 \Delta_{41} + |U_{\alpha 5}|^2 \sin^2 \Delta_{51}) \\ - 4|U_{\alpha 4}|^2|U_{\alpha 5}|^2 \sin^2 \Delta_{54}$$

[Sorel, Conrad, Shaevitz, PRD 70 (2004) 073004; Maltoni, Schwetz, PRD 76 (2007) 093005; Karagiorgi et al, PRD 80 (2009) 073001; Kopp, Maltoni, Schwetz, PRL 107 (2011) 091801; Giunti, Laveder, PRD 84 (2011) 073008; Donini et al, JHEP 07 (2012) 161; Archidiacono et al, PRD 86 (2012) 065028; Jacques, Krauss, Lunardini, PRD 87 (2013) 083515; Conrad et al, AHEP 2013 (2013) 163897; Archidiacono et al, PRD 87 (2013) 125034; Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050; Giunti, Laveder, Y.F. Li, H.W. Long, PRD 88 (2013) 073008; Girardi, Meroni, Petcov, JHEP 1311 (2013) 146]

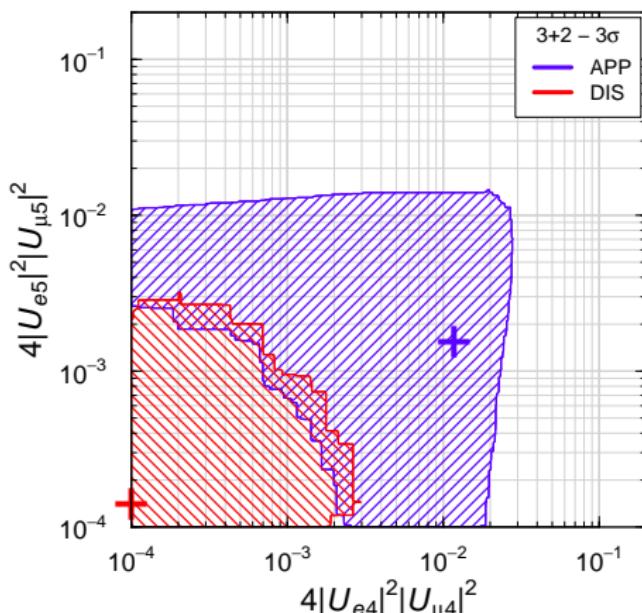
- Good: CP violation
- Bad: Two massive sterile neutrinos at the eV scale!

4 more parameters:  $\underbrace{\Delta m_{41}^2, |U_{e4}|^2, |U_{\mu 4}|^2, \Delta m_{51}^2, |U_{e5}|^2, |U_{\mu 5}|^2, \eta}_{3+1}$

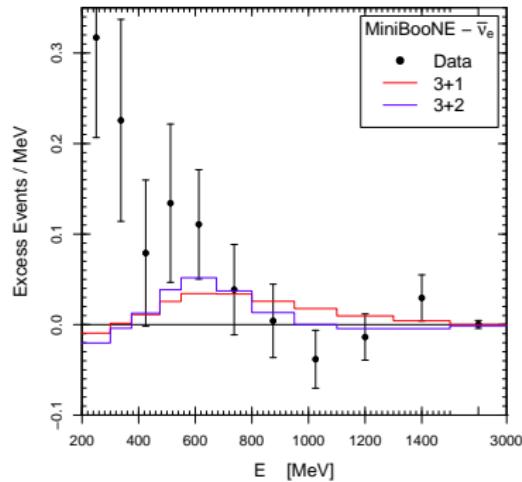
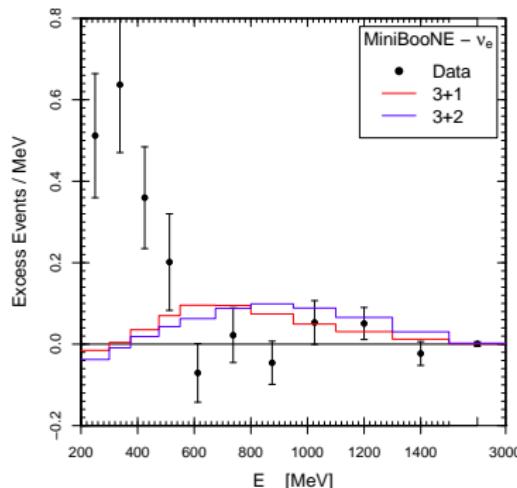
Global Fits	Our Fit		KMMS	
	3+1	3+2	3+1	3+2
GoF	5%	7%	19%	23%
PGoF	0.1%	0.04%	0.01%	0.003%

- Our Fit: 2014 update of Giunti, Laveder, Li, Long, PRD 88 (2013) 073008
- KMMS: Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050

APP-DIS 3+2 Tension:

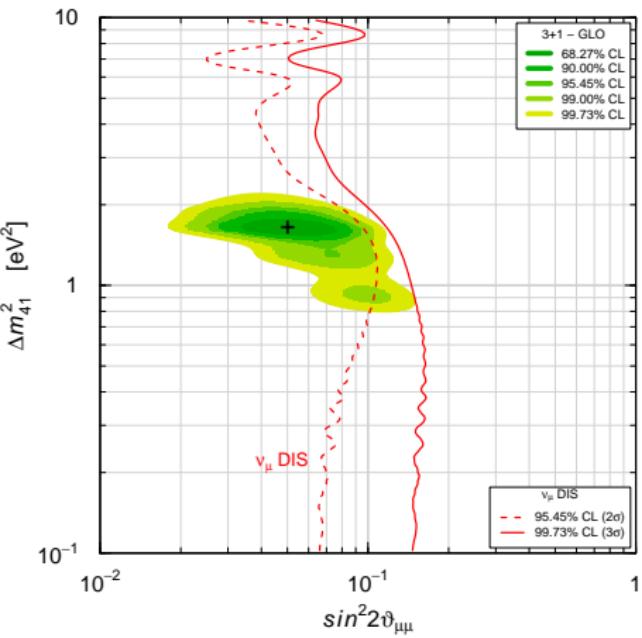
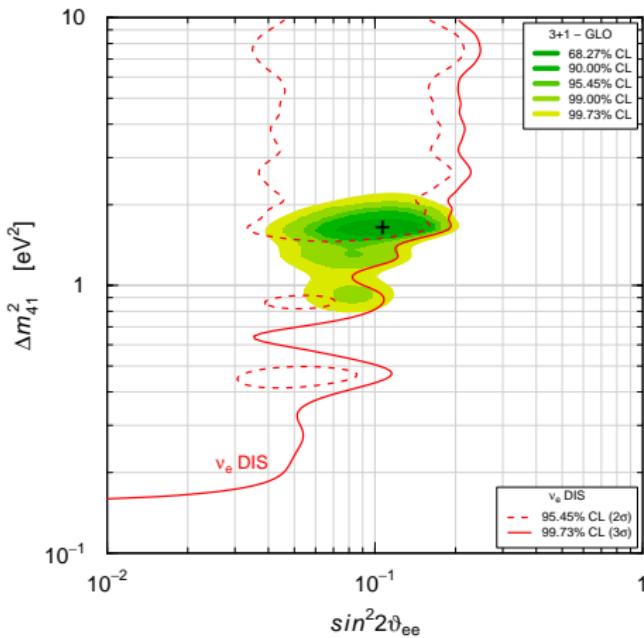


# 3+2 cannot fit MiniBooNE Low-Energy Excess



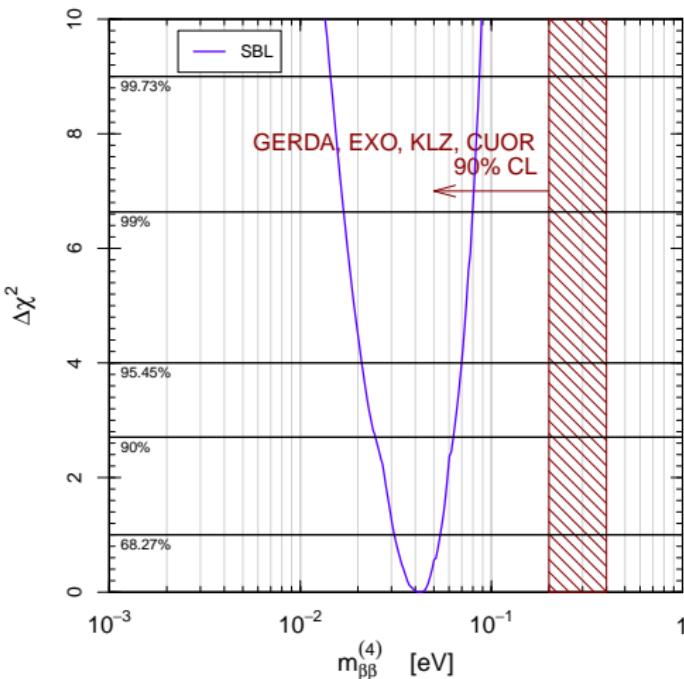
- ▶ Note difference between 3+2  $\nu_e$  and  $\bar{\nu}_e$  histograms due to CP violation
- ▶ 3+2 can fit slightly better the small  $\bar{\nu}_e$  excess at about 600 MeV
- ▶ 3+2 fit of low-energy excess as bad as 3+1
- ▶ Claims that 3+2 can fit low-energy excess do not take into account constraints from other data
- ▶ Conclusion: forget 3+2! (at least until new data require it)

# $\nu_e$ and $\nu_\mu$ Disappearance



# Neutrinoless Double- $\beta$ Decay

$$m_{\beta\beta} = |U_{e1}|^2 m_1 + |U_{e2}|^2 e^{i\alpha_{21}} m_2 + |U_{e3}|^2 e^{i\alpha_{31}} m_3 + |U_{e4}|^2 e^{i\alpha_{41}} m_4$$



[Giunti, Laveder, Li, Long, 2014]

$$m_{\beta\beta}^{(k)} = |U_{ek}|^2 m_k$$

$$\begin{aligned} m_1 &\ll m_4 \\ \downarrow \\ m_{\beta\beta}^{(4)} &\simeq |U_{e4}|^2 \sqrt{\Delta m_{41}^2} \end{aligned}$$

surprise:  
possible cancellation  
with  $m_{\beta\beta}^{(3\nu)}$

[Barry et al, JHEP 07 (2011) 091]

[Li, Liu, PLB 706 (2012) 406]

[Rodejohann, JPG 39 (2012) 124008]

[Girardi, Meroni, Petcov, JHEP 1311 (2013) 146]

# Future experiments @ reactors

Projects	Ref	$P_{th}$ (MW)	$M_{target}$ (tons)	$L$ (m)	Depth (m.w.e.)
Nucifer (FRA)	[1]	70	0.75	7	13
Stereo (FRA)	[2]	50	1.75	[8.8-11.2]	18
Neutrino 4 (RUS)	[3]	100	2.2	[6-12]	few
Poseidon (RUS)	[4]	100	$\sim 3$	[5-8]	$\sim 15$
DANSS (RUS)	[5]	3000	0.9	[9.7-12.2]	50
Solid (GBR)	[6]	[45-80]	3	[6-8]	10
Hanbit (KOR)	[7]	2800	1	27	[10-23]
Hanaro (KOR)	[7]	30	0.5	6	few
Prospect (USA)	[8]	20-120	1 & 10	4 & 18	few
CARR (CHN)	[9]	60	-	7 & 15	few

# Future experiments @ accelerators

Projects	Ref	$P$ (MW)	$M_{target}$ (tons)	$E$ (MeV)	L (m)
SBN (USA)	[10]	> 0.09	[112 & 89 & 476]	~ 800	[110 & 470 & 600]
JPARC MLF (JPN)	[11] [12]	~ 1	50	~ 40	[17-23]
KPipe (JPN)	[13]	~ 1	684	~ 236	[32-152]
IsoDAR-KamLAND (JPN)	[14] [15]	3.4	1000	~ 6.5	[10-40]
IsoDAR-JUNO (CHN)	[15]	3.4	20000	~ 6.5	[20-100]
OscSNS (USA)	[16]	1.4	450	~ 40	[50-70]

# Borexino source experiment

## Expected Sensitivity (Phase A)

sources in pit

$^{51}\text{Cr}$

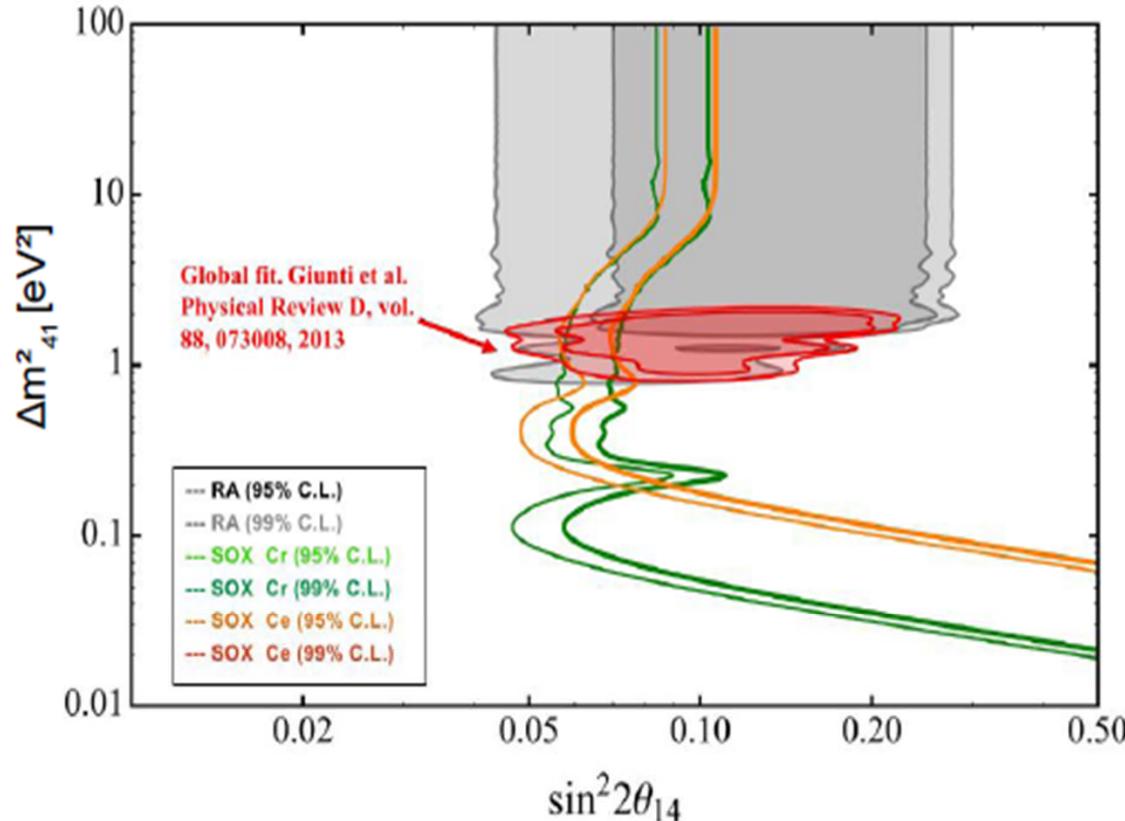
- Time: ~100 days
- Activity: 10 MCi
- $r_{\text{FV}} < 3.3 \text{ m}$

$^{144}\text{Ce}-^{144}\text{Pr}$

- Time: ~1.5 years
- Activity: 100 kCi
- $r_{\text{FV}} < 4.25 \text{ m}$

Neutrino 2014

Additional information: JHEP08 (2013) 038



$r_{\text{FV}}$ : Radius of fiducial volume

# Conclusions

- ▶ Short-Baseline  $\nu_e$  and  $\bar{\nu}_e$  Disappearance:
  - ▶ Experimental data agree on Reactor  $\bar{\nu}_e$  and Gallium  $\nu_e$  anomalies.
  - ▶ Problem: unknown systematic uncertainties (Reactor  $\bar{\nu}_e$  flux).
  - ▶ Many promising projects to test unambiguously short-baseline  $\nu_e$  and  $\bar{\nu}_e$  disappearance in a few years with reactors and radioactive sources.
  - ▶ Independent tests through effect of  $m_4$  in  $\beta$ -decay and  $\beta\beta_{0\nu}$ -decay.
- ▶ Short-Baseline  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  LSND Signal:
  - ▶ Not seen by other SBL  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  experiments.
  - ▶ MiniBooNE experiment has been inconclusive.
  - ▶ Experiments with near detector are needed to check LSND signal!
  - ▶ If  $|U_{e4}| > 0$  why not  $|U_{\mu 4}| > 0$ ?  $\implies \sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2|U_{\mu 4}|^2 > 0$
- ▶ Pragmatic 3+1 Fit is fine: moderate APP-DIS tension.
- ▶ 3+2 is not needed: same APP-DIS tension as 3+1 and no evidence of CP violation.
- ▶ Cosmology:
  - ▶ Tension between  $\Delta N_{\text{eff}} = 1$  and  $m_s \approx 1 \text{ eV}$ .
  - ▶ Cosmological and oscillation data may be reconciled by a non-standard cosmological mechanism.

# Goodness of Fit

- ▶ Assumption or approximation: Gaussian uncertainties and linear model
- ▶  $\chi^2_{\min}$  has  $\chi^2$  distribution with Number of Degrees of Freedom

$$\text{NDF} = N_D - N_P$$

$N_D$  = Number of Data       $N_P$  = Number of Fitted Parameters

- ▶  $\langle \chi^2_{\min} \rangle = \text{NDF}$        $\text{Var}(\chi^2_{\min}) = 2\text{NDF}$

- ▶  $\text{GoF} = \int_{\chi^2_{\min}}^{\infty} p_{\chi^2}(z, \text{NDF}) dz$        $p_{\chi^2}(z, n) = \frac{z^{n/2-1} e^{-z/2}}{2^{n/2} \Gamma(n/2)}$

# Parameter Goodness of Fit

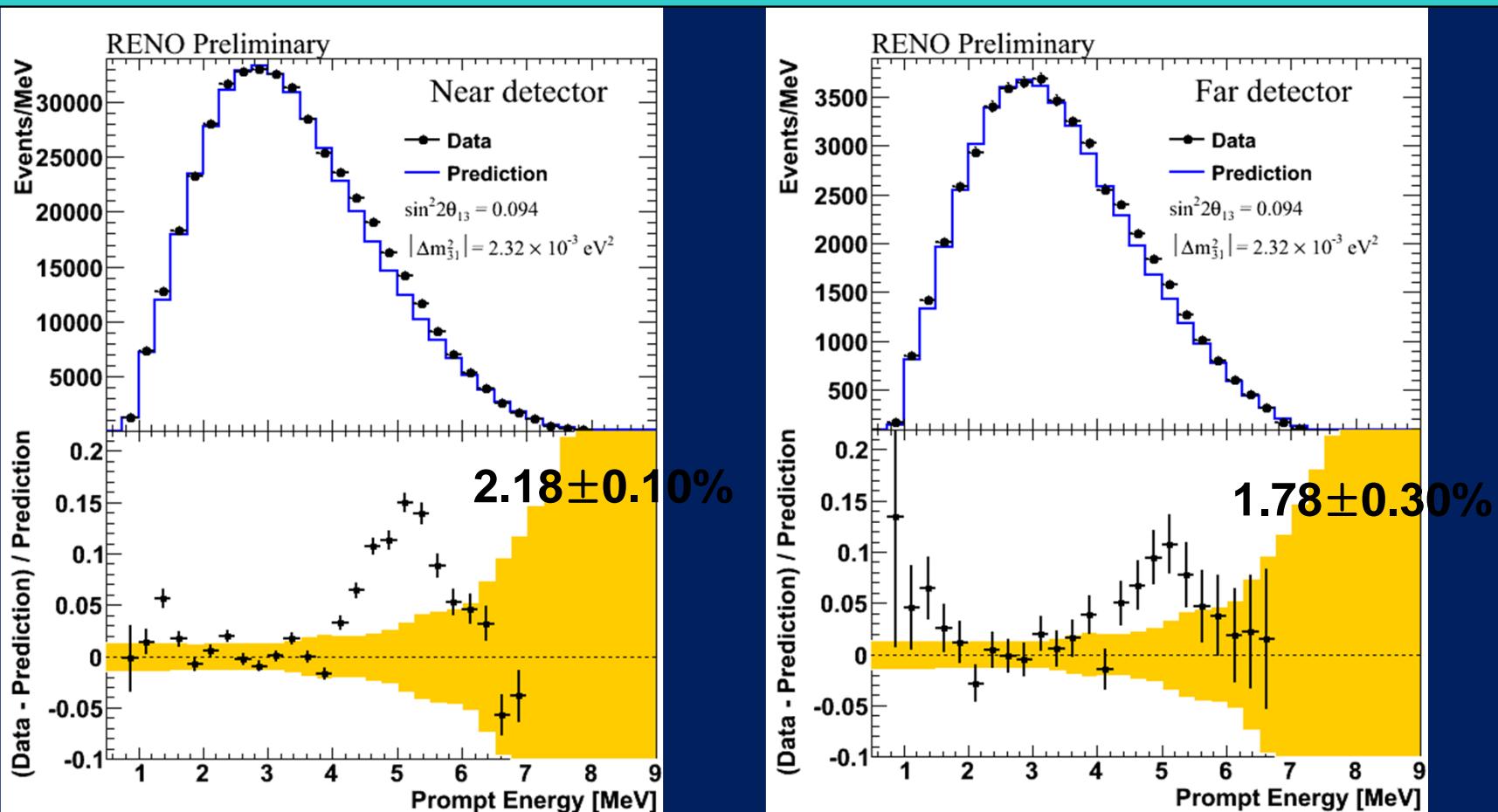
Maltoni, Schwetz, PRD 68 (2003) 033020, arXiv:hep-ph/0304176

- ▶ Measure compatibility of two (or more) sets of data points  $A$  and  $B$  under fitting model
- ▶  $\chi^2_{\text{PGoF}} = (\chi^2_{\min})_{A+B} - [(\chi^2_{\min})_A + (\chi^2_{\min})_B]$
- ▶  $\chi^2_{\text{PGoF}}$  has  $\chi^2$  distribution with Number of Degrees of Freedom

$$\text{NDF}_{\text{PGoF}} = N_P^A + N_P^B - N_P^{A+B}$$

- ▶  $\text{PGoF} = \int_{\chi^2_{\text{PGoF}}}^{\infty} p_{\chi^2}(z, \text{NDF}_{\text{PGoF}}) dz$

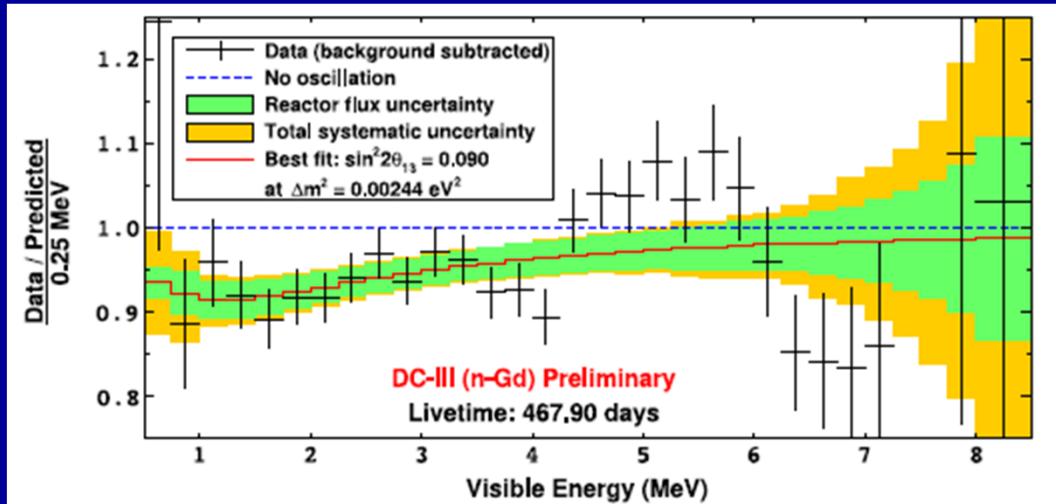
# Observation of a New Reactor Neutrino Component at 5 MeV



Fraction of 5 MeV excess (%) to expected flux [\[2011 Huber+Mueller\]](#)

- Near :  $2.18 \pm 0.40$  (experimental)  $\pm 0.49$  (expected shape error)
- Far :  $1.78 \pm 0.71$  (experimental)  $\pm 0.49$  (expected shape error)

# The 5 MeV Excess Seen at Double-Chooz and Daya Bay



Double-Chooz, Neutrino 2014

Daya Bay, ICHEP 2014

