

# Phenomenology of Neutrino Oscillations and Mixing

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Neutrino Unbound: <http://www.nu.to.infn.it>

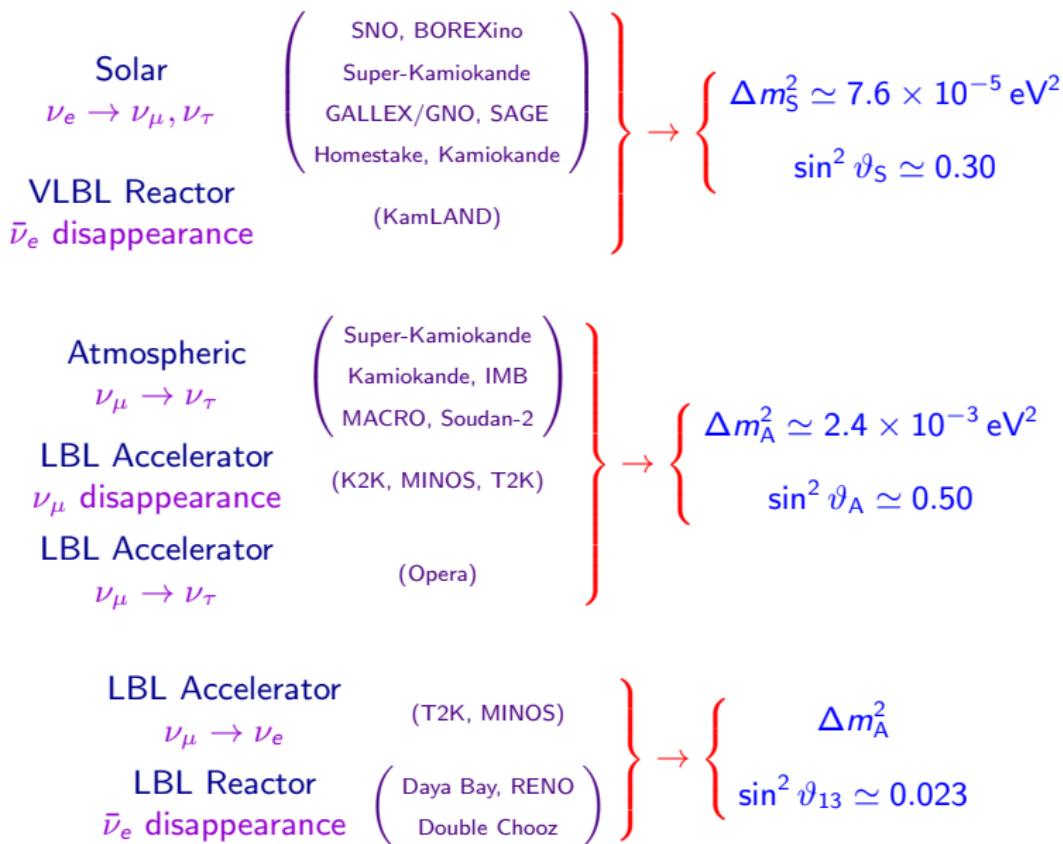
in collaboration with C. Giunti (INFN, Torino)

Astroparticle Physics Seminar

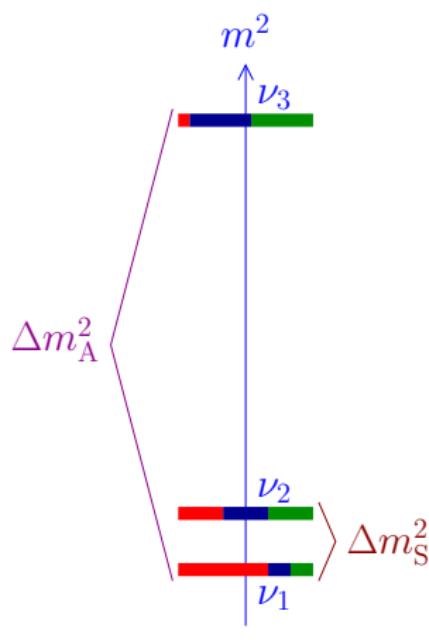
Torino, Italy

26 September 2013

# Experimental Evidences of Neutrino Oscillations

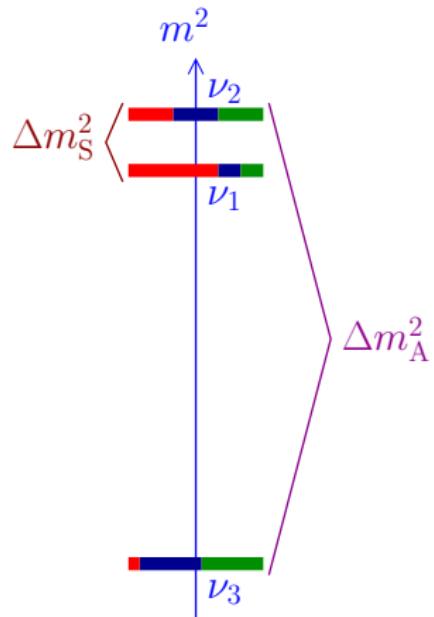


# Three-Neutrino Mixing Paradigm



Normal Spectrum

$\nu_e$        $\nu_\mu$        $\nu_\tau$



Inverted Spectrum

$$\Delta m_S^2 = \Delta m_{21}^2 = 7.50 \pm 0.20 \times 10^{-5} \text{ eV}^2 \quad \text{uncertainty} \simeq 2.6\%$$

$$\Delta m_A^2 = |\Delta m_{31}^2| \simeq |\Delta m_{32}^2| = 2.32_{-0.08}^{+0.12} \times 10^{-3} \text{ eV}^2 \quad \text{uncertainty} \simeq 5\%$$

$$U = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta_{13}} \\ -s_{12}c_{23}-c_{12}s_{23}s_{13}e^{i\delta_{13}} & c_{12}c_{23}-s_{12}s_{23}s_{13}e^{i\delta_{13}} & s_{23}c_{13} \\ s_{12}s_{23}-c_{12}c_{23}s_{13}e^{i\delta_{13}} & -c_{12}s_{23}-s_{12}c_{23}s_{13}e^{i\delta_{13}} & c_{23}c_{13} \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_2} & 0 \\ 0 & 0 & e^{i\lambda_3} \end{pmatrix}$$

$$= \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{13}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{13}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\lambda_2} & 0 \\ 0 & 0 & e^{i\lambda_3} \end{pmatrix}$$

$\vartheta_{23} = \vartheta_A$       Chooz, Palo Verde       $\vartheta_{12} = \vartheta_S$        $\beta\beta_{0\nu}$   
 $\sin^2 \vartheta_{23} \simeq 0.4 - 0.6$       T2K, MINOS       $\sin^2 \vartheta_{12} = 0.30 \pm 0.01$   
 Daya Bay, RENO  
 $\sin^2 \vartheta_{13} = 0.023 \pm 0.002$

$$\frac{\delta \sin^2 \vartheta_{23}}{\sin^2 \vartheta_{23}} \simeq 40\% \quad \frac{\delta \sin^2 \vartheta_{13}}{\sin^2 \vartheta_{13}} \simeq 10\% \quad \frac{\delta \sin^2 \vartheta_{12}}{\sin^2 \vartheta_{12}} \simeq 5\%$$

# Global Comparison of $\vartheta_{13}$ Measurements

Best Fit +  
68% C.L.

## Accelerator Experiments\*

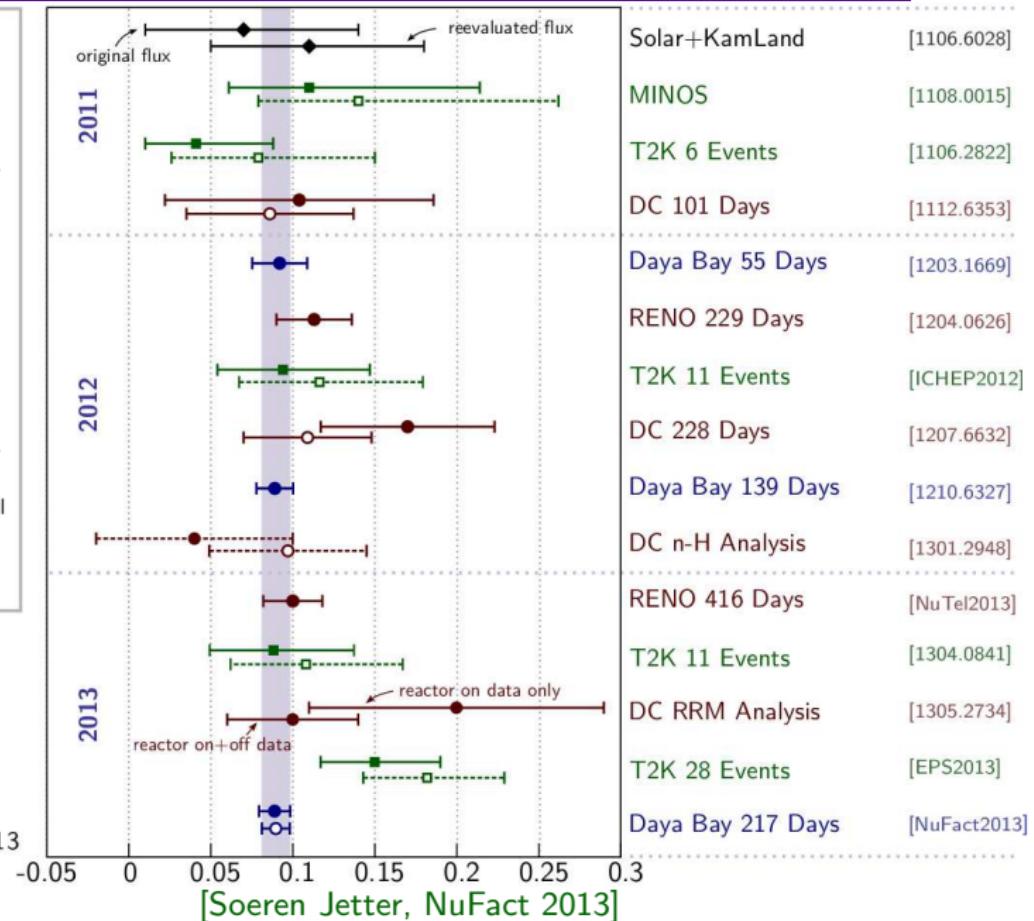
- Normal Hierarchy
- Inverted Hierarchy

\*All results assuming:  
 $\delta_{CP} = 0$ ,  
 $\theta_{23} = 45^\circ$

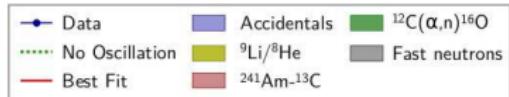
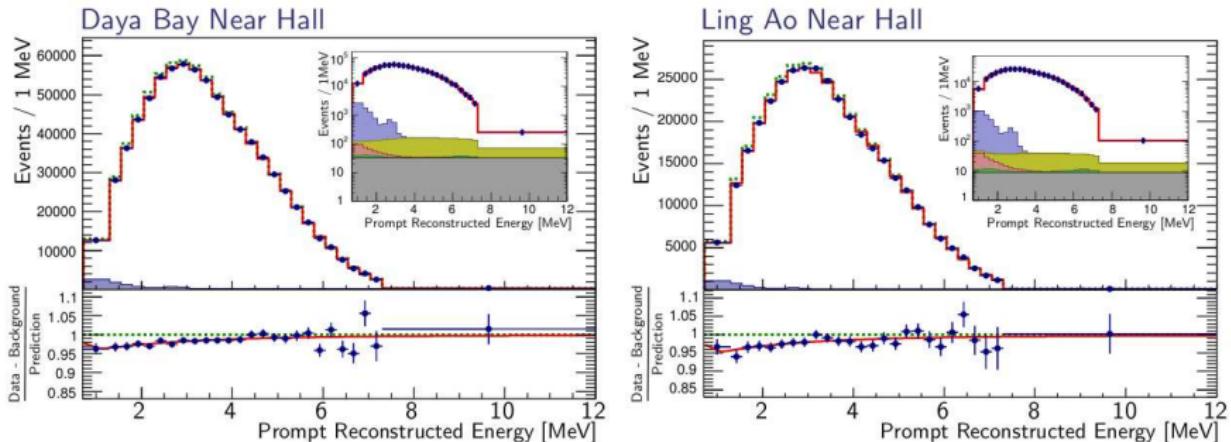
## Reactor Experiments

- Rate only
- Rate+Spectral
- n-Gd
- - - n-H

$$\sin^2 2\theta_{13}$$



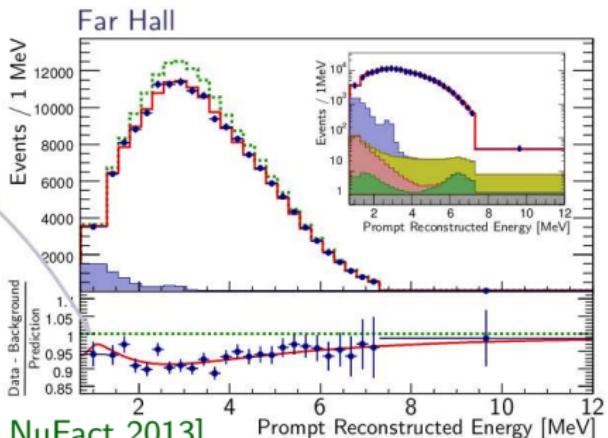
# Daya Bay - 22 August 2013



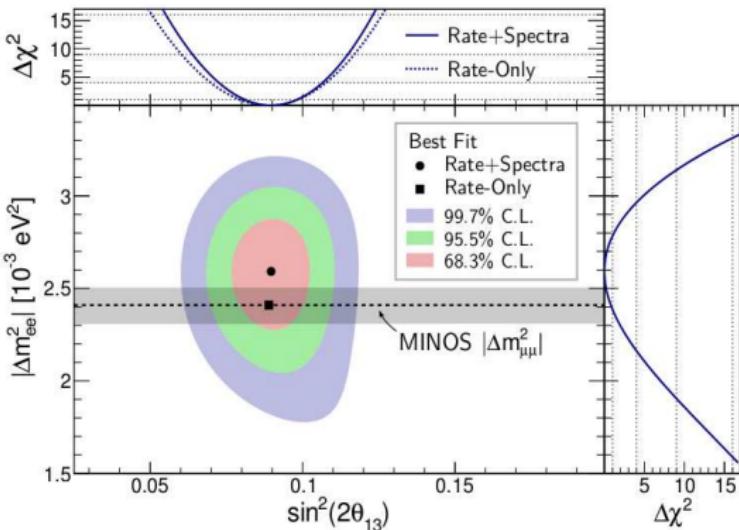
Spectral distortion  
consistent with oscillation

Shape distortion from  
energy losses in acrylic

- Both background and predicted no-oscillation spectra from best fit
- Statistical errors only



[Soeren Jetter, NuFact 2013]

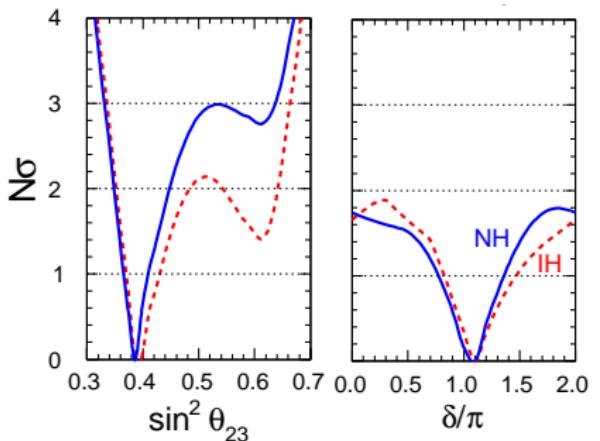


$$\sin^2 2\theta_{13} = 0.090^{+0.008}_{-0.009}$$

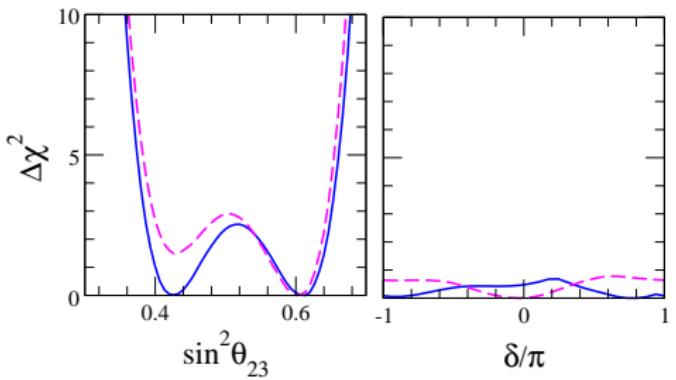
$$|\Delta m^2_{ee}| = 2.59^{+0.19}_{-0.20} \cdot 10^{-3} \text{ eV}^2$$

$$\chi^2 / N_{\text{DoF}} = 162.7 / 153$$

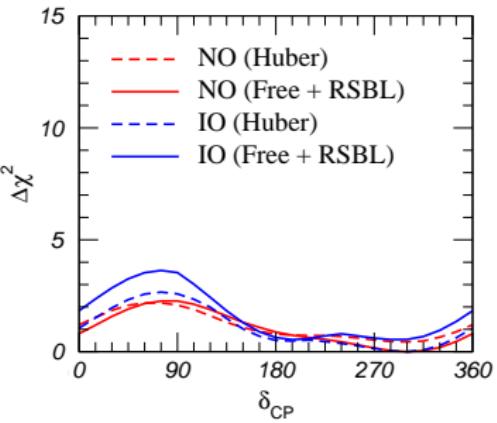
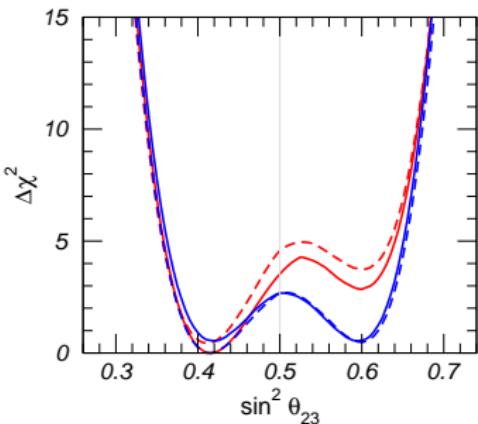
[Soeren Jetter, NuFact 2013]



[Fogli, Lisi, Marrone, Montanino, Palazzo, Rotunno,  
PRD 86 (2012) 013012]



[Forero, Tortola, Valle, PRD 86 (2012) 073012]



[Gonzalez-Garcia, Maltoni, Salvado, Schwetz,  
JHEP 12 (2012) 123; <http://www.nu-fit.org>]

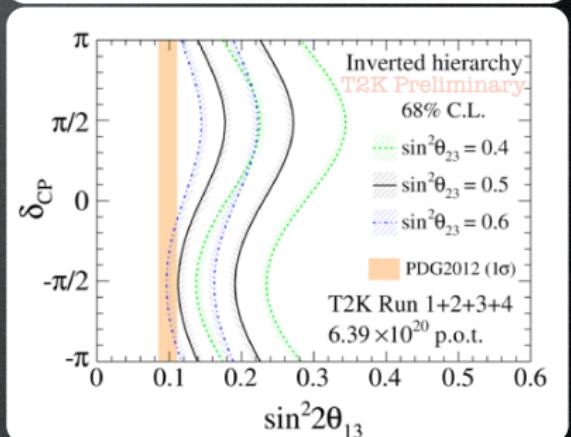
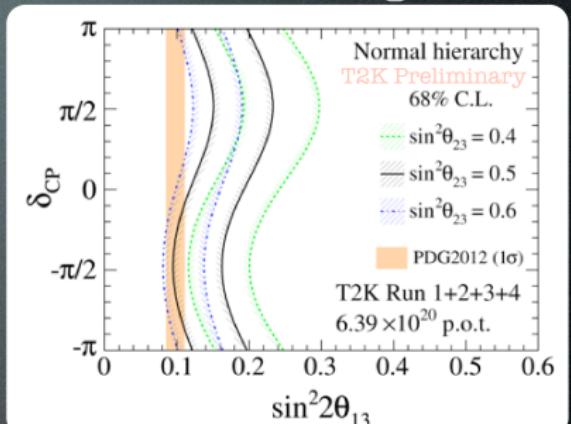
# Open Problems

- ▶  $\vartheta_{23} \stackrel{<}{\stackrel{>}{\sim}} 45^\circ$  ?
  - ▶ Atmospheric  $\nu$ , T2K, NO $\nu$ A, .....
- ▶ Mass Hierarchy ?
  - ▶ NO $\nu$ A, Atmospheric  $\nu$ , JUNO (Daya Bay II), RENO-50, Supernova  $\nu$ , ...
- ▶ CP violation ?
  - ▶ NO $\nu$ A, LAGUNA-LBNO, LBNE (USA), HyperK, ...
- ▶ Absolute Mass Scale ?
  - ▶  $\beta$  Decay, Neutrinoless Double- $\beta$  Decay, Cosmology, ...
- ▶ Dirac or Majorana ?
  - ▶ Neutrinoless Double- $\beta$  Decay, ...
- ▶ Beyond Three-Neutrino Mixing ? Sterile Neutrinos ?

# Effect of $\theta_{23}$ Uncertainty

- $\nu_e$  appearance probability also depends on the value of  $\theta_{23}$
- If  $\theta_{23}$  is fixed at values near the edge of the current allowed region, the fit contours shift
- Future improved measurements of  $\theta_{23}$  will be important to extract information about other oscillation parameters (including  $\delta_{CP}$ ) in long-baseline experiments
  - A T2K combined  $\nu_e + \nu_\mu$  analysis is underway

Note: these are 1D contours for various values of  $\delta_{CP}$ , not 2D contours

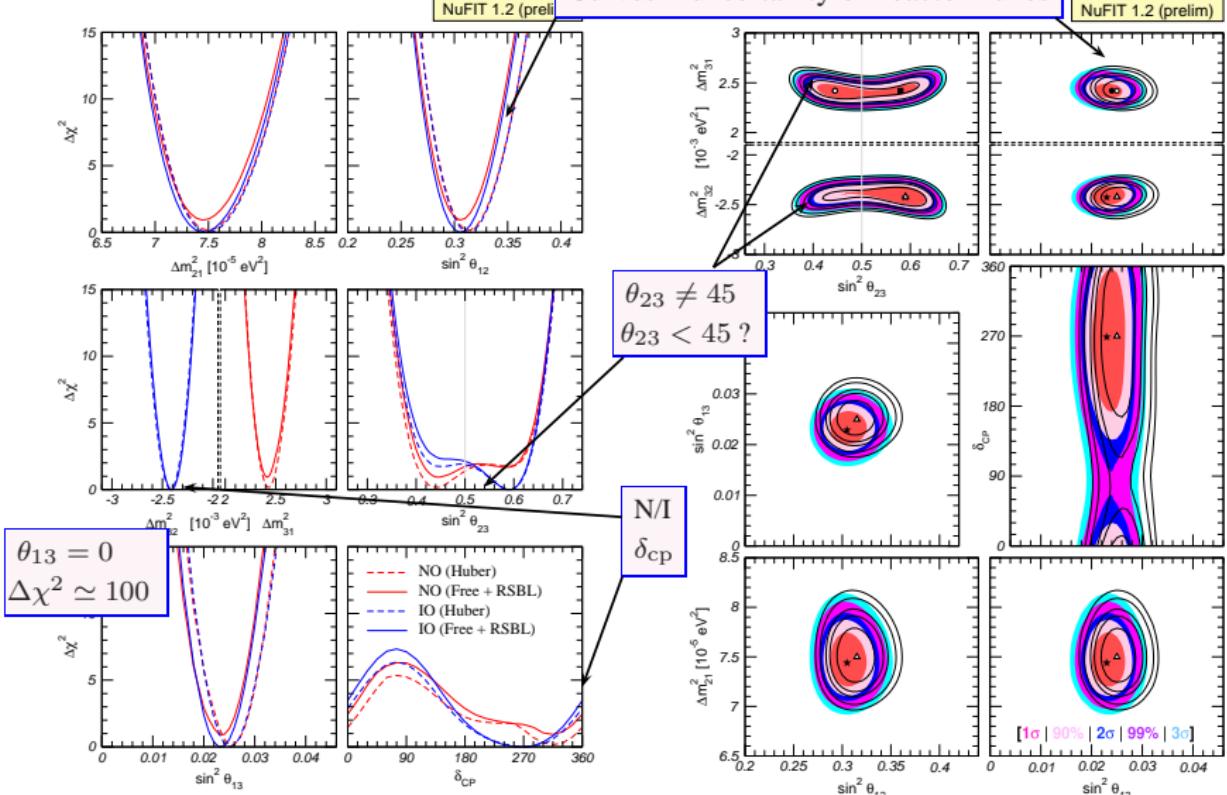


# 3 $\nu$ Flavour Parameters: Present Status

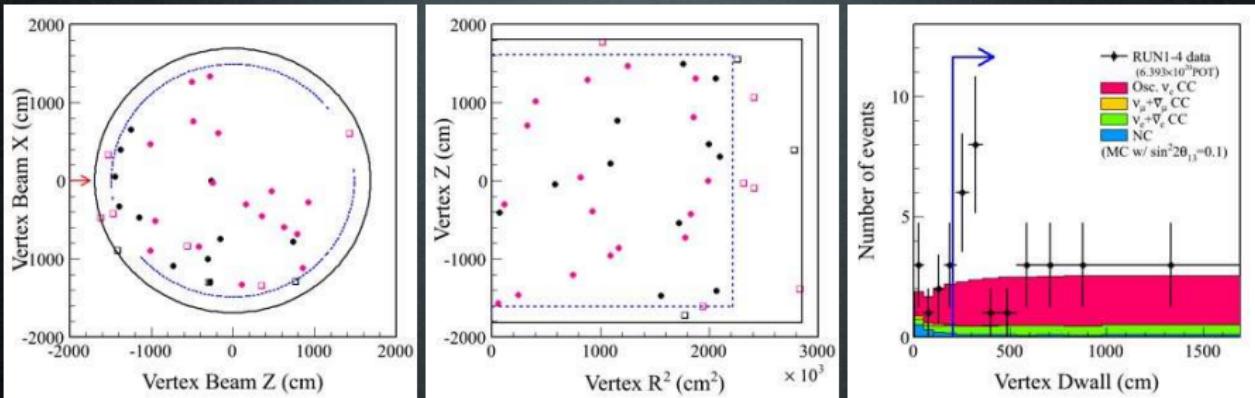
Global 6-parameter fit <http://www.nu-fit.org>

Maltoni, Schwetz, Salvado, MCGG

Curves = uncertainty on reactor fluxes



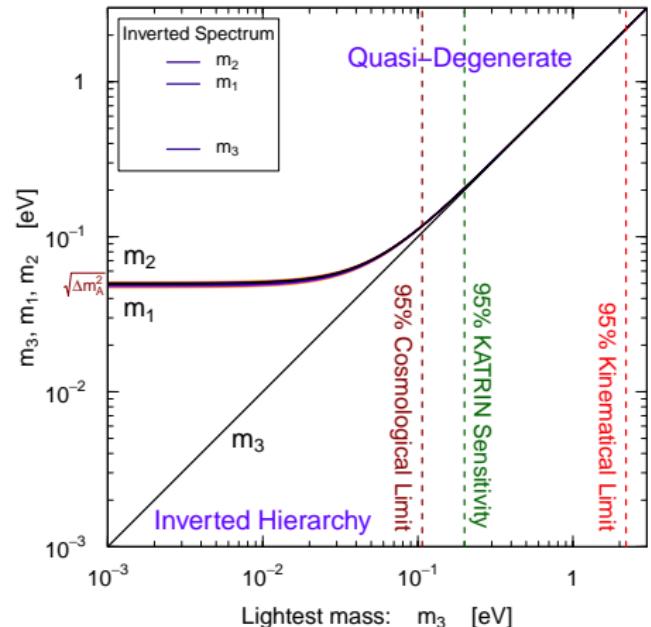
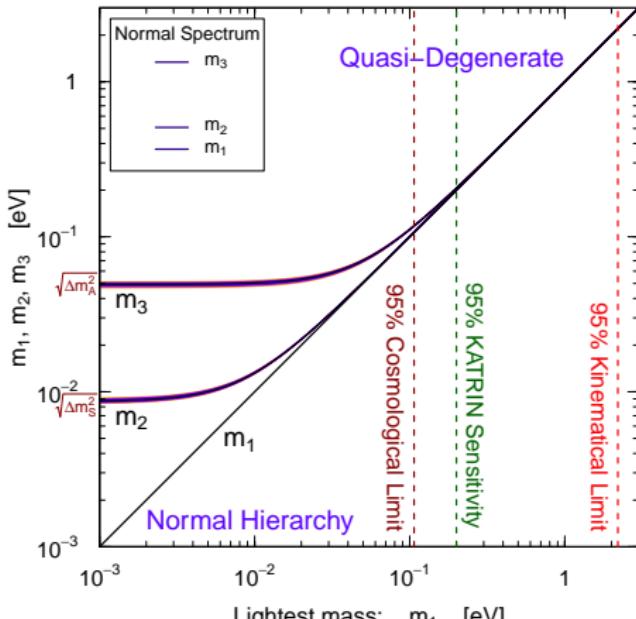
# Far Detector $\nu_e$ Vertex Distribution



	RUN1+2+3	RUN4	RUN1+2+3+4
Dwall	34.4%	54.7%	20.9%
Fromwall beam <sub>  </sub>	6.04%	85.6%	8.93%
$R^2 + Z$	32.4%	98.1%	64.5%

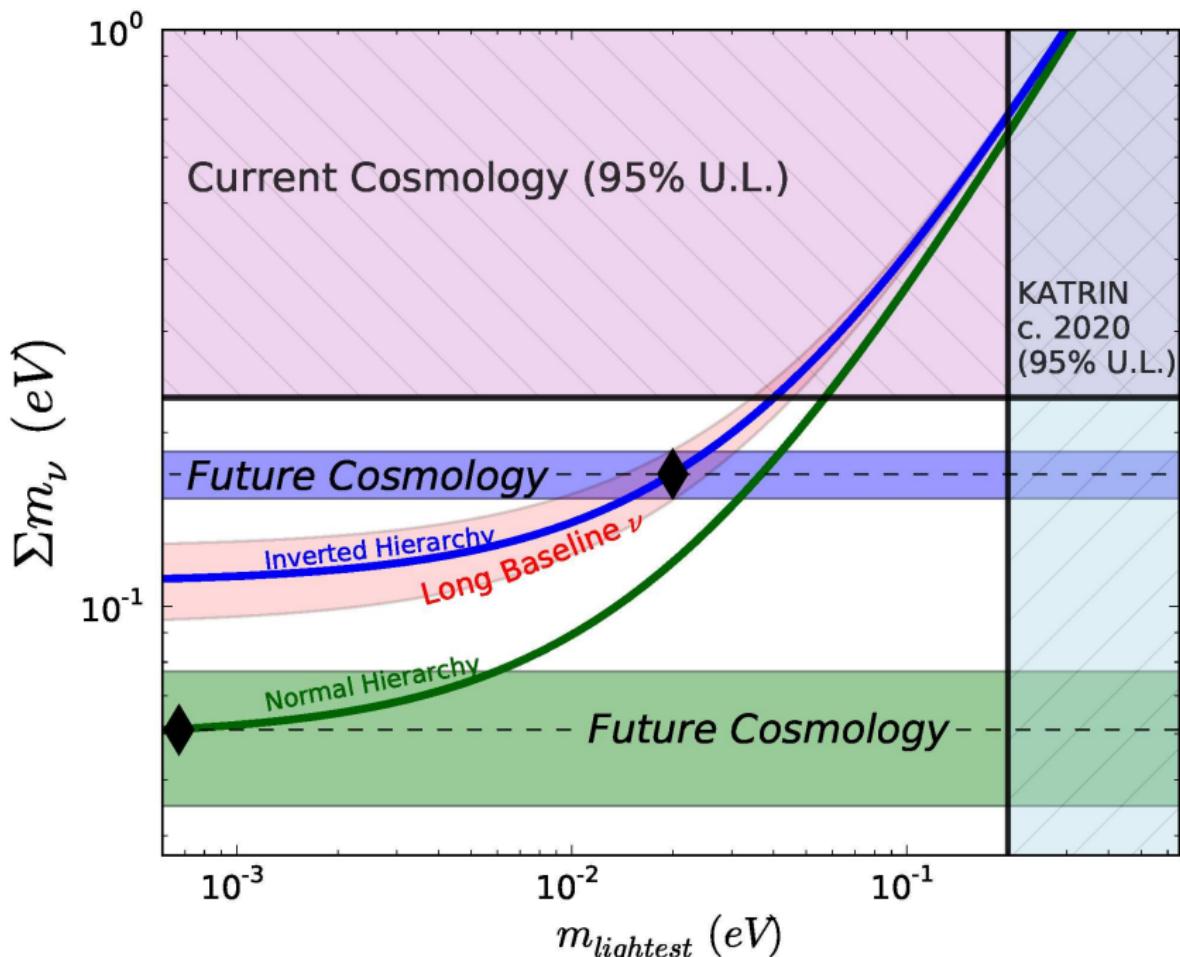
- With increased statistics, the p-values for the test distributions have increased

# Absolute Scale of Neutrino Masses



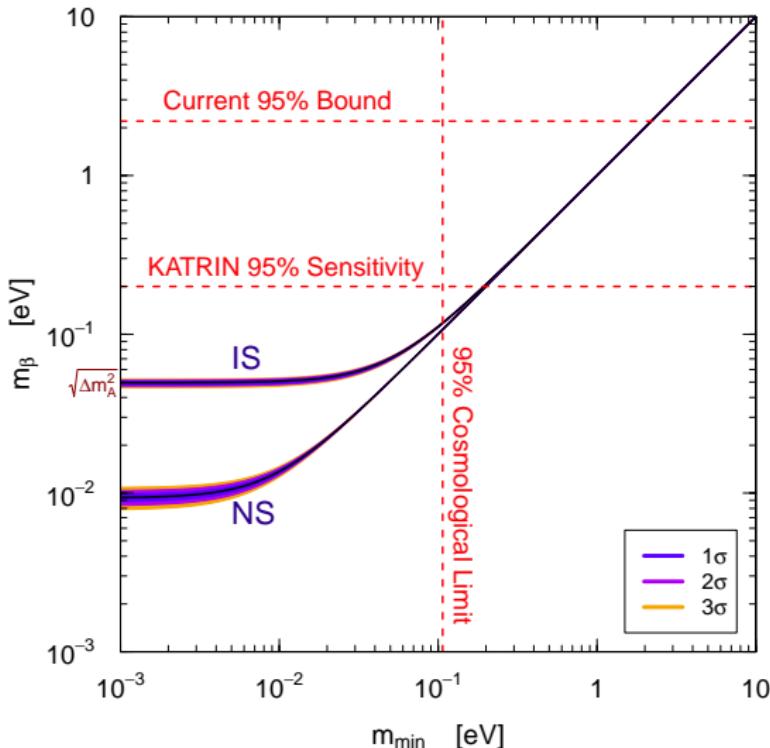
Quasi-Degenerate for  $m_1 \simeq m_2 \simeq m_3 \simeq m_\nu \gtrsim \sqrt{\Delta m_A^2} \simeq 5 \times 10^{-2}$  eV

95% Cosmological Limit: Planck + WMAP9 + highL + BAO [arXiv:1303.5076]



# Effective Neutrino Mass in Beta-Decay

$$m_\beta^2 = |U_{e1}|^2 m_1^2 + |U_{e2}|^2 m_2^2 + |U_{e3}|^2 m_3^2$$



► Quasi-Degenerate:

$$m_\beta^2 \simeq m_\nu^2 \sum_k |U_{ek}|^2 = m_\nu^2$$

► Inverted Hierarchy:

$$m_\beta^2 \simeq (1 - s_{13}^2) \Delta m_A^2 \simeq \Delta m_A^2$$

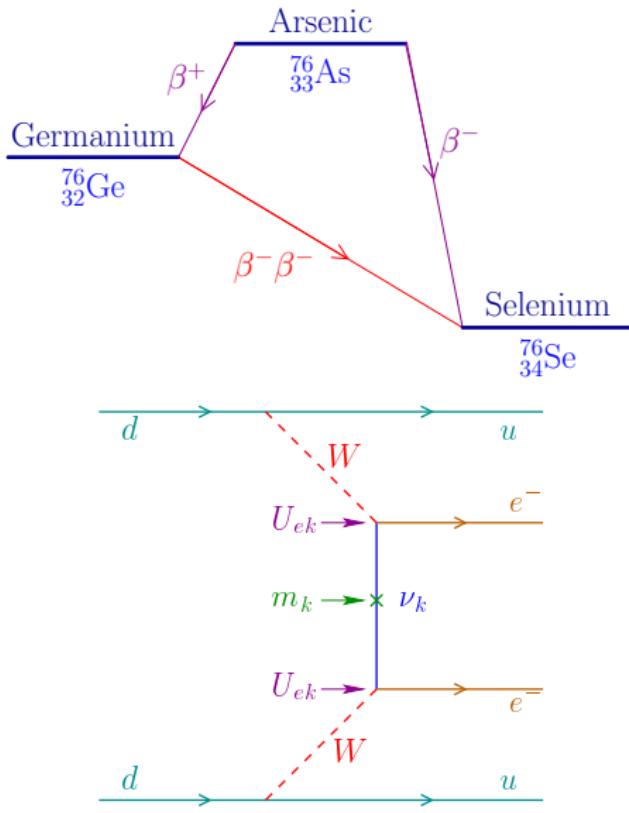
► Normal Hierarchy:

$$\begin{aligned} m_\beta^2 &\simeq s_{12}^2 c_{13}^2 \Delta m_S^2 + s_{13}^2 \Delta m_A^2 \\ &\simeq 2 \times 10^{-5} + 6 \times 10^{-5} \text{ eV}^2 \end{aligned}$$

►  $m_\beta \lesssim 4 \times 10^{-2} \text{ eV}$

↓  
Normal Spectrum

# Majorana $\nu$ : Neutrinoless Double-Beta Decay



$$(T_{1/2}^{0\nu})^{-1} = G_{0\nu} |\mathcal{M}_{0\nu}|^2 m_{\beta\beta}^2$$

Effective Majorana Mass

$$m_{\beta\beta} = \left| \sum_{k=1}^3 U_{ek}^2 m_k \right|$$

EXO + KamLAND-Zen



[PRL 109 (2012) 032505; PRL 110 (2013) 062502]

$$|m_{\beta\beta}| \lesssim 0.12 - 0.25 \text{ eV} \quad (90\% \text{C.L.})$$

GERDA

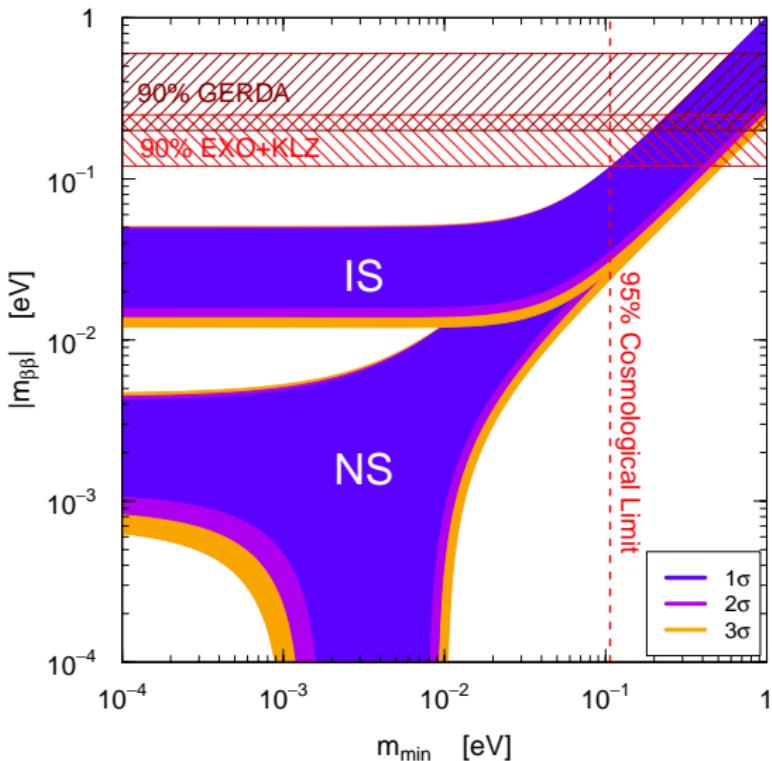


[arXiv:1307.4720]

$$|m_{\beta\beta}| \lesssim 0.2 - 0.6 \text{ eV} \quad (90\% \text{C.L.})$$

# Effective Majorana Neutrino Mass

$$m_{\beta\beta} = |U_{e1}|^2 m_1 + |U_{e2}|^2 e^{i\alpha_2} m_2 + |U_{e3}|^2 e^{i\alpha_3} m_3$$



► Quasi-Degenerate:

$$|m_{\beta\beta}| \simeq m_\nu \sqrt{1 - s_{2\vartheta_{12}}^2 s_{\alpha_2}^2}$$

► Inverted Hierarchy:

$$|m_{\beta\beta}| \simeq \sqrt{\Delta m_A^2 (1 - s_{2\vartheta_{12}}^2 s_{\alpha_2}^2)}$$

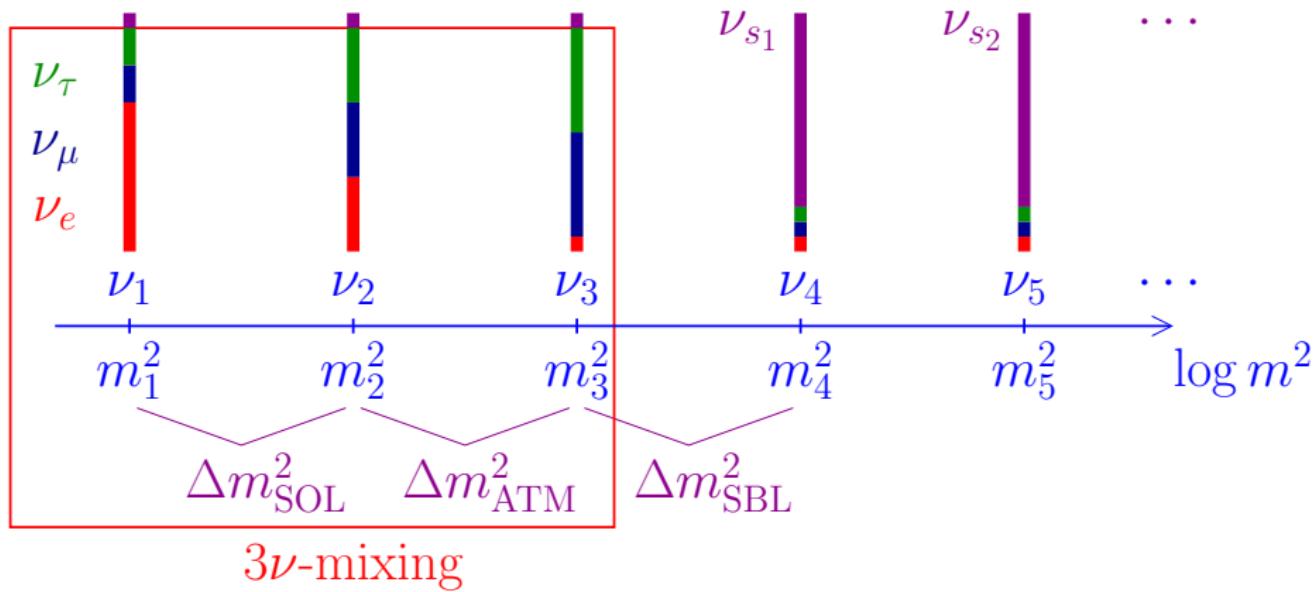
► Normal Hierarchy:

$$\begin{aligned} |m_{\beta\beta}| &\simeq |s_{12}^2 \sqrt{\Delta m_S^2} + e^{i\alpha} s_{13}^2 \sqrt{\Delta m_A^2}| \\ &\simeq |2.7 + 1.2 e^{i\alpha}| \times 10^{-3} \text{ eV} \end{aligned}$$

$$m_1 \gtrsim 10^{-3} \text{ eV} \Rightarrow \text{cancellation?}$$

$$|m_{\beta\beta}| \lesssim 10^{-2} \text{ eV} \implies \text{Normal Spectrum}$$

# Beyond Three-Neutrino Mixing: Sterile Neutrinos



# Light Sterile Neutrinos

- ▶ Sterile means no standard model interactions

[Pontecorvo, Sov. Phys. JETP 26 (1968) 984]

- ▶ Active neutrinos ( $\nu_e, \nu_\mu, \nu_\tau$ ) can oscillate into light sterile neutrinos ( $\nu_s$ )

- ▶ Observables:

- ▶ Disappearance of active neutrinos (neutral current deficit)
- ▶ Indirect evidence through combined fit of data (current indication)
- ▶ Short-baseline anomalies +  $3\nu$ -mixing:

$$\Delta m_{21}^2 \ll |\Delta m_{31}^2| \ll |\Delta m_{41}^2| \leq \dots$$

$\nu_1$	$\nu_2$	$\nu_3$	$\nu_4$	$\dots$
$\nu_e$	$\nu_\mu$	$\nu_\tau$	$\nu_{s_1}$	$\dots$

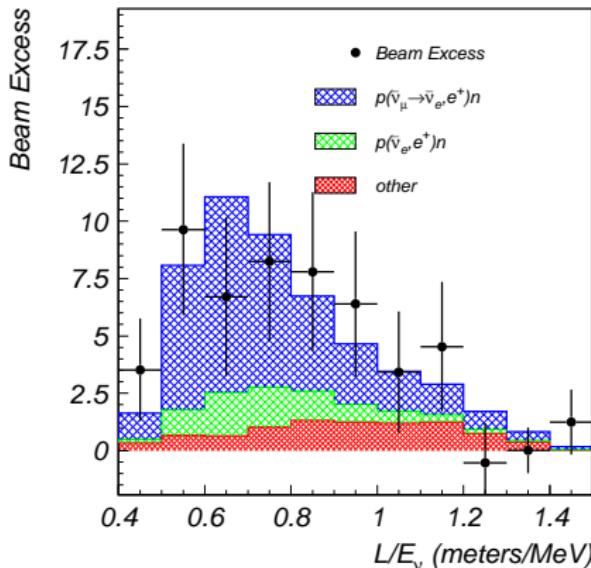
# LSND

[PRL 75 (1995) 2650; PRC 54 (1996) 2685; PRL 77 (1996) 3082; PRD 64 (2001) 112007]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

$$L \simeq 30 \text{ m}$$

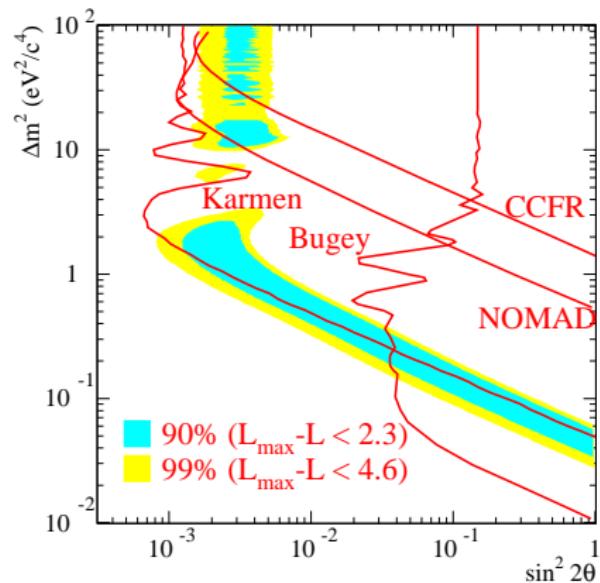
$$20 \text{ MeV} \leq E \leq 200 \text{ MeV}$$



$3.8\sigma$  excess

$$\Delta m_{\text{LSND}}^2 \gtrsim 0.2 \text{ eV}^2$$

$$(\gg \Delta m_A^2 \gg \Delta m_S^2)$$



# MiniBooNE

$L \simeq 541 \text{ m}$

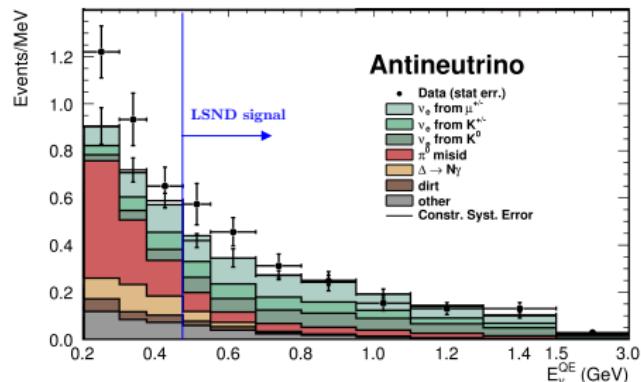
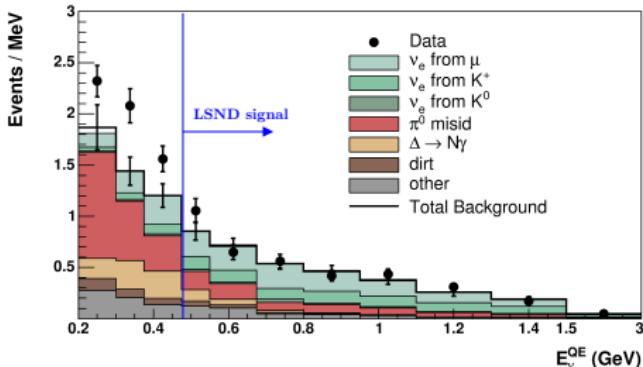
$200 \text{ MeV} \leq E \lesssim 3 \text{ GeV}$

$$\nu_\mu \rightarrow \nu_e$$

[PRL 102 (2009) 101802]

$$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$$

[PRL 110 (2013) 161801]



- ▶ Purpose: check LSND signal.
- ▶ Different  $L$  and  $E$ .
- ▶ Similar  $L/E$  (oscillations).
- ▶ LSND signal:  $E > 475 \text{ MeV}$ .
- ▶ Agreement with LSND signal?
- ▶ CP violation?
- ▶ Low-energy anomaly!

# Reactor Electron Antineutrino Anomaly

[Mention et al, PRD 83 (2011) 073006]

[update in White Paper, arXiv:1204.5379]

new reactor  $\bar{\nu}_e$  fluxes

[Mueller et al, PRC 83 (2011) 054615]

[Huber, PRC 84 (2011) 024617]

$\sim 2.8\sigma$  anomaly

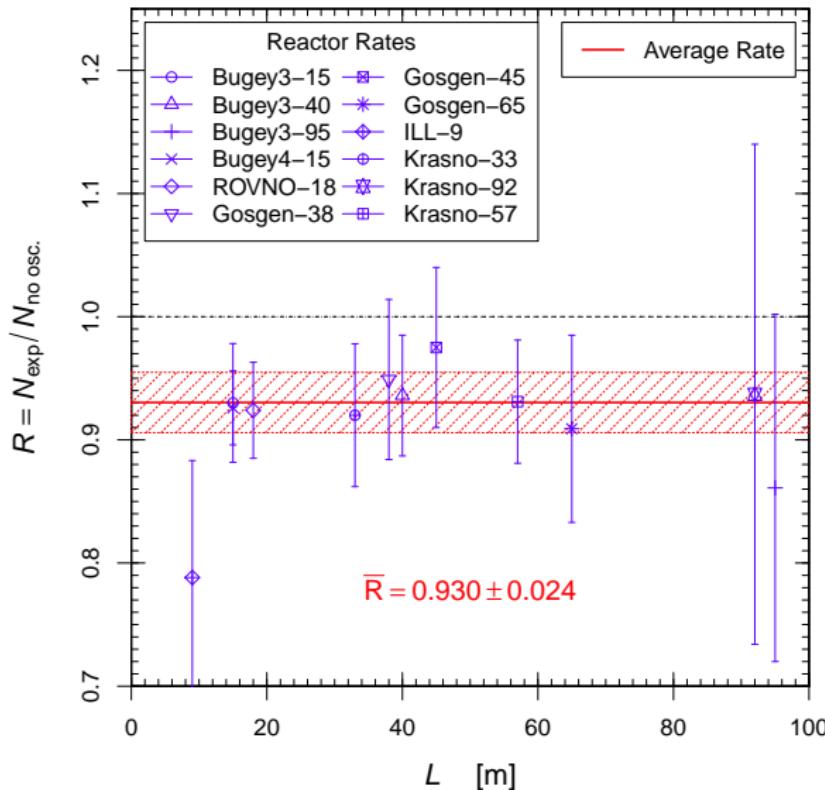
[see also:

Sinev, arXiv:1103.2452;

Ciuffoli, Evslin, Li, JHEP 12 (2012) 110;

Zhang, Qian, Vogel, PRD 87 (2013) 073018;

Ivanov et al, arXiv:1306.1995]



# Gallium Anomaly

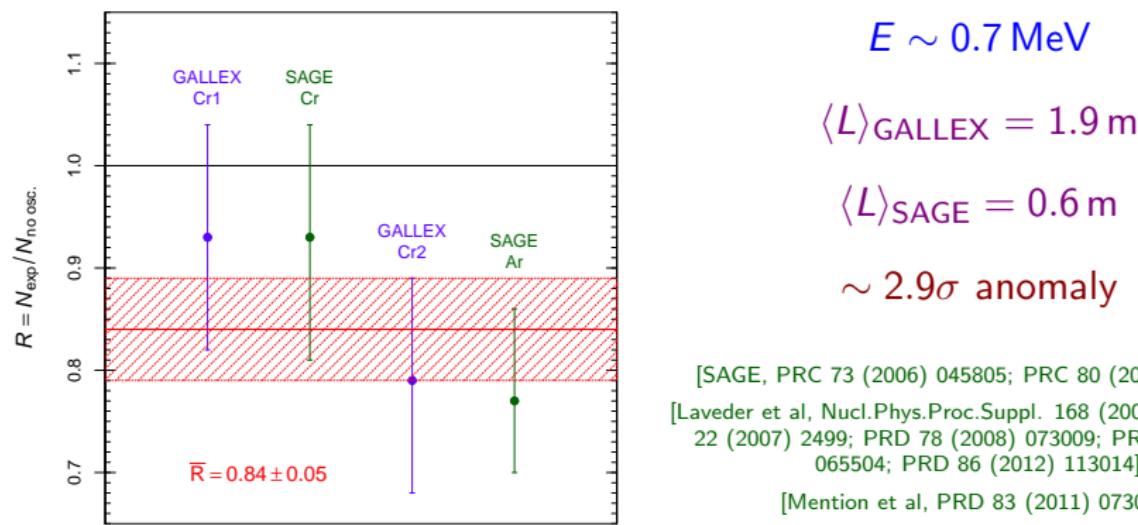
Gallium Radioactive Source Experiments: GALLEX and SAGE

Detection Process:  $\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e^-$

$\nu_e$  Sources:  $e^- + {}^{51}\text{Cr} \rightarrow {}^{51}\text{V} + \nu_e$        $e^- + {}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl} + \nu_e$

Anomaly supported by new  ${}^{71}\text{Ga}({}^3\text{He}, {}^3\text{H}){}^{71}\text{Ge}$  cross section measurement

[Frekers et al., PLB 706 (2011) 134]



# Effective SBL Oscillation Probabilities in 3+1 Schemes

$$P_{\substack{(-) \\ \nu_\alpha \rightarrow \nu_\beta}} = \sin^2 2\vartheta_{\alpha\beta} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\beta} = 4|U_{\alpha 4}|^2 |U_{\beta 4}|^2$$

No CP Violation!

$$P_{\substack{(-) \\ \nu_\alpha \rightarrow \nu_\alpha}} = 1 - \sin^2 2\vartheta_{\alpha\alpha} \sin^2 \left( \frac{\Delta m_{41}^2 L}{4E} \right)$$

$$\sin^2 2\vartheta_{\alpha\alpha} = 4|U_{\alpha 4}|^2 (1 - |U_{\alpha 4}|^2)$$

Perturbation of  $3\nu$  Mixing:  $|U_{e4}|^2 \ll 1$ ,  $|U_{\mu 4}|^2 \ll 1$ ,  $|U_{\tau 4}|^2 \ll 1$ ,  $|U_{s4}|^2 \simeq 1$

$$U = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} & U_{e4} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} & U_{\mu 4} \\ U_{\tau 1} & U_{\tau 2} & U_{\tau 3} & U_{\tau 4} \\ U_{s1} & U_{s2} & U_{s3} & U_{s4} \end{pmatrix}$$

↑  
SBL

$\sin^2 2\vartheta_{\alpha\alpha} \ll 1$   
 $\Downarrow$   
 $|U_{\alpha 4}|^2 \simeq \frac{\sin^2 2\vartheta_{\alpha\alpha}}{4}$

[Okada, Yasuda, IJMPA 12 (1997) 3669-3694]

[Bilenky, Giunti, Grimus, EPJC 1 (1998) 247]

# 3+1: Appearance vs Disappearance

- $\nu_e$  disappearance experiments:

$$\sin^2 2\vartheta_{ee} = 4|U_{e4}|^2 (1 - |U_{e4}|^2) \simeq 4|U_{e4}|^2$$

- $\nu_\mu$  disappearance experiments:

$$\sin^2 2\vartheta_{\mu\mu} = 4|U_{\mu 4}|^2 (1 - |U_{\mu 4}|^2) \simeq 4|U_{\mu 4}|^2$$

- $\nu_\mu \rightarrow \nu_e$  experiments:

$$\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \simeq \frac{1}{4} \sin^2 2\vartheta_{ee} \sin^2 2\vartheta_{\mu\mu}$$

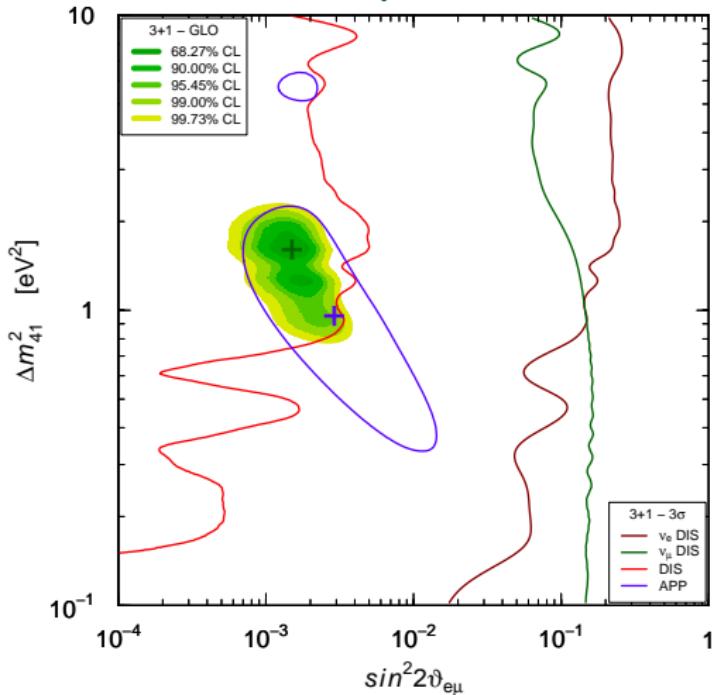
- Upper bounds on  $\sin^2 2\vartheta_{ee}$  and  $\sin^2 2\vartheta_{\mu\mu}$   $\Rightarrow$  strong limit on  $\sin^2 2\vartheta_{e\mu}$

[Okada, Yasuda, Int. J. Mod. Phys. A12 (1997) 3669-3694]

[Bilenky, Giunti, Grimus, Eur. Phys. J. C1 (1998) 247]

# 3+1 Global Fit

[Giunti, Laveder, Y.F. Li, H.W. Long, arXiv:1308.5288]



MiniBooNE  $E > 475$  MeV  
 $\text{GoF} = 29\%$        $\text{PGoF} = 9\%$

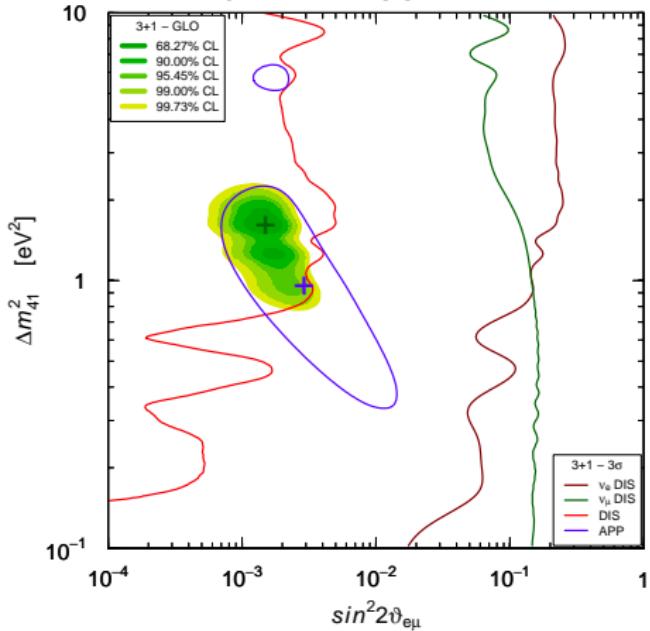
[different approach and conclusions: Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050]

- ▶ APP  $\nu_\mu \rightarrow \nu_e$  &  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$ : LSND (Y), MiniBooNE (?), OPERA (N), ICARUS (N), KARMEN (N), NOMAD (N), BNL-E776 (N)
- ▶ DIS  $\nu_e$  &  $\bar{\nu}_e$ : Reactors (Y), Gallium (Y),  $\nu_e C$  (N), Solar (N)
- ▶ DIS  $\nu_\mu$  &  $\bar{\nu}_\mu$ : CDHSW (N), MINOS (N), Atmospheric (N), MiniBooNE/SciBooNE (N)

No Osc. excluded at  $6.2\sigma$   
 $\Delta\chi^2/\text{NDF} = 46.2/3$

# MiniBooNE Impact on SBL Oscillations?

with MiniBooNE



GoF = 29%

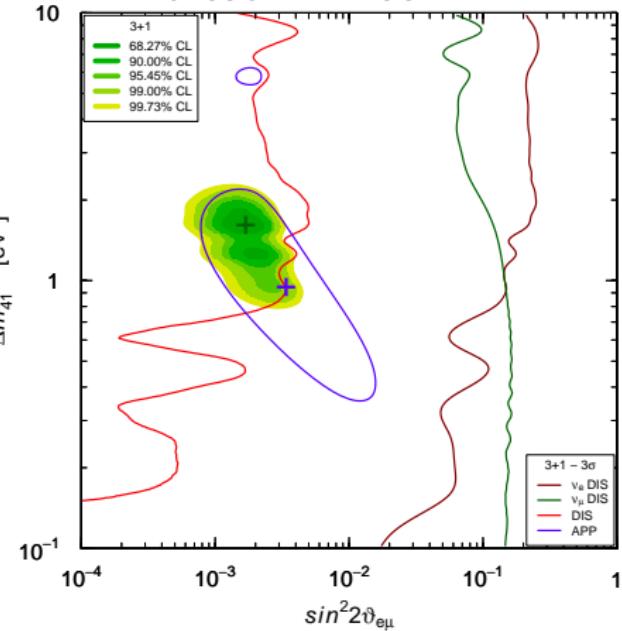
PGoF = 9%

No Osc. excluded at  $6.2\sigma$

$\Delta\chi^2/NDF = 46.2/3$

Without LSND: No Osc. excluded only at  $2.1\sigma$  ( $\Delta\chi^2/NDF = 8.3/3$ )

without MiniBooNE



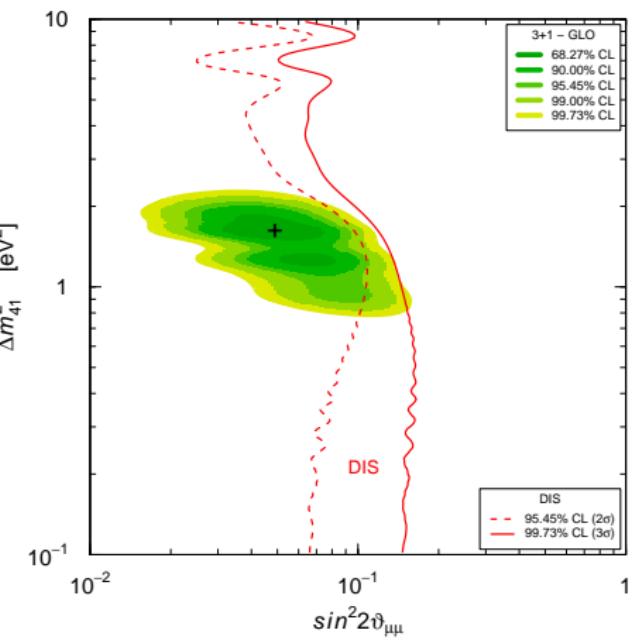
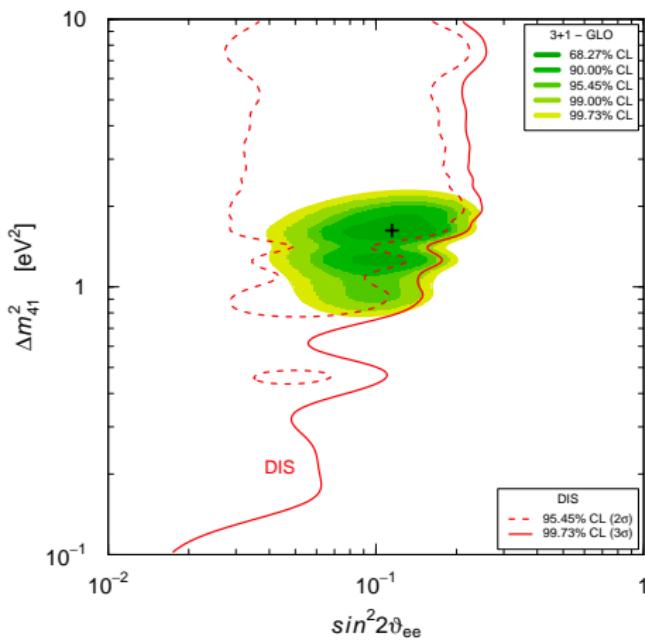
GoF = 19%

PGoF = 8%

No Osc. excluded at  $6.3\sigma$

$\Delta\chi^2/NDF = 47.1/3$

# $\nu_e$ and $\nu_\mu$ Disappearance



# Many Exciting New Experiments and Projects

## ► Reactor $\bar{\nu}_e$ Disappearance:

- Nucifer (OSIRIS, Saclay), Stereo (ILL, Grenoble) [arXiv:1204.5379]
- DANSS (Kalinin Nuclear Power Plant, Russia) [arXiv:1304.3696],  
POSEIDON (PIK, Gatchina, Russia) [arXiv:1204.2449]
- SCRAAM (San Onofre, California) [arXiv:1204.5379]
- CARR (China Advanced Research Reactor) [arXiv:1303.0607]
- Neutrino-4 (SM-3, Dimitrovgrad, Russia), SOLID (BR2, Belgium),  
Hanaro (Korea) [D. Lhuillier, EPSHEP 2013]

## ► Radioactive Source $\nu_e$ and $\bar{\nu}_e$ Disappearance:

- SOX (Borexino, Gran Sasso, Italy) [arXiv:1304.7721]
- CeLAND ( $^{144}\text{Ce}$ @KamLAND, Japan) [arXiv:1107.2335]
- SAGE (Baksan, Russia) [arXiv:1006.2103]
- IsoDAR (DAE $\delta$ ALUS, USA) [arXiv:1210.4454, arXiv:1307.2949]
- SNO+, JUNO, RENO [T. Lasserre, Neutrino 2012]

## ► Accelerator $\overset{(-)}{\nu_\mu} \rightarrow \overset{(-)}{\nu_e}$ Appearance:

- ICARUS/NESSIE (CERN) [arXiv:1304.2047, arXiv:1306.3455]
- nuSTORM [arXiv:1308.0494]
- OscSNS (Oak Ridge, USA) [arXiv:1305.4189, arXiv:1307.7097]

# Conclusions

- ▶ Robust Three-Neutrino Mixing Paradigm. Open problems:  $\vartheta_{23} \leq 45^\circ?$ , CP Violation, Mass Hierarchy, Absolute Mass Scale, Dirac or Majorana?
- ▶ Short-Baseline  $\nu_e$  and  $\bar{\nu}_e$  3+1 Disappearance:
  - ▶ Reactor  $\bar{\nu}_e$  anomaly is alive and exciting
  - ▶ Gallium  $\nu_e$  anomaly strengthened by new cross-section measurements
  - ▶ Many promising projects to test short-baseline  $\nu_e$  and  $\bar{\nu}_e$  disappearance in a few years with reactors and radioactive sources
  - ▶ Independent tests through effect of  $m_4$  in  $\beta$ -decay and  $(\beta\beta)_{0\nu}$ -decay
- ▶ Short-Baseline  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  LSND Signal:
  - ▶ MiniBooNE experiment has been inconclusive
  - ▶ If  $|U_{e4}| > 0$  why not  $|U_{\mu 4}| > 0$ ?  $\Rightarrow$  Maybe LSND luckily observed a fluctuation of a small  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  transition probability with amplitude  $\sin^2 2\vartheta_{e\mu} = 4|U_{e4}|^2|U_{\mu 4}|^2$ , which has not been seen by other appearance experiments
  - ▶ Better experiments are needed to check LSND signal
- ▶ Cosmology:
  - ▶ Important effects of sterile neutrinos
  - ▶ Implications depend on theoretical framework and considered data set
  - ▶ Cosmological indications must be checked by laboratory experiments

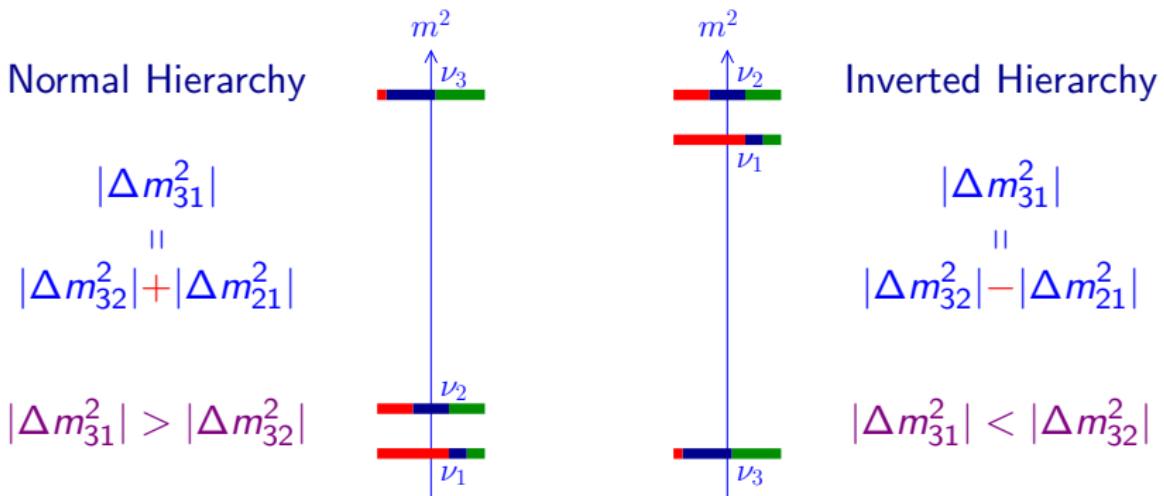
## Backup Slides

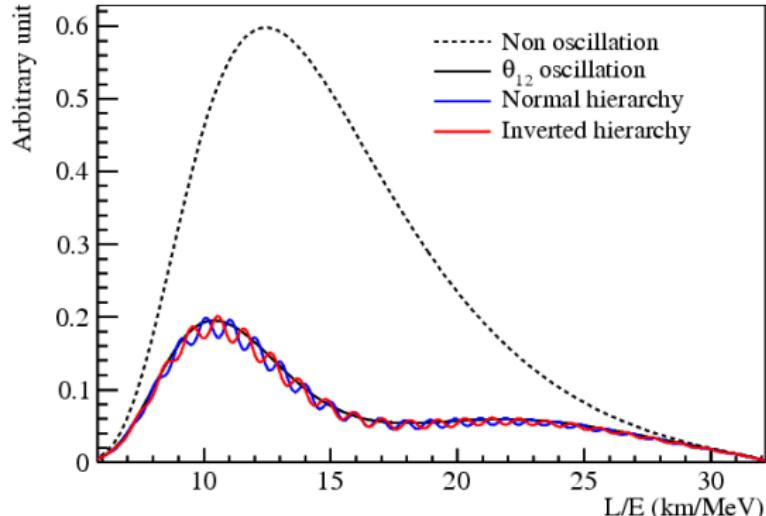
# Mass Hierarchy

## 1. Matter Effect: Atmospheric, Long-Baseline, Supernova Experiments

- $\nu_e \rightleftharpoons \nu_\mu$  MSW resonance:  $V = \frac{\Delta m_{13}^2 \cos 2\vartheta_{13}}{2E} \Leftrightarrow \Delta m_{13}^2 > 0$  NH
- $\bar{\nu}_e \rightleftharpoons \bar{\nu}_\mu$  MSW resonance:  $V = -\frac{\Delta m_{13}^2 \cos 2\vartheta_{13}}{2E} \Leftrightarrow \Delta m_{13}^2 < 0$  IH

## 2. Phase Difference: Reactor $\bar{\nu}_e \rightarrow \bar{\nu}_e$ : JUNO - Daya Bay II (China), RENO-50 (Korea)





$$F(L/E) = \phi(E)\sigma(E)P_{ee}(L/E)$$

$$P_{ee}(L/E) = 1 - P_{21} - P_{31} - P_{32}$$

$$P_{21} = \cos^4(\theta_{13}) \sin^2(2\theta_{12}) \sin^2(\Delta_{21})$$

$$P_{31} = \cos^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2(\Delta_{31})$$

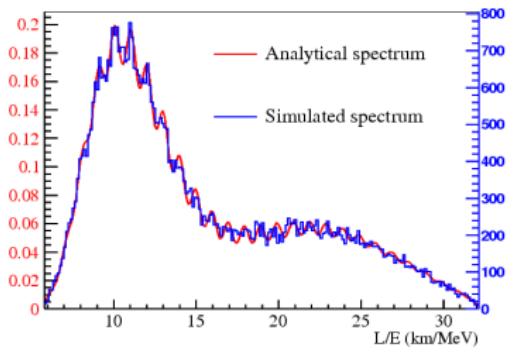
$$P_{32} = \sin^2(\theta_{12}) \sin^2(2\theta_{13}) \sin^2(\Delta_{32})$$

$$\Delta_{21} \ll \Delta_{31} \approx \Delta_{32}$$

S.T. Petcov et al., PLB533(2002)94  
 S.Choubey et al., PRD68(2003)113006  
 J. Learned et al., hep-ex/0612022

L. Zhan, Y. Wang, J. Cao, L. Wen,  
 PRD78:111103, 2008  
 PRD79:073007, 2009

**Precision energy spectrum measurement: Looking for interference between  $P_{31}$  and  $P_{32}$**   
 ➔ relative measurement



[Miao He, NuFact 2013]

## CP Violation

$$P_{\nu_\alpha \rightarrow \nu_\beta} - P_{\bar{\nu}_\alpha \rightarrow \bar{\nu}_\beta} = -16 J_{\alpha\beta} \sin\left(\frac{\Delta m_{21}^2 L}{4E}\right) \sin\left(\frac{\Delta m_{31}^2 L}{4E}\right) \sin\left(\frac{\Delta m_{32}^2 L}{4E}\right)$$

$$J_{\alpha\beta} = \text{Im}(U_{\alpha 1} U_{\alpha 2}^* U_{\beta 1}^* U_{\beta 2}) = \pm J$$

$$J = s_{12} c_{12} s_{23} c_{23} s_{13} c_{13}^2 \sin \delta_{13}$$

Necessary conditions for observation of CP violation:

- ▶ Sensitivity to all mixing angles:  $\vartheta_{12}$ ,  $\vartheta_{23}$  and smaller  $\vartheta_{13}$
- ▶ Sensitivity to oscillations due to small  $\Delta m_{21}^2$  and large  $\Delta m_{31}^2$   
 $(\Delta m_{32}^2 = \Delta m_{31}^2 - \Delta m_{21}^2)$

# Sterile Neutrinos from Physics Beyond the SM

- ▶ Neutrinos are special in the Standard Model: the only **neutral fermions**
- ▶ In extensions of SM neutrinos can mix with non-SM fermions

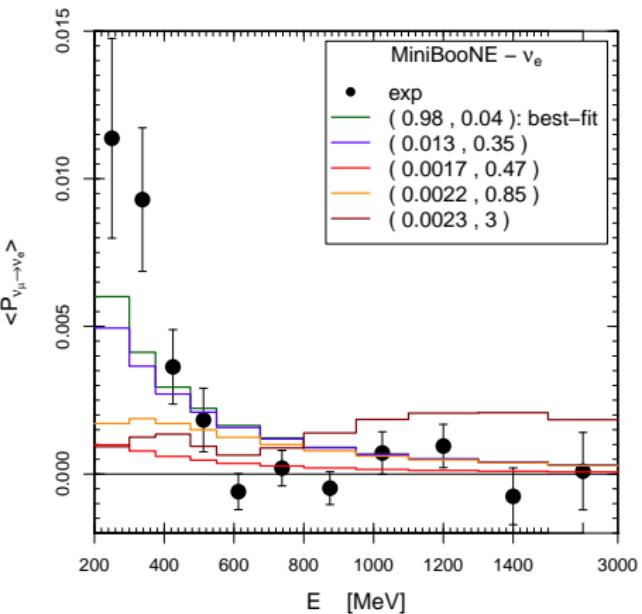
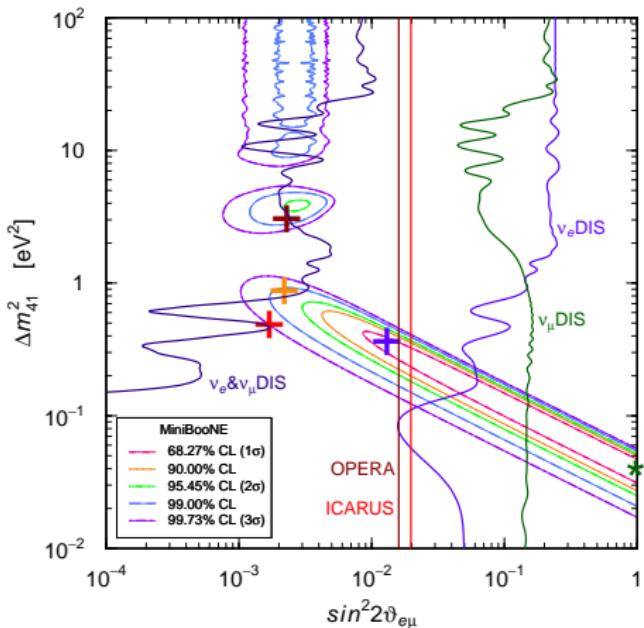
▶ SM:  $L_L = \begin{pmatrix} \nu_L \\ \ell_L \end{pmatrix}$        $\tilde{\Phi} = i\sigma_2 \Phi^* = \begin{pmatrix} \phi^0 \\ \phi^- \end{pmatrix} \xrightarrow[\text{Breaking}]{\text{Symmetry}} \begin{pmatrix} \nu/\sqrt{2} \\ 0 \end{pmatrix}$

- ▶ SM singlet  $\overline{L}_L \tilde{\Phi}$  can couple to new singlet chiral fermion field  $\nu_R$  (right-handed neutrino) related to physics beyond the SM
- ▶ Known examples: SUSY, new symmetries, extra dimensions, mirror world, ...  
[see [http://www.nu.to.infn.it/Sterile\\_Neutrinos/](http://www.nu.to.infn.it/Sterile_Neutrinos/)]
- ▶ Dirac mass term  $\sim \overline{L}_L \tilde{\Phi} \nu_R$  + Majorana mass term  $\sim \overline{\nu}_R^c \nu_R$
- ▶ Diagonalization of mass matrix  $\implies$  massive Majorana neutrinos

		LOW	HIG	noMB	noLSND
No Osc.	$\chi^2$	339.2	308.0	283.2	286.7
	NDF	259	253	221	255
	GoF	0.06 %	1 %	0.3 %	8 %
3+1 Osc.	$\chi^2_{\min}$	291.7	261.8	236.1	278.4
	NDF	256	250	218	252
	GoF	6 %	29 %	19 %	12 %
$\Delta m_{41}^2 [\text{eV}^2]$		1.6	1.6	1.6	1.7
	$ U_{e4} ^2$	0.033	0.03	0.03	0.024
	$ U_{\mu 4} ^2$	0.012	0.013	0.014	0.0073
	$\sin^2 2\vartheta_{e\mu}$	0.0016	0.0015	0.0017	0.0007
	$\sin^2 2\vartheta_{ee}$	0.13	0.11	0.12	0.093
	$\sin^2 2\vartheta_{\mu\mu}$	0.048	0.049	0.054	0.03
	$(\chi^2_{\min})_{\text{APP}}$	99.3	77.0	50.9	91.8
$\Delta \chi^2_{\text{PG}}$	$(\chi^2_{\min})_{\text{DIS}}$	180.1	180.1	180.1	180.1
	$\Delta \chi^2_{\text{PG}}$	12.7	4.8	5.1	6.4
	$\text{NDF}_{\text{PG}}$	2	2	2	2
	$\text{GoF}_{\text{PG}}$	0.2 %	9 %	8 %	4 %
	p-val <sub>No Osc.</sub>	$3 \times 10^{-10}$	$5 \times 10^{-10}$	$3 \times 10^{-10}$	$4 \times 10^{-2}$
$n\sigma_{\text{No Osc.}}$		$6.3\sigma$	$6.2\sigma$	$6.3\sigma$	$2.1\sigma$

[Giunti, Laveder, Y.F. Li, H.W. Long, arXiv:1308.5288]

# MiniBooNE Low-Energy Excess?



- ▶ No fit of low-energy excess for realistic  $\Delta m_{41}^2 \gtrsim 0.8$  eV $^2$  and  $\sin^2 2\theta_{e\mu} \lesssim 5 \times 10^{-3}$
- ▶ APP-DIS PGoF = 0.1%
- ▶ Neutrino energy reconstruction problem?

[Martini, Ericson, Chanfray, PRD 85 (2012) 093012; PRD 87 (2013) 013009]

# Effective SBL Oscillation Probabilities in 3+2 Schemes

$$\phi_{kj} = \Delta m_{kj}^2 L / 4E$$

$$\eta = \arg[U_{e4}^* U_{\mu 4} U_{e5} U_{\mu 5}^*]$$

$$P_{\substack{(-) \\ \nu_\mu \rightarrow \nu_e}} = 4|U_{e4}|^2 |U_{\mu 4}|^2 \sin^2 \phi_{41} + 4|U_{e5}|^2 |U_{\mu 5}|^2 \sin^2 \phi_{51} \\ + 8|U_{\mu 4} U_{e4} U_{\mu 5} U_{e5}| \sin \phi_{41} \sin \phi_{51} \cos(\phi_{54}^{(+)} - \eta)$$

$$P_{\substack{(-) \\ \nu_\alpha \rightarrow \nu_\alpha}} = 1 - 4(1 - |U_{\alpha 4}|^2 - |U_{\alpha 5}|^2)(|U_{\alpha 4}|^2 \sin^2 \phi_{41} + |U_{\alpha 5}|^2 \sin^2 \phi_{51}) \\ - 4|U_{\alpha 4}|^2 |U_{\alpha 5}|^2 \sin^2 \phi_{54}$$

[Sorel, Conrad, Shaevitz, PRD 70 (2004) 073004; Maltoni, Schwetz, PRD 76 (2007) 093005; Karagiorgi et al, PRD 80 (2009) 073001; Kopp, Maltoni, Schwetz, PRL 107 (2011) 091801; Giunti, Laveder, PRD 84 (2011) 073008; Donini et al, JHEP 07 (2012) 161; Conrad, Ignarra, Karagiorgi, Shaevitz, Spitz, AHEP 2013 (2013) 163897; Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050]

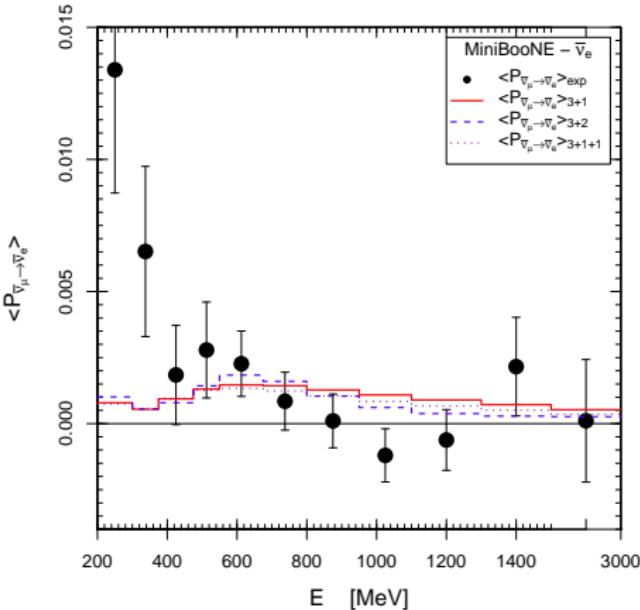
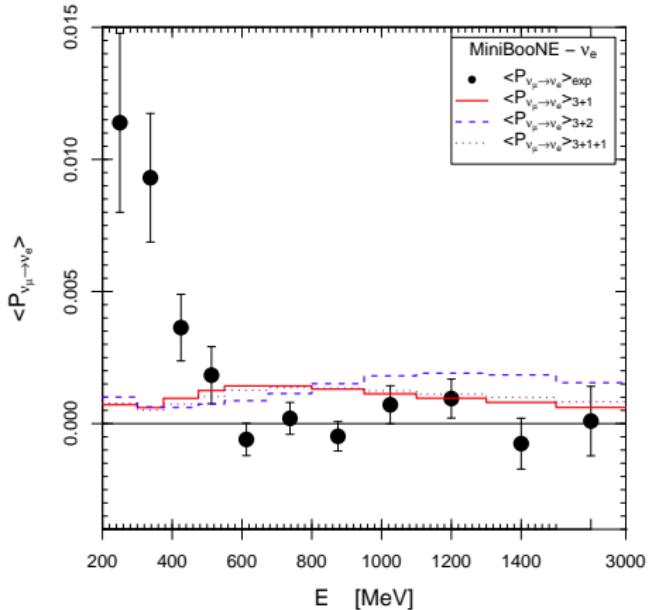
- Good: CP violation
- Bad: Two massive sterile neutrinos at the eV scale!

4 more parameters:  $\underbrace{\Delta m_{41}^2, |U_{e4}|^2, |U_{\mu 4}|^2, \Delta m_{51}^2, |U_{e5}|^2, |U_{\mu 5}|^2, \eta}_{3+1}$

# 3+2

- ▶ 3+2 should be preferred to 3+1 only if
  - ▶ there is evidence of two peaks of the probability corresponding to two  $\Delta m^2$ 's  
or
  - ▶ there is CP-violating difference of  $\nu_\mu \rightarrow \nu_e$  and  $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$  transitions
- ▶ 2008  $\nu$  + 2010  $\bar{\nu}$  MiniBooNE data indicated  $\nu - \bar{\nu}$  difference
  - ↓
  - reasonable and useful to consider 3+2
- ▶  $\nu - \bar{\nu}$  difference almost disappeared with 2012  $\bar{\nu}$  data
- ▶ Occam razor: 3+1 is enough!
- ▶ Different approach and conclusions:
  - ▶ Kopp, Machado, Maltoni, Schwetz, JHEP 1305 (2013) 050:  
Use all MiniBooNE data. No 3+1 global fit. 3+2 slightly preferred? Small allowed region.
  - ▶ Conrad, Ignarra, Karagiorgi, Shaevitz, Spitz, AHEP 2013 (2013) 163897:  
Use all MiniBooNE data. 3+2 strongly preferred. Very small allowed regions.

# MiniBooNE Low-Energy Excess?



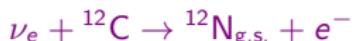
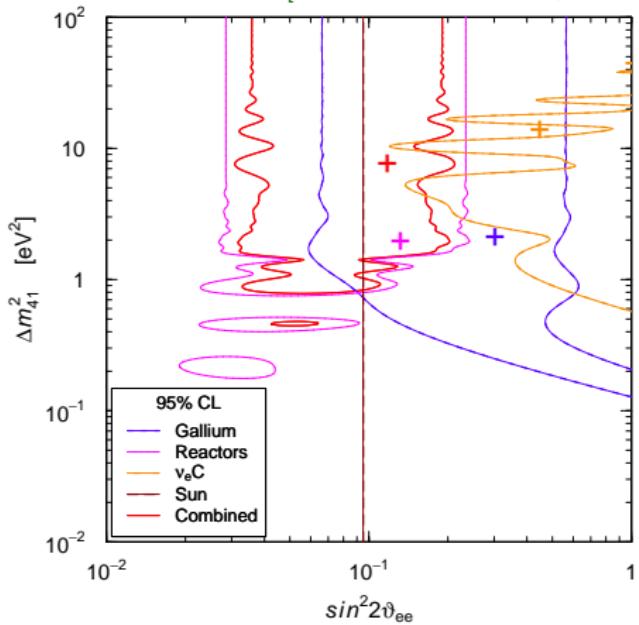
- ▶ 3+1:    GoF = 6%              PGoF = 0.2%
- ▶ 3+2:    GoF = 8%              PGoF = 0.1%
- ▶ 3+1+1: GoF = 6%              PGoF = 0.2%

	3+2 LOW	3+2 HIG	3+1+1 LOW	3+1+1 HIG
$\chi^2_{\min}$	284.4	256.4	289.8	259.0
NDF	252	246	253	247
GoF	8 %	31 %	6 %	29 %
$\Delta m^2_{41} [\text{eV}^2]$	1.9	0.93	1.6	1.6
$ U_{e4} ^2$	0.03	0.015	0.026	0.023
$ U_{\mu 4} ^2$	0.012	0.0097	0.011	0.012
$\Delta m^2_{51} [\text{eV}^2]$	4.1	1.6		
$ U_{e5} ^2$	0.013	0.018	0.0088	0.0092
$ U_{\mu 5} ^2$	0.0065	0.0091	0.0049	0.0052
$\eta/\pi$	0.51	1.6	0.4	0.45
$(\chi^2_{\min})_{\text{APP}}$	87.7	69.8	94.8	75.5
$(\chi^2_{\min})_{\text{DIS}}$	179.1	179.1	180.1	180.1
$\Delta \chi^2_{\text{PG}}$	17.7	7.5	14.9	3.4
NDF <sub>PG</sub>	4	4	3	3
GoF <sub>PG</sub>	0.1 %	11 %	0.2 %	34 %
p-val <sub>3+1</sub>	0.12	0.25	0.59	0.42
$n\sigma_{3+1}$	$1.6\sigma$	$1.2\sigma$	$0.54\sigma$	$0.81\sigma$

[Giunti, Laveder, Y.F. Li, H.W. Long, arXiv:1308.5288]

# Global $\nu_e$ and $\bar{\nu}_e$ Disappearance

[Giunti, Laveder, Y.F. Li, Q.Y. Liu, H.W. Long, PRD 86 (2012) 113014]



KARMEN + LSND

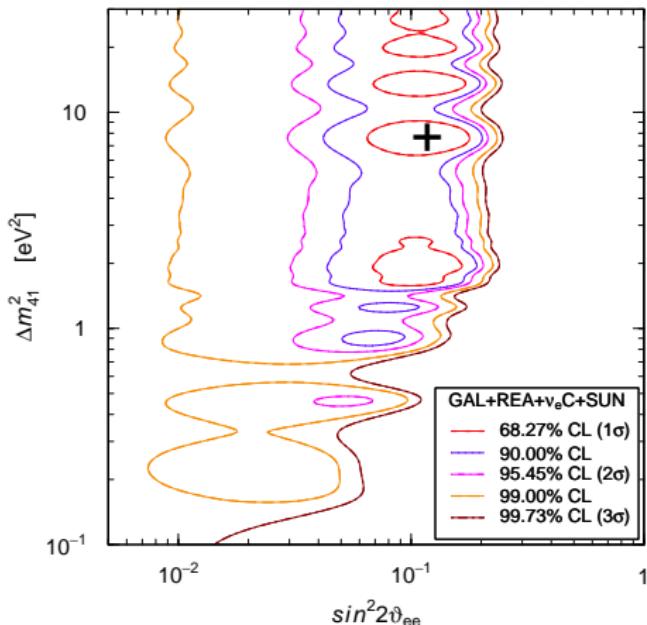
[Conrad, Shaevitz, PRD 85 (2012) 013017]

[Giunti, Laveder, PLB 706 (2011) 200]

solar  $\nu_e$  + KamLAND  $\bar{\nu}_e$  +  $\vartheta_{13}$

[Giunti, Li, PRD 80 (2009) 113007]

[Palazzo, PRD 83 (2011) 113013; PRD 85 (2012) 077301]



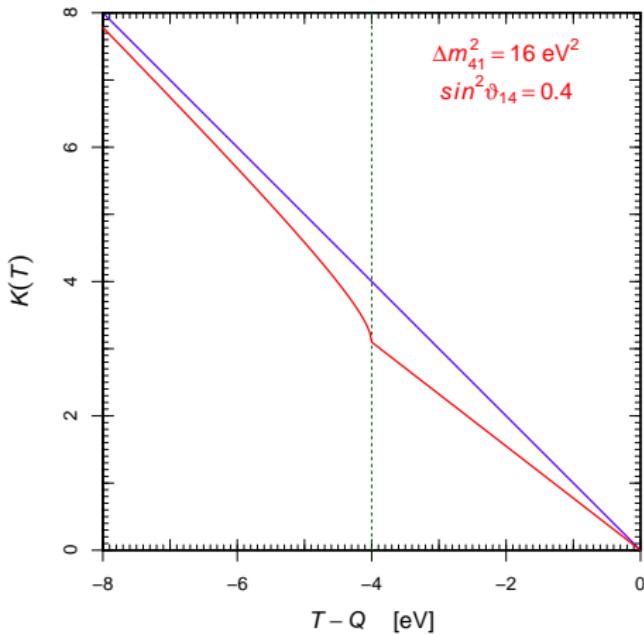
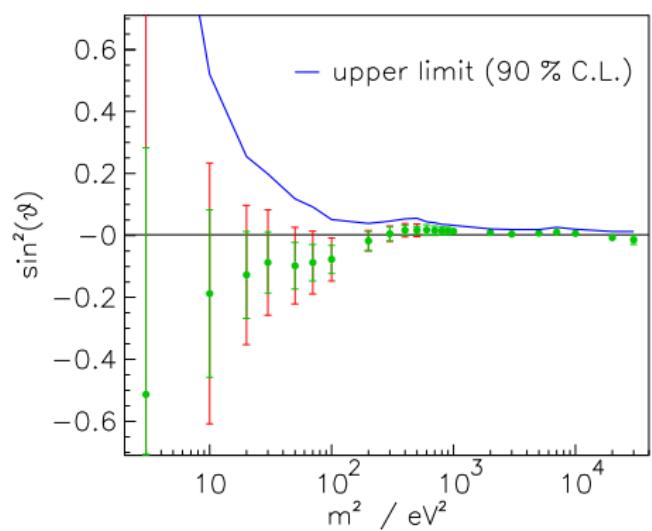
$$\text{GoF} = 62\% \quad \text{PGoF} = 4\%$$

No Osc. excluded at  $2.7\sigma$

$$\Delta\chi^2/\text{NDF} = 10.1/2$$

# Mainz Limit on $m_4^2$

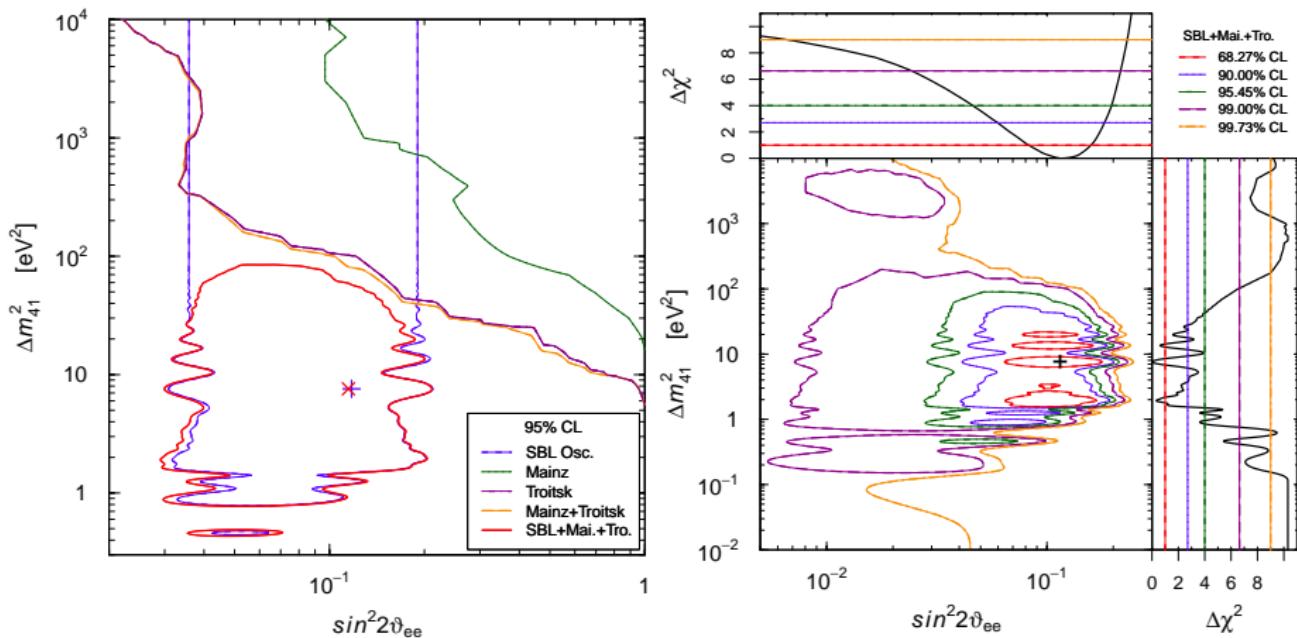
[Kraus, Singer, Valerius, Weinheimer, EPJC 73 (2013) 2323]



$$m_4 \gg m_1, m_2, m_3 \implies \Delta m_{41}^2 \equiv m_4^2 - m_1^2 \simeq m_4^2$$

# Troitsk: Surprising Much Better Limit on $m_4^2$

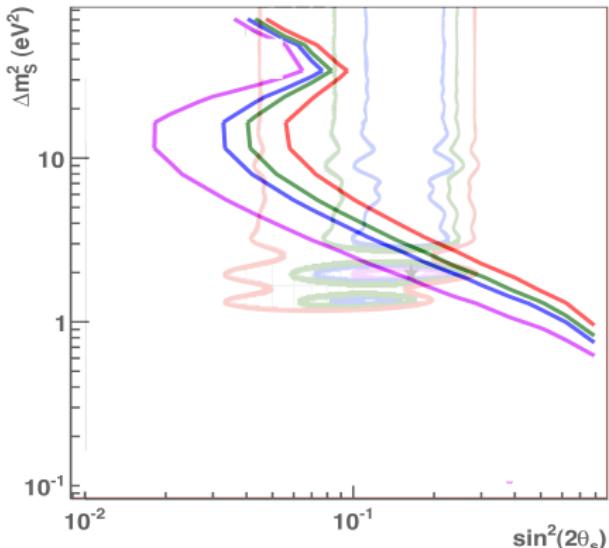
[Belesev et al, JETP Lett. 97 (2013) 67; arXiv:1307.5687]



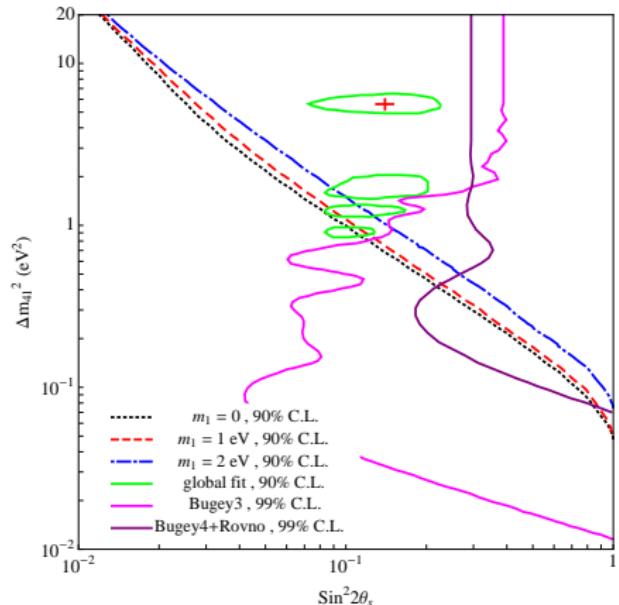
$$2\sigma : \quad 0.85 \lesssim \Delta m_{41}^2 \lesssim 43 \text{ eV}^2 \quad \Rightarrow \quad 6 \text{ cm} \lesssim \frac{L_{41}^{\text{osc}}}{E [\text{MeV}]} \lesssim 3 \text{ m}$$

[Giunti, Laveder, Y.F. Li, H.W. Long, PRD 87 (2013) 013004]

# KATRIN Sensitivity



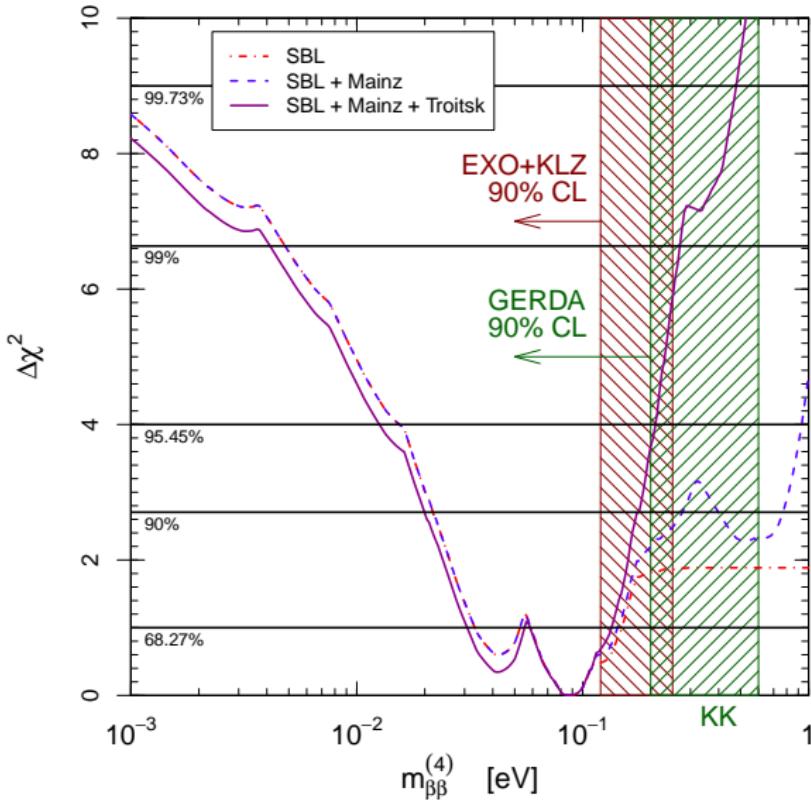
[Formaggio, Barrett, PLB 706 (2011) 68]



[Esmaili, Peres, PRD 85 (2012) 117301]

[see also Sejersen Riis, Hannestad, JCAP (2011) 1475; Sejersen Riis, Hannestad, Weinheimer, PRC 84 (2011) 045503]

# Neutrinoless Double- $\beta$ Decay



$$|m_{\beta\beta}| = \left| \sum_{k=1}^4 U_{ek}^2 m_k \right|$$

$$m_{\beta\beta}^{(4)} = |U_{e4}|^2 \sqrt{\Delta m_{41}^2}$$

caveat:  
possible cancellation  
with  $m_{\beta\beta}^{(3\nu-IH)}$

[Barry et al, JHEP 07 (2011) 091]

[Li, Liu, PLB 706 (2012) 406]

[Rodejohann, JPG 39 (2012) 124008]