Neutrino Physics: Non-Accelerator Results



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Neutrinos in the Standard Model



In the Standard Model, $m_{\nu} \equiv 0$. (Current limit is $\sum m_i < \sim 0.6$ eV). Neutrinos are many orders of magnitude lighter than the other fermions.



Only weak interactions — carried by very heavy W, Z particles with short ranges Flavour universality: identical couplings to all generations

Flavour conservation at all vertices: "electron-ness", "mu-ness", & "tau-ness" are conserved quantities (although not required by any symmetry of Lagrangian)



Weak interactions only couple to left-handed ν 's, or right-handed $\bar{\nu}$'s

This is a pure V-A interaction (maximally parity violating). Weak current has the form:

$$j_{\mu} = \bar{\psi}\gamma_{\mu}(1-\gamma_5)\psi$$

Right-handed ν 's either don't exist, or are sterile (don't interact).

A plausible, but wrong, argument ...

- 1. Ockham's Razor: the simplest solution is if right-handed ν 's don't exist.
- 2. In Standard Model, mass couples left-handed and right-handed states.
- 3. Therefore, to avoid right-handed states, neutrinos should have no mass.

Neutrino Flavour Mixing

In Standard Model, neutrinos are rather boring ... they have no mass, and only seem to be there to conserve lepton number, flavour number, and energy/momenta/spin.

In 1962, Maki, Nakagawa, and Sakata proposed, on the basis of *zero* experimental evidence, a new phenomenon called neutrino oscillation.

To understand what led MNS to this, let's look at quark mixing first.

Weak Interactions with Quarks

The simple version: W particle couples $u \leftrightarrow d$, $c \leftrightarrow s$, $t \leftrightarrow b$,



But this can't be complete, since we see weak decays such as:

$$\Lambda(uds) \rightarrow p(uud) + \pi^{-}(d\bar{u})$$

Somehow the strange quark in the Λ gets turned into an up quark!

Quark Flavour Mixing

In reality, W particle couplings mix quark generations:



We say that flavour eigenstates (eg. d,s,b) are *rotated* with respect to weak eigenstates (d',s',b')

$$\left(\begin{array}{c} u \\ d' \end{array}\right) \quad \left(\begin{array}{c} c \\ s' \end{array}\right) \quad \left(\begin{array}{c} t \\ b' \end{array}\right)$$

$$\begin{pmatrix} d' \\ s' \\ b' \end{pmatrix} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix} \begin{pmatrix} d \\ s \\ b \end{pmatrix}$$

This allows generation-mixing decays such as $\Lambda(uds) \to p\pi^-$

Neutrino Mixing



Since ν 's have only weak interactions, flavour eigenstates are defined as those states that couple to W. So it's not sensible to talk of rotation between weak eigenstate and flavour eigenstates.

But what if the flavour eigenstates are rotated relative to the *mass* eigenstates (eigenstates of Hamiltonian with well-defined mass)?

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 3} & U_{\tau 3} \end{bmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

How does superposition of mass eigenstates evolve in vacuum?

$$\begin{aligned} |\nu_e\rangle &= \cos\theta |\nu_1\rangle + \sin\theta |\nu_2\rangle \\ |\nu_\mu\rangle &= -\sin\theta |\nu_1\rangle + \cos\theta |\nu_2\rangle \end{aligned}$$

Each term evolves with a phase factor of $e^{i(px-Et)}$

If $m_1 \neq m_2$, then arguments of exponential will be different! For example, if we consider p to be fixed, then

$$E = \sqrt{p^2 + m^2} = p\sqrt{1 + m^2/p^2} \approx p + m^2/(2p)$$

As neutrino propagates, a phase difference develops between terms!

$$|\nu(t)\rangle \propto \cos\theta |\nu_1\rangle + e^{i\phi}\sin\theta |\nu_2\rangle$$

with

 $\phi = \left(\frac{m_1^2}{2p} - \frac{m_2^2}{2p}\right)t$

Neutrino Oscillation

Net result: at some later time, $|\nu(t)\rangle \neq |\nu_e\rangle$.

Probability that the original ν_e is detected as a ν_{μ} at some later time:

$$P(\nu_e \to \nu_\mu) = |\langle \nu_\mu | \nu(t) \rangle|^2 = \sin^2 2\theta \sin^2 \left(\frac{1.27\Delta m^2 L}{E}\right)$$



 θ = neutrino mixing angle Δm^2 = $m_1^2 - m_2^2$ (in eV²) L = distance ν has travelled (in km)

Neutrino oscillation:

- requires at least one non-zero neutrino mass
- requires non-zero mixing elements
- results from the QM of the propagation, not from an interaction

Matter Effects On Neutrino Oscillation

Surprisingly the oscillation formula can be dramatically altered in matter!

$$i\frac{d}{dt}\left(\begin{array}{c}\nu_{e}\\\nu_{\mu}\end{array}\right) = \left(\begin{array}{c}-\frac{\Delta m^{2}}{4E}\cos 2\theta + \sqrt{2}G_{F}N_{e} & \frac{\Delta m^{2}}{4E}\sin 2\theta\\\frac{\Delta m^{2}}{4E}\sin 2\theta & \frac{\Delta m^{2}}{4E}\cos 2\theta\end{array}\right)\left(\begin{array}{c}\nu_{e}\\\nu_{\mu}\end{array}\right)$$

The relevant process is forward scattering, in which no momentum is exchanged. In matter, ν_e 's have a different forward scattering amplitude than the other flavours:



This produces a matter-induced potential that is different for ν_e . Effectively ν_e 's have a different "index of refraction" in matter. The size of the potential is proportional to the electron density N_e .

For solar ν 's, matter effects are dominant.



Atmospheric Neutrinos



Super-Kamiokande



veto tubes

1 km overburden

Super-Kamiokande Atmospheric ν Results





PRD 71, 112005 (2005)

Super-K sees suppression of ν_{μ} flux at large zenith angles (distances).

 ν_e flux is unaffected.

Looks to be $u_{\mu}
ightarrow
u_{ au}$ oscillations

Super-K provided first clear evidence for neutrino oscillations (1998)!

Super-Kamiokande: Evidence for oscillatory signature



A subset of well-reconstructed events is used to do an L/E analysis.

Dip at the first oscillation minimum is a signature of oscillation .

Alternate models of neutrino decay, decoherence ruled out at $\sim 5\sigma$ level.

Taus or Steriles?

u_{τ} search at Super-K



Hypothesis of no ν_{τ} appearance disfavored by 2.4 σ

PRL 97, 171801 (2006)

 $u_{\mu} \rightarrow \nu_{sterile}$? Different angular distribution due to matter effects.



Purely $u_{\mu}
ightarrow
u_{sterile}$ ruled out at 7 σ

Solar Neutrinos

The Sun is an intense source of MeV neutrinos! $4p + 2e^- \rightarrow {}^4\text{He} + 2\nu_e + 26.731 \text{ MeV}$





The Pioneers



The ³⁷Cl experiment started in the 1960's Ray Davis and John Bahcall with the tetrachloroethylene tank. 100,000 gallons of cleaning fluid!

$$\nu_e + {}^{37}\mathrm{Cl}
ightarrow e^- + {}^{37}\mathrm{Ar}$$



"There's room for a lot of science if I choose this route and just start doing things."

A setback ...

Predicted rate: $7.6^{+1.3}_{-1.1}$ SNU's Measured rate: 2.56 ± 0.23 SNU's

Most people reacted in two ways ...

- Experiment must be wrong. No one can look for 50 Ar atoms in 600 tons of cleaning fluid and expect to find them all!
- Theory must be wrong. The solar models are too complicated to take seriously. The flux changes with solar temperature by T^{25} . Even a tiny mistake could change fluxes greatly!

Ray Davis checked and rechecked his experiment. John Bahcall refined astrophysical calculations. Both stuck to their guns.

Others began planning new experiments ...

Super-Kamiokande Solar Neutrino results

 $\nu_x + e^- \rightarrow \nu_x + e^-$

Rate $\propto \phi(\nu_e) + rac{1}{6}\phi(
u_{\mu au})$

 $\phi = 2.35 \pm 0.02 \pm 0.08 \times 10^{6} \ \nu/\text{cm}^{2}/\text{s}$ $\phi_{SSM} = 5.69 \pm 0.91 \times 10^{6} \ \nu/\text{cm}^{2}/\text{s}$

(PRD 73 (2006) 112001)

Clear directional ν signal from Sun!



No day-night variations (matter effects) or spectral distortions seen—could simply be seeing flux suppression.





Solar Neutrino Flux Measurements

Two Classes of Experiment (pre-SNO)

- Radiochemical
 - u_e interactions convert target nuclei
 - Radioactive products extracted and counted after exposure time
- Water Cerenkov
 - Real-time detection of scattered atomic e^- 's
 - Mixed CC and NC sensitivity



Experiment	Detection Reaction	Threshold	Primary Sources
Homestake	$ u_e + {}^{37}\text{Cl} \rightarrow e^- + {}^{37}\text{Ar}$	0.8 MeV	⁷ Be, ⁸ B
Kamiokande	$\nu_{e,(\mu,\tau)} + e \rightarrow \nu_{e,(\mu,\tau)} + e$	7.3 MeV	⁸ B
SAGE, GALLEX/GNO	$ u_e + {}^{71}\text{Ga} ightarrow e^+ + {}^{71}\text{Ge}$	0.23 MeV	<i>pp</i> , ⁷ Be, ⁸ B
Super-K	$\nu_{e,(\mu,\tau)} + e \rightarrow \nu_{e,(\mu,\tau)} + e$	5 MeV	⁸ B

The Solar Neutrino Problem

• Standard Solar Model Predictions:



Sudbury Neutrino Observatory 2092 m to Surface 18 m Diameter Support Structure for 9500 PMTs, 60% coverage 1000 Tonnes D₂O 12 m Diameter Acrylic Vessel 1700 Tonnes Inner Shielding H₂O 5300 Tonnes Outer Shield H₂O

Urylon Liner and Radon Seal

SNO Neutrino Event



Solar ν Interactions in SNO



For the favored Large Mixing Angle (LMA) solution to solar neutrino problem:

$$|U_{e2}|^2 \approx \sin^2 \theta_{12} \approx \frac{\phi_{CC}}{\phi_{NC}}$$

Three Phases of the SNO Experiment

D_2O Phase	Salt Phase	NCD Phase
(pure D_20)	$(D_2O + 0.2\% \text{ NaCl})$	(³ He counters)
Nov 1999 - May 2001	July 2001 - Sept 2003	Dec 2004 - Dec 2006
$n+d ightarrow t+\gamma$	$n+{}^{35}$ Cl $ ightarrow{}^{36}$ Cl $+\gamma$'s	$n+^3$ He $ ightarrow p+t$
$(\sigma=0.0005b)$	$(\sigma=44~b)$	$(\sigma=5330b)$
Detect a Compton- scattered electron from a 6.25 MeV γ	Detect Compton-scattered electrons from multiple γ 's totalling 8.6 MeV	Detect 764 keV of ionization from the charged particles in ³ He proportional counters
PRL 87, 071301 (2001) PRL 89, 011301 (2002) PRL 89, 011302 (2002) PRD 70, 093014 (2004)	PRL 92, 181301 (2004) PRL 92, 102004 (2004) PRC 72, 055502 (2005) PRD 72, 052010 (2005)	Analysis in progress

SNO Signal Probability Distributions



Fit the PDFs to the data to determine fluxes. Leave out the energy PDFs to fit for the spectral shapes.

Fits to SNO Salt Phase Data



Evidence for Solar Neutrino Flavour Transformation



oscillation?

30

SNO Neutron Capture Detectors



An array of 3 He proportional counters inside D₂O to detect neutrons using the ionization signal from

${}^{3}\mathrm{He} \, {\rm \textbf{+}}\, n \rightarrow p + t$

Photo of NCD counters from above



Goals of NCD phase:

- Measure NC flux with different systematics
- Break CC/NC statistical correlation
- Reduced uncertainty on CC/NC ratio \rightarrow better measurement of θ_{12}



Future Solar Neutrino Experiments



There are various ideas for precision measurement of ⁷Be and pep neutrinos by low-background scintillator detectors:

- Borexino
- KamLAND
- SNO+
- liquid noble gas detectors

- Constrain solar models
- Test exotic scenarios: non-standard interactions, mass-varying neutrinos, spin-favour precession ...

See Tony Noble's talk for more.

Evidence for Reactor Neutrino Oscillations





KamLAND: Observation of reactor neutrino disappearance at L/E value where solar neutrino effect occurs.

Evidence for Reactor Neutrino Oscillations



KamLAND: L/E analysis



KamLAND & solar neutrino together:

- confirm oscillation as the cause of the observed flavour transformation
- provide precise measurements of solar ν mixing parameters (e.g. $\delta(\Delta m^2)\sim 10\%$

The 3×3 framework



mass

Two Δm^2 values, but hierarchy (sign of Δm^2_{23}) uncertain.

Two well-determined mixing parameters, but θ_{13} and δ_{CP} unknown!

$$\begin{pmatrix} \nu_{e} \\ \nu_{\mu} \\ \nu_{\tau} \end{pmatrix} = \begin{bmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu 1} & U_{\mu 2} & U_{\mu 3} \\ U_{\tau 1} & U_{\tau 3} & U_{\tau 3} \end{bmatrix} \begin{pmatrix} \nu_{1} \\ \nu_{2} \\ \nu_{3} \end{pmatrix}$$

$$\approx \begin{bmatrix} 0.9 & 0.5 & s_{13}e^{i\delta} \\ -0.35 & 0.6 & 0.7 \\ 0.35 & -0.6 & 0.7 \end{bmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Reactor θ_{13} Experiments

$$P(\bar{\nu}_e \to \bar{\nu}_e) = 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{1.27\Delta m_{13}^2 L}{E}\right) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \left(\frac{1.27\Delta m_{12}^2 L}{E}\right)$$

Remember that KamLAND saw oscillation of reactor neutrinos at $L\approx 180$ km?



But what about those reactor experiments at *short* distances that saw nothing?

For $\Delta m^2_{13} \approx 2.5 \times 10^{-3}$ and $E \sim 5$ MeV, should have oscillation maximum at $L \approx 2$ km.

Since this is driven by oscillation between ν_1 and ν_3 , the relevant mixing angle is the mixing between ν_e and ν_3 —that is, θ_{13} .

CHOOZ limits:

 $R = 1.01 \pm 0.028 \,(\text{stat}) \pm 0.027 \,(\text{sys})$

 $\sin^2 2\theta_{13} < 0.15 \ (90\% C.L.)$

New θ_{13} Experiments

A next generation reactor experiment could improve the θ_{13} limit by an order of magnitude by:

- Large increase in statistics: use a GW-scale reactor and run for a few hundred GW-tonne-years
- Reduce systematics to < 1%: use both a near and a far detector to cancel systematics.
- Better detector design

Reactor experiments sensitive *only* to θ_{13} , not δ_{CP} or matter effects. Very complementary!



The Double CHOOZ far detector *Many* proposals: Double CHOOZ (France), Daya Bay (China), Angra (Brazil), RENO (Korea), ...



- Neutrinos have mass and oscillate. Compelling evidence from four different kinds of experiments:
 - 1. atmospheric neutrinos
 - 2. solar neutrinos
 - 3. reactor neutrinos
 - 4. long baseline neutrino beams (not covered in this talk)
- Neutrino mixing opens a whole new area of lepton flavour physics. *This is new physics beyond the Standard Model, involving new fields and new fundamental constants!*
- Non-accelerator neutrino physics has played the critical role in the revolution in neutrino physics.

Backup slides follow

KamLAND detector



(hep-ex/0212021)

Neutrino Mass Hierarchy



Neutrino Mixing Matrix

Adjust L/E to view oscillations at different Δm^2 's

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & e^{i\delta}s_{13} \\ 0 & 1 & 0 \\ -e^{-i\delta}s_{13} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Atmospheric ν 's: Short baseline reactor ν 's: Solar ν 's: $\theta_{23} \approx \pi/4$ $\theta_{13} < \pi/20$ $\theta_{12} \approx \pi/6$
Maximal mixing! (?) Small, quark-like mixing Large, non-maximal mixing

Compare to identical parameterization of CKM matrix ...

$$\theta_{23} \approx \pi/76$$
 $\theta_{13} \approx \pi/870$ $\theta_{12} \approx \pi/14$

Non-Standard Neutrino Interactions

Neutrino oscillation adds mixing between mass and flavour eigenstates to the SM, but doesn't alter the allowed interactions themselves. All interactions are still left-handed, flavour-conserving, and obey flavour universality.

But many models (GUT or otherwise) allow for violations of all of these.

Interpretation of data in terms of neutrino oscillation generally ignores the possibility of these terms.



- 1. Flavour-changing neutral currents
- 2. Altered vertex factors
- 3. Large magnetic moments ("spin-flavour precession")

Can be present as linear terms in oscillation (appear as squared terms in decays)

An example: non-standard neutrino interactions with solar ν 's





Influence of NSI on effective solar neutrino oscillation probability

Plots from Mirana, Tortola, and Valle (hep-ph/0406280)

Bad news: neutrino interactions are the most poorly constrained of all SM interactions, for obvious experimental reasons

Good news: searches for NSI are sensitive to new physics at the TeV scale

Determining the Absolute Neutrino Mass

What is the Absolute Neutrino Mass?

Three extreme cases:

NORMAL HIERARCHICAL	INVERTED HIERARCHY	DEGENERATE
$m_1 \ll m_2 \ll m_3$	$m_1 pprox m_2 \gg m_3$	$m_1 pprox m_2 pprox m_3$

m_1	\approx	0	m_1	\approx	$\sqrt{\Delta m^2_{23}}$	m_1	\sim	$0.2\mathrm{eV}$
m_2	\approx	$\sqrt{\Delta m_{12}^2}$		\approx	$0.050 \mathrm{eV}$	m_2	\sim	$0.2\mathrm{eV}$
	\approx	$0.009\mathrm{eV}$	m_2	\approx	$\sqrt{\Delta m_{23}^2}$	m_3	\sim	$0.2\mathrm{eV}$
m_3	\approx	$\sqrt{\Delta m^2_{23}}$		\approx	$0.050 \mathrm{eV}$			
	\approx	$0.050\mathrm{eV}$	m_3	\approx	0			

(Most like other fermions. Favoured by GUTs)

Personal prejudice favors normal hierarchical, but all are possible, as are intermediate cases.



KATRIN collaboration, hep-ex/0109033

Most sensitive ν_e searches come from measuring the endpoint of the energy spectrum of tritium decay.

$$m(\nu_e) \le 2.5 \text{ eV} \ (95\% \ C.L.)$$

KATRIN proposal: new tritium endpoint measurement with sensitivity down to 0.2 eV

Collider limits:

 $m(
u_{\mu}) < 190~{
m keV}$ (90% C.L.) $m(
u_{ au}) < 18.2~{
m MeV}$ (95% C.L.)

Cosmological Mass Limits

 10^{5}

Neutrinos constitute "hot dark matter":

$$\Omega_{\nu}h^{2} = \frac{m_{1}+m_{2}+m_{3}}{94 \text{ eV}}$$
$$n_{\nu} \approx 112 \text{ cm}^{-3}$$

Neutrinos reduce clustering at small angular scales during structure formation, since they "stream out of" small density perturbations.

This can leave signatures in, for example

- CMB
- large scale structure
- weak lenses

Oscillation experiments limit $\Omega_{\nu} > 0.001$, about the same mass as in stars!



= 0.5 eV

Effects of neutrino mass on large scale structure (angular power spectrum), with 2dFGRS data superimposed. Adopted from Elgaroy and Lahav, hep-ph/0412075

= 3.0 eV

Various model-dependent limits:

$$\sum_{i} m_i < \sim 0.4 - 0.7 \,\mathrm{eV}$$

Cosmology could well be the only way to determine m_{ν} if small!

 $= 0.0 \, eV$

10⁰

Neutrinoless Double Beta Decay ($0\nu\beta\beta$)



Ordinary double beta decay occurs when single beta decay is energetically surpressed, but double beta decay isn't. A doubly weak process—very rare! *Neutrinoless* double beta decay violates lepton number $(|\Delta L| = 2)$, but is allowed if a neutrino is its own antiparticle. Rate of $0\nu\beta\beta$ decay depends on effective neutrino mass:

$$R \propto \langle m_{\nu} \rangle^2 = \left| \sum_{i}^{N} U_{ei}^2 m_i \right|^2$$

Double Beta Decay—Experimental Technique



Experimental signature: the sum of the two electrons' energies yields a peak at the endpoint.

Current limits:

Isotope	$T_{1/2}^{0 u}$ (y)	$\langle m_{ u} angle$ (eV)
48 Ca	$> 9.5 \times 10^{21} (76\%)$	< 8.3
76 Ge	$> 1.9 \times 10^{25}$	< 0.35
	$> 1.6 \times 10^{25}$	< 0.33 - 1.35
82 Se	$> 2.7 \times 10^{22} (68\%)$	< 5
100 Mo	$> 5.5 \times 10^{22}$	< 2.1
116 Cd	$> 7 \times 10^{22}$	< 2.6
128 Te	$> 7.7 \times 10^{24}$	< 1.1 - 1.5
130 Te	$> 1.4 \times 10^{23}$	< 1.1 - 2.6
136 Xe	$> 4.4 \times 10^{23}$	< 1.8 - 5.2
150 Nd	$> 1.2 \times 10^{21}$	< 3

(Elliott & Vogel, Ann. Rev. Nucl. Part. Sci 52 (2002))

Claimed Detection for Moscow-Heidelberg Experiment



Adapted from H.V. Klapdor-Kleingrothaus, hep-ph/0512263 The Moscow-Heidelberg collaboration has previously published an upper limit on $0\nu\beta\beta$ decay in 76 Ge.

In recent years a small subset of the Moscow-Heidelberg collaboration claimed to see evidence for a positive signal (4.2σ) .

Inferred effective mass is

 $m_{\nu}\approx 0.2-0.6~{\rm eV}$

Claim is "controversial"

The MAJORANA Experiment



Proposal for a massive germanium experiment

- 86% enriched ⁷⁶Ge
- Ge gives extremely good energy resolution—great for resolving endpoint peak
- Goal is 2500 kg-years exposure
- Very clean materials, pulse shape discrimination, and segmented detectors to reject backgrounds
- "Proven" technology

Sensitivity goal: < 50 meV

The EXO Experiment



Look at 10 tonnes of 136 Xe in a liquid or gas TPC. Use laser spectroscopy on the resulting ion to confi rm it is barium, rejecting backgrounds. Sensitivity of $\sim 10~{\rm meV}$

Double Beta Decay Sensitivity



Proposed double beta decay experiments, if successfully, could distinguish between normal and inverted hierarchy, but only if ν 's are Majorana particles.

Null result by itself cannot rule out either Majorana neutrinos or largish masses.

No real idea how to improve sensitivity to cover normal hierarchy.