

# Lecture 2. CCQE

# Lecture 2: CCQE

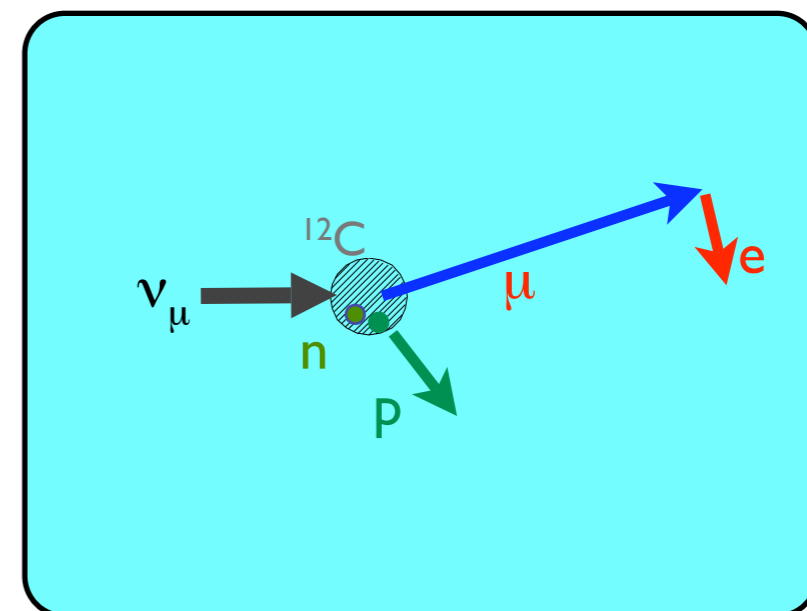
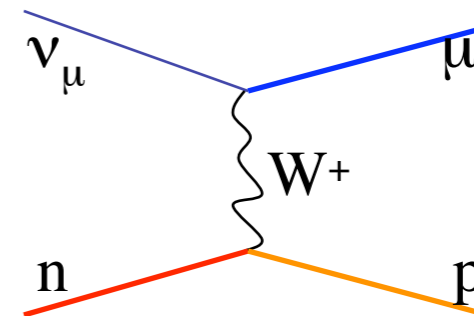
- Introduction
- Event kinematics and topology
- Experimental Searches
  - Event Selections
  - Efficiencies and Systematics
  - Extracted parameters
- Upcoming measurements



K2K  
(SciFi & SciBar),  
MiniBooNE,  
SciBooNE

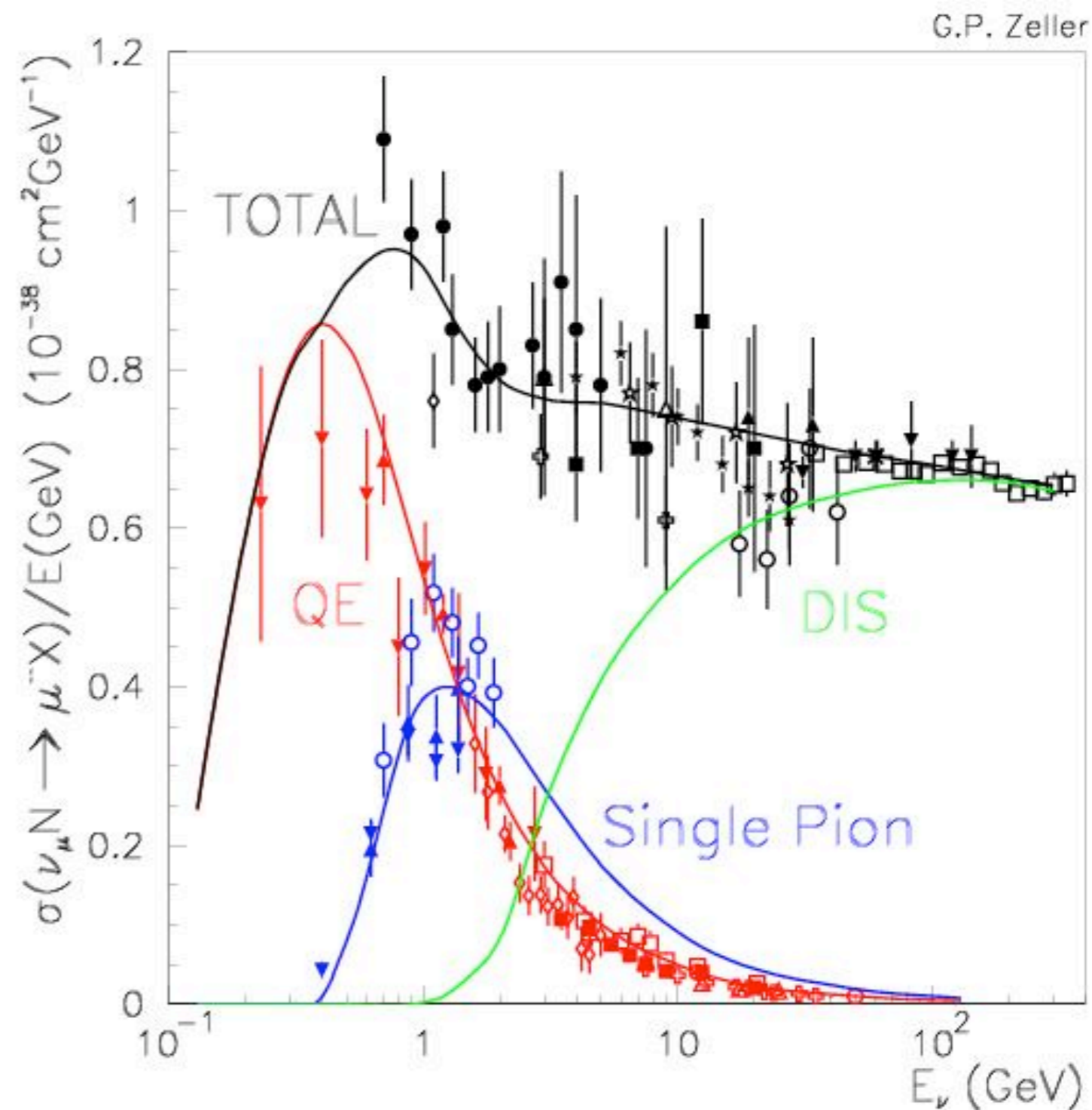
# CCQE Intro

- Terminology:
  - Charged current quasi-elastic
- Simple reaction kinematics
- Dominant reaction at 1 GeV



# CCQE Intro

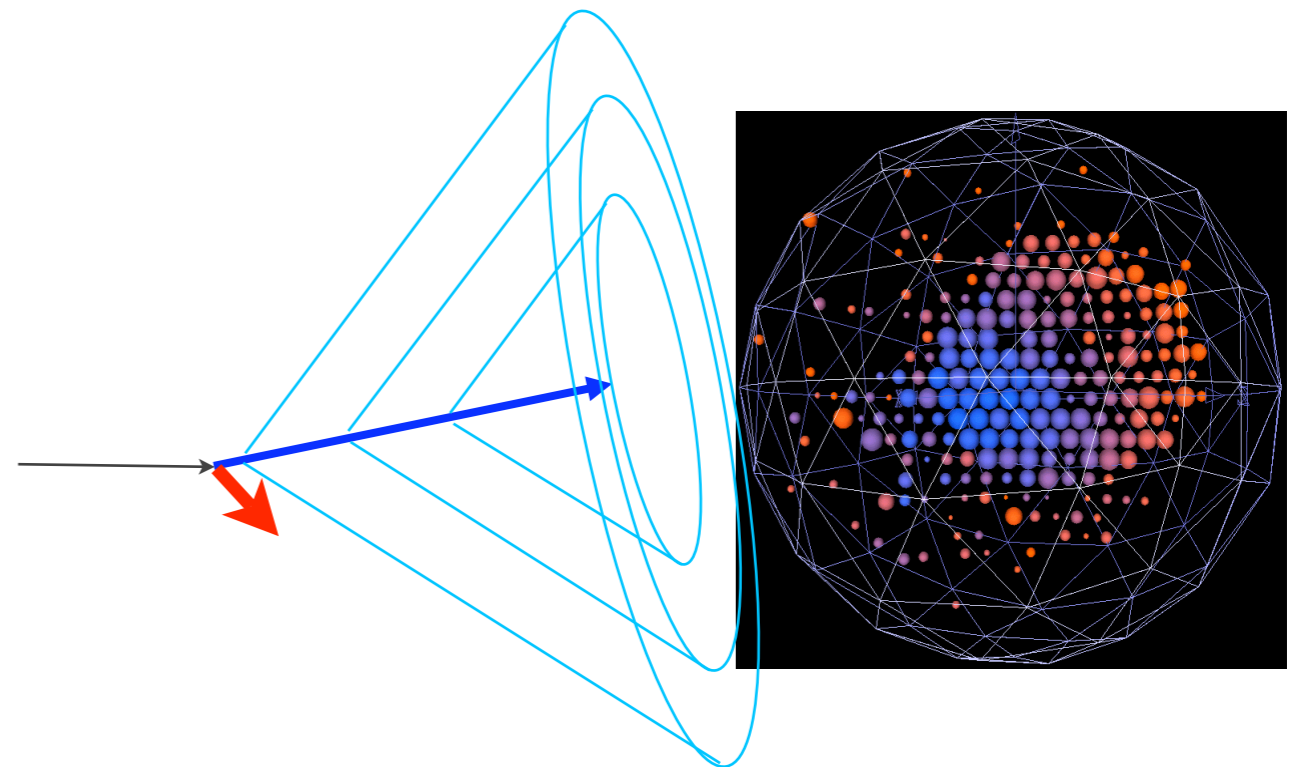
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# CCQE Intro

$$E_{\nu}^{QE} = \frac{1}{2} \frac{2M_p E_{\mu} - m_{\mu}^2}{M_p - E_{\mu} + \sqrt{(E_{\mu}^2 - m_{\mu}^2) \cos \theta_{\mu}}}$$

- Determine flux (in near detector)
- Reconstruct neutrino energy using outgoing lepton
- Energy reconstruction is important for neutrino oscillation measurements

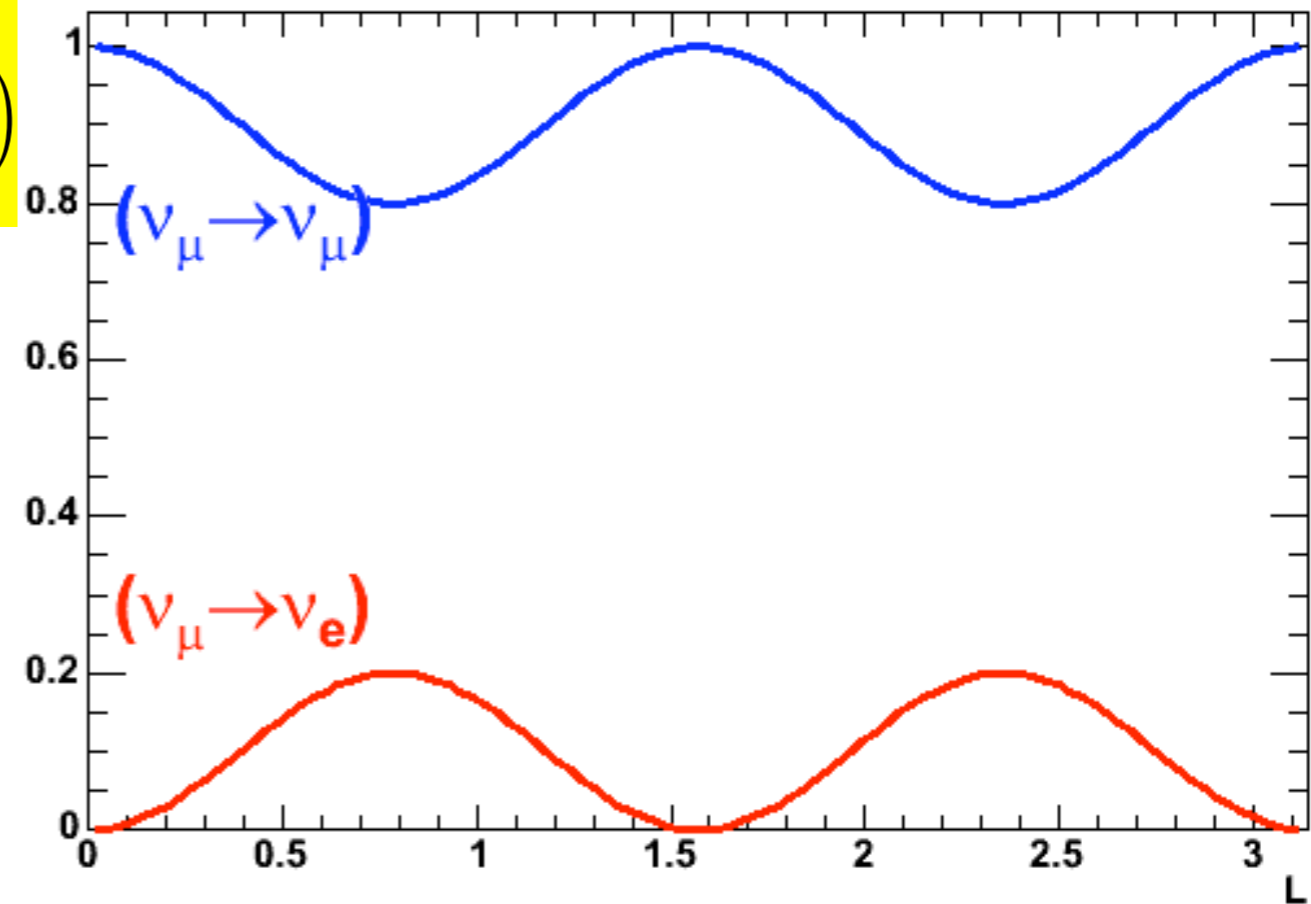


$$P_{osc}(\nu_{\mu} \rightarrow \nu_e) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 (\text{eV}^2) L (\text{km})}{E_{\nu} (\text{GeV})} \right)$$

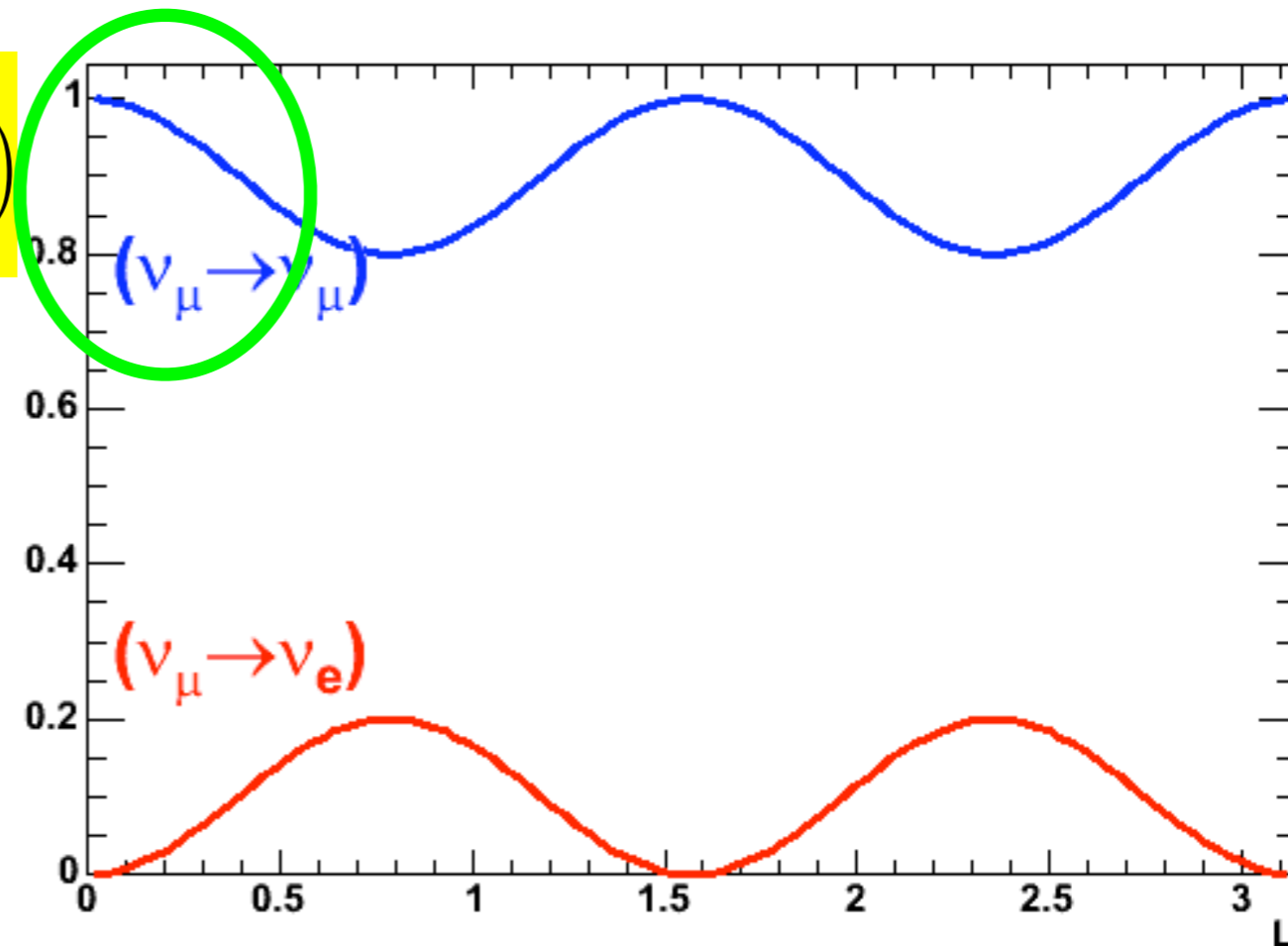


$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta_{12} \sin^2\left(1.27 \Delta m_{12}^2 \frac{L}{E}\right)$$

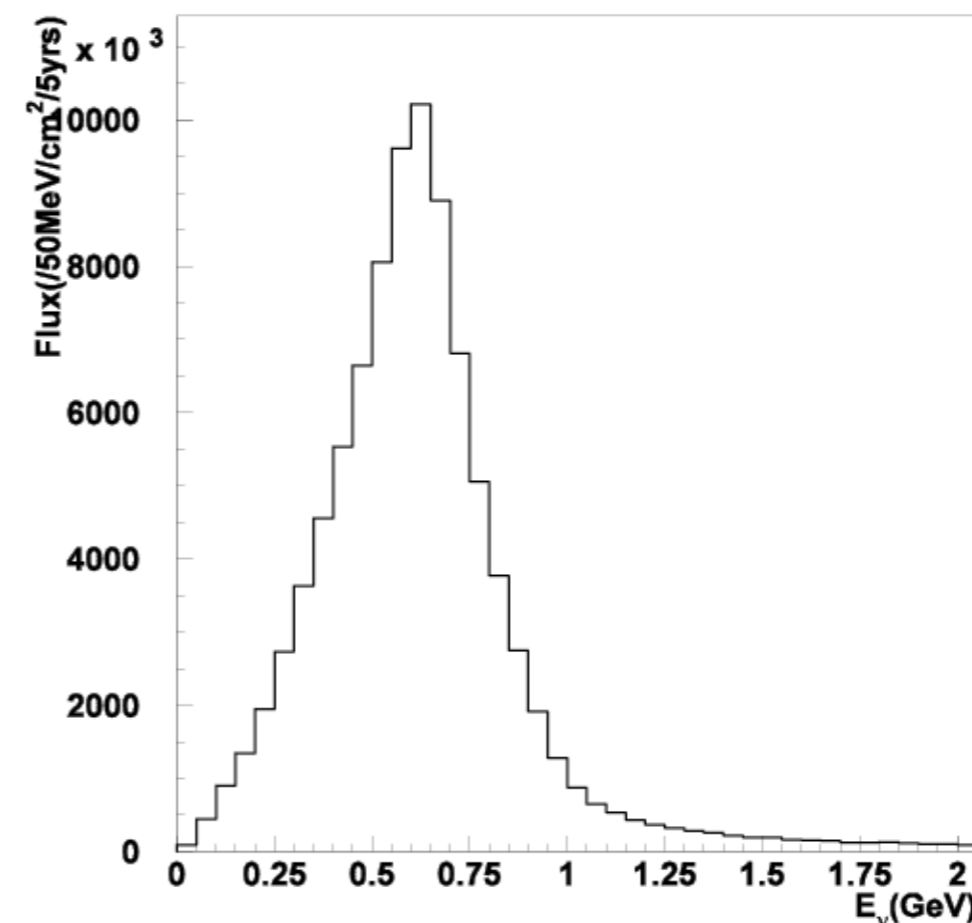
- 2 fundamental parameters
  - $\Delta m^2 \leftrightarrow$  period
  - $\theta_{12} \leftrightarrow$  magnitude
- 2 experimental parameters
  - $L =$  distance travelled
  - $E =$  neutrino energy
- Choose  $L$  &  $E$  to target ranges of  $\Delta m^2$  and  $\theta$
- Neutrinos disappear and appear



$$P(\nu_\mu \rightarrow \nu_e) = \sin^2 2\theta_{12} \sin^2\left(1.27 \Delta m_{12}^2 \frac{L}{E}\right)$$

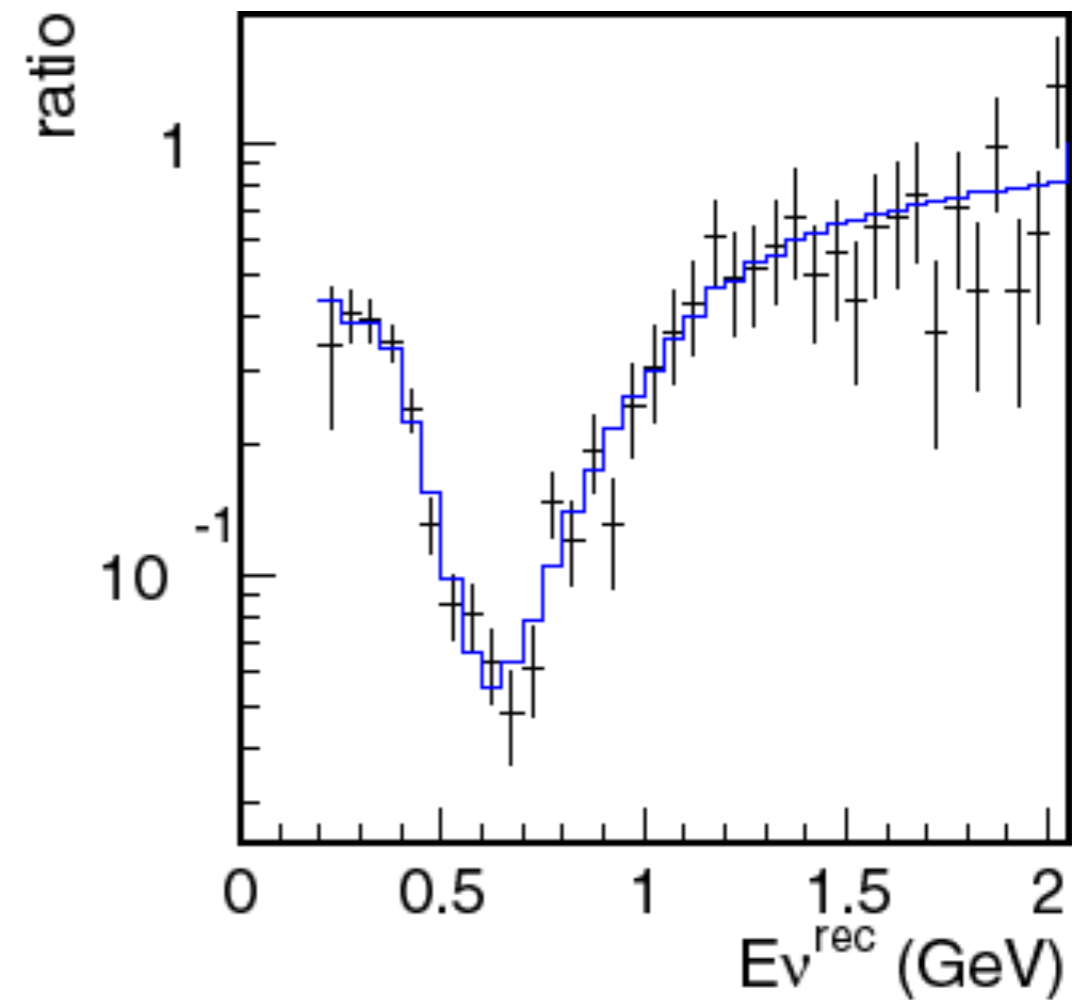
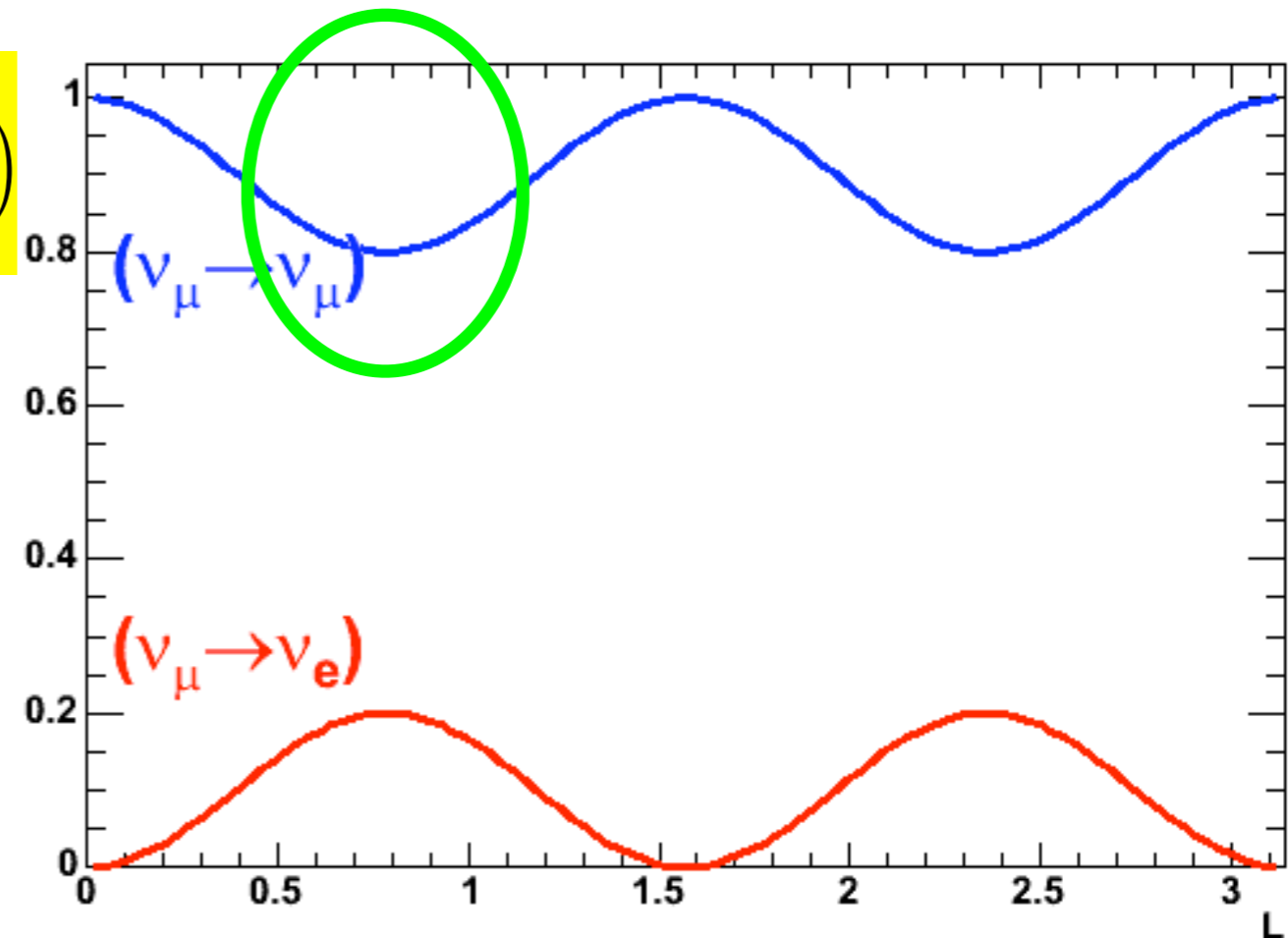


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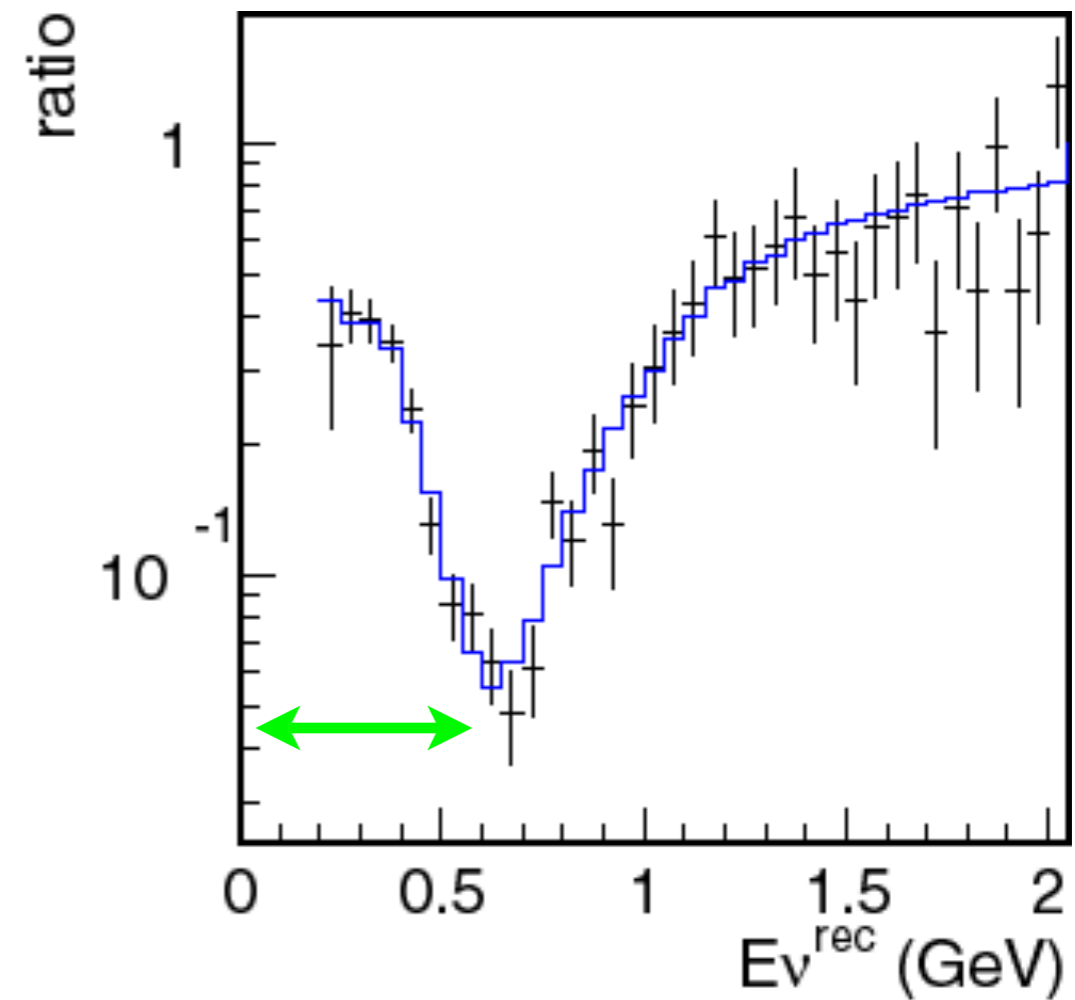
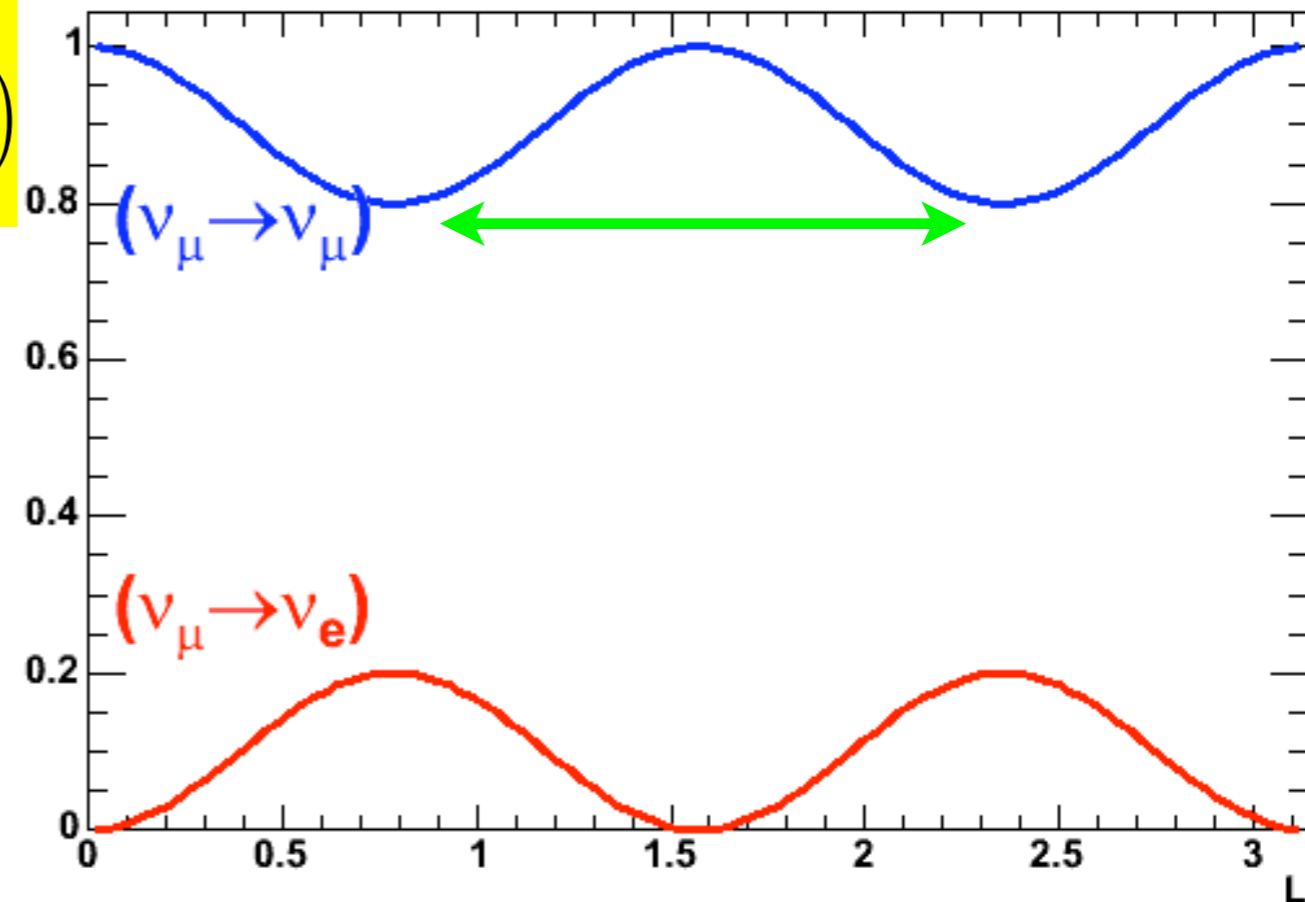
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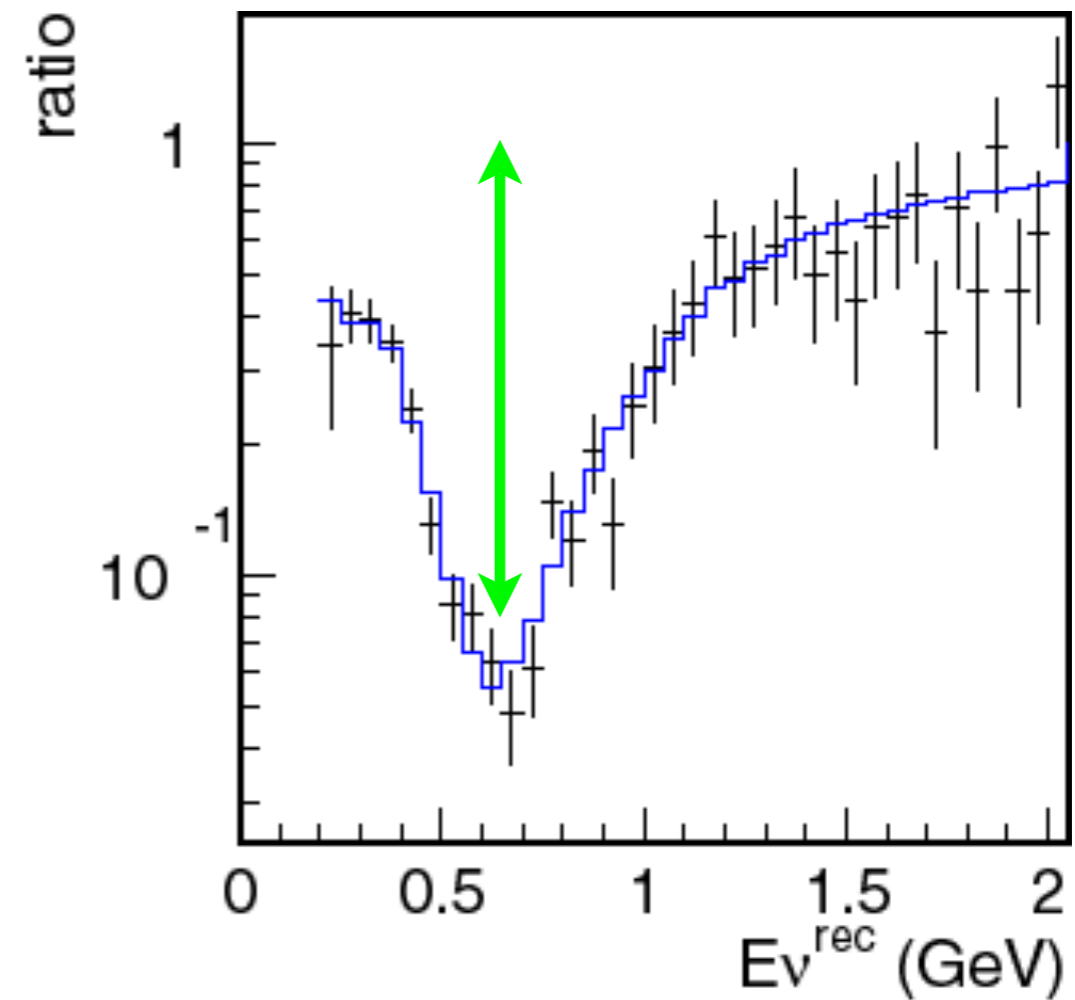
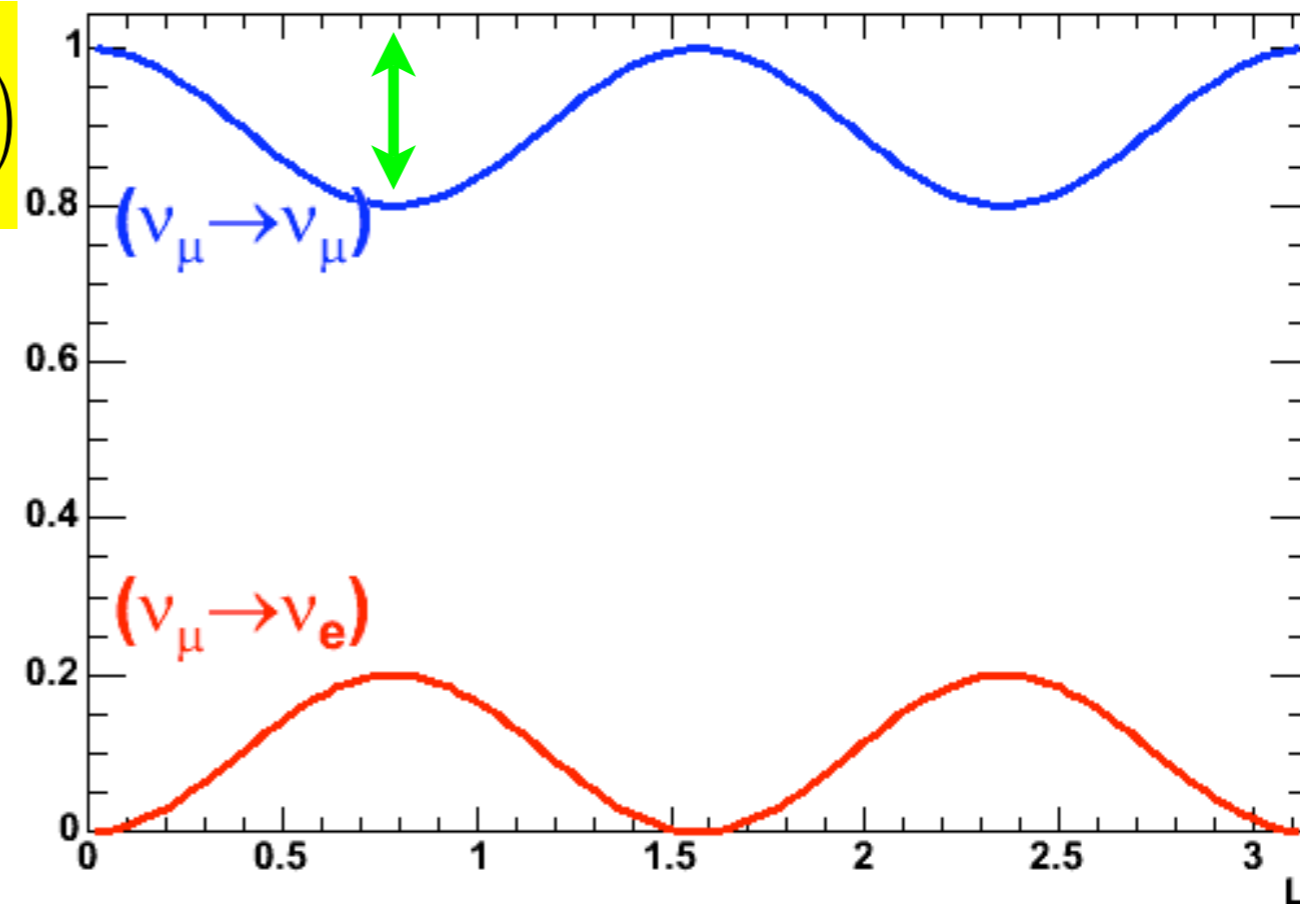
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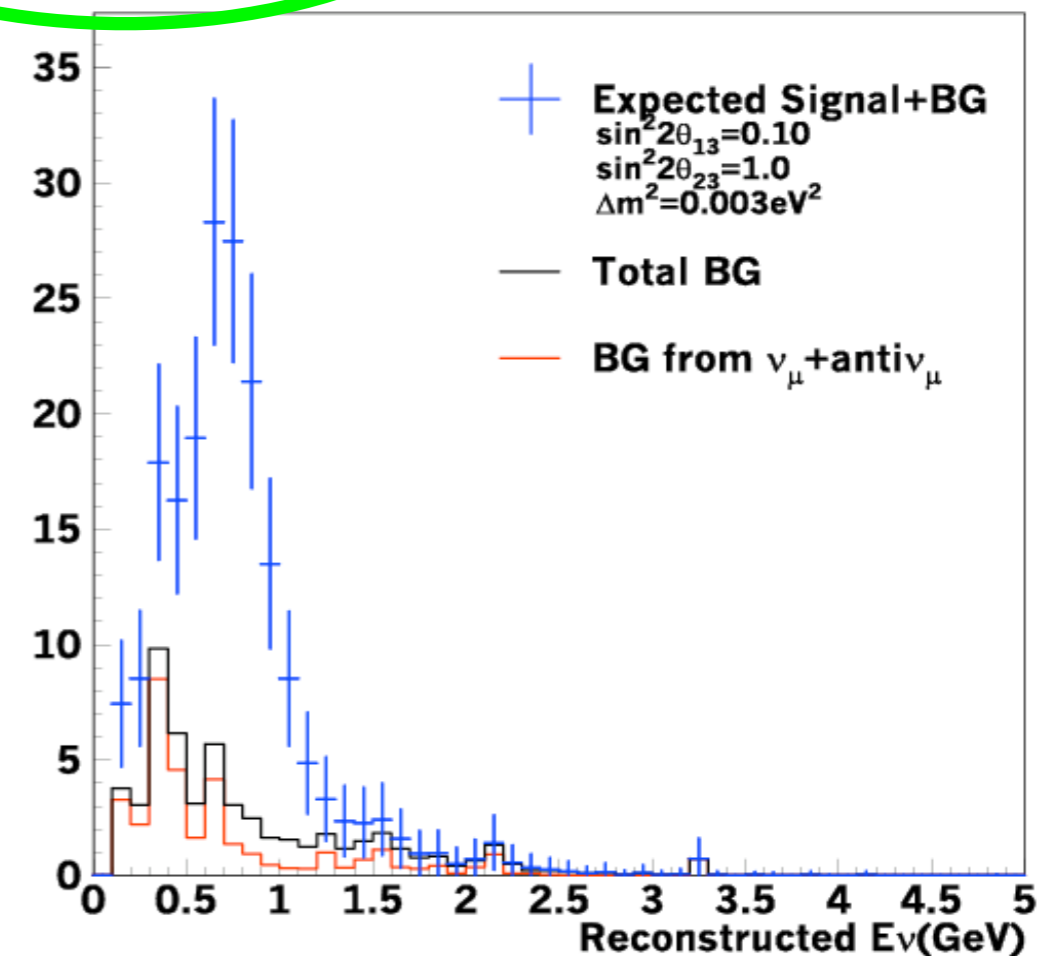
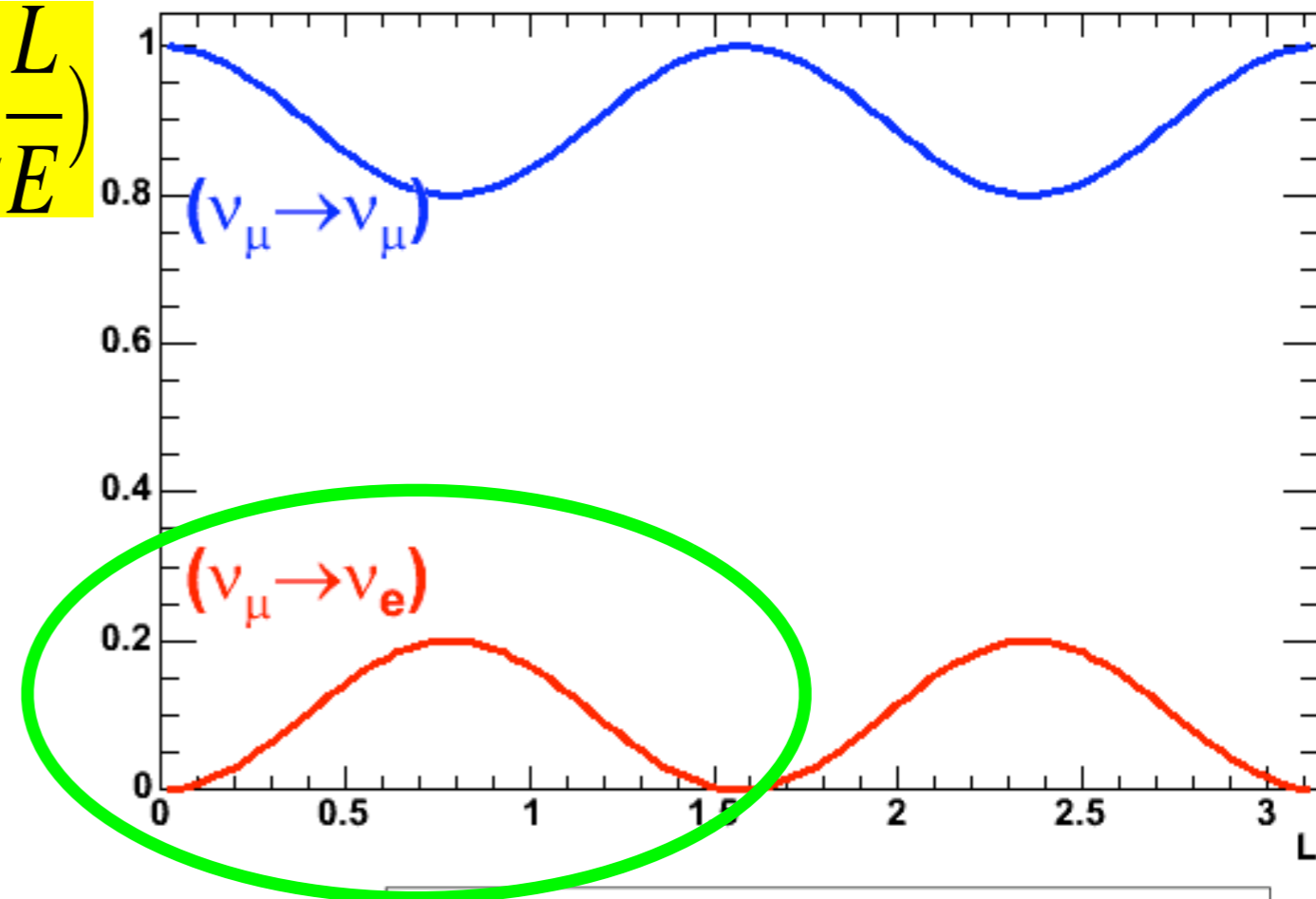
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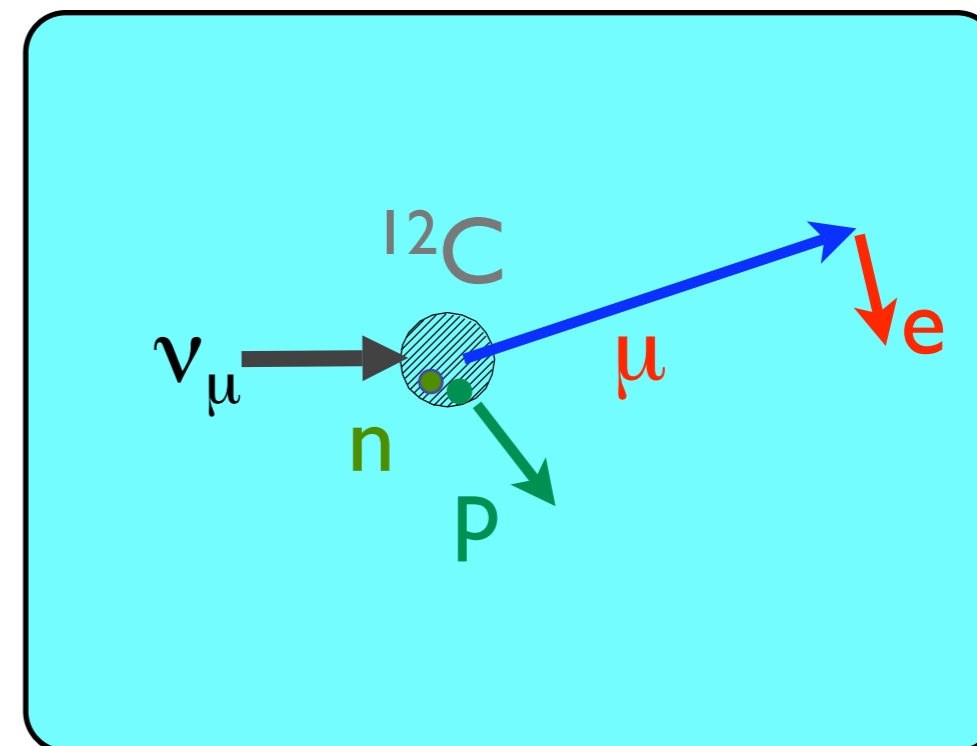
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# CCQE Topology

- Final state particles in detector:
  - Outgoing lepton
    - Key to measurement
    - Muons can be tagged with penetration, PID or decay electron
  - Recoil nucleon
    - Usually below Cherenkov threshold
  - Recoil nucleus
    - Effectively invisible



Main background comes from  $\text{CC}|\pi^+$  with unobserved pion

# Axial Form Factor

- Recall CCQE cross section written in Llewellyn Smith formalism:

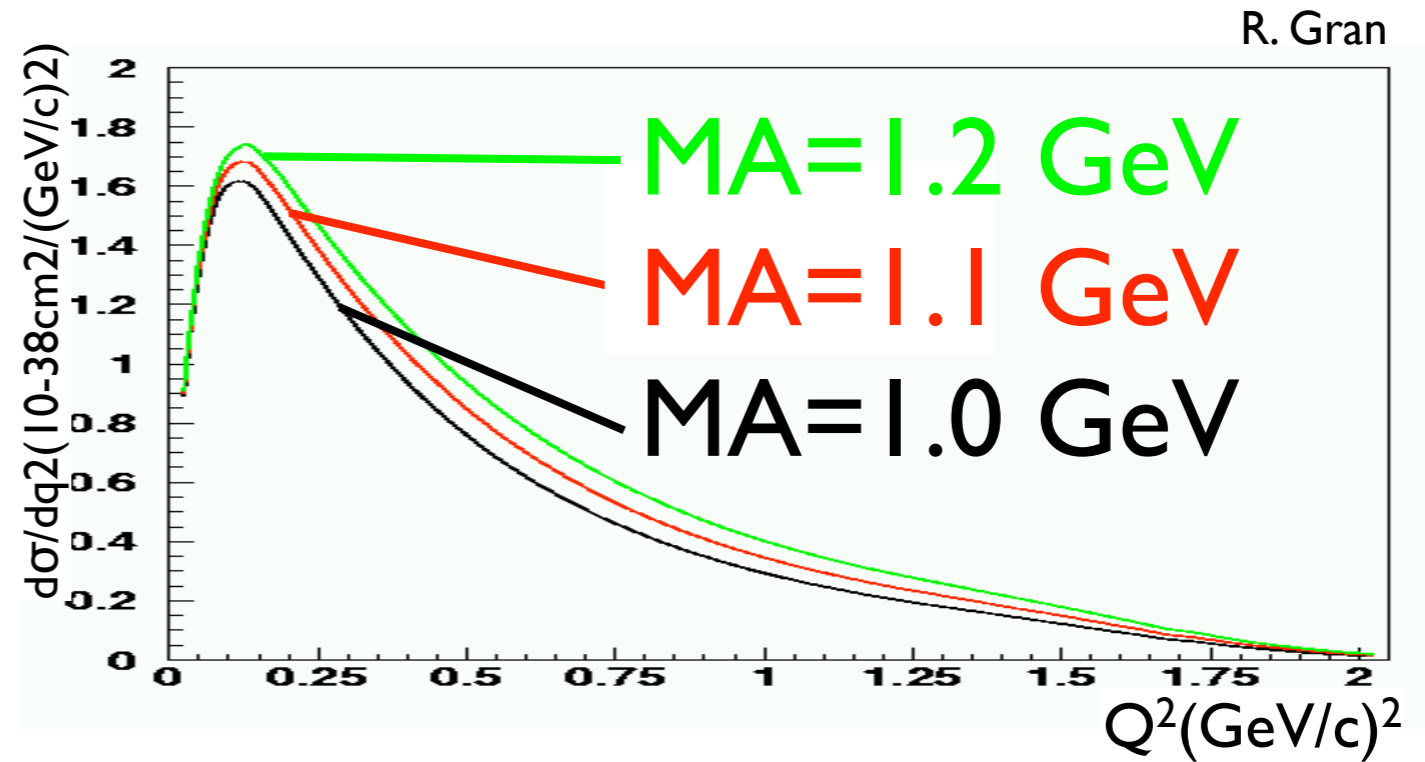
$$\langle N' | J_\mu | N \rangle = \bar{u}(N') \left[ \gamma_\mu F_V'(q^2) + \frac{i\sigma_{\mu\nu} q^\nu \xi F_V^2(q^2)}{2M} + \gamma_5 \gamma_\mu F_A(q^2) \right] u(N)$$

- Axial form factor usually parameterized as a dipole function:

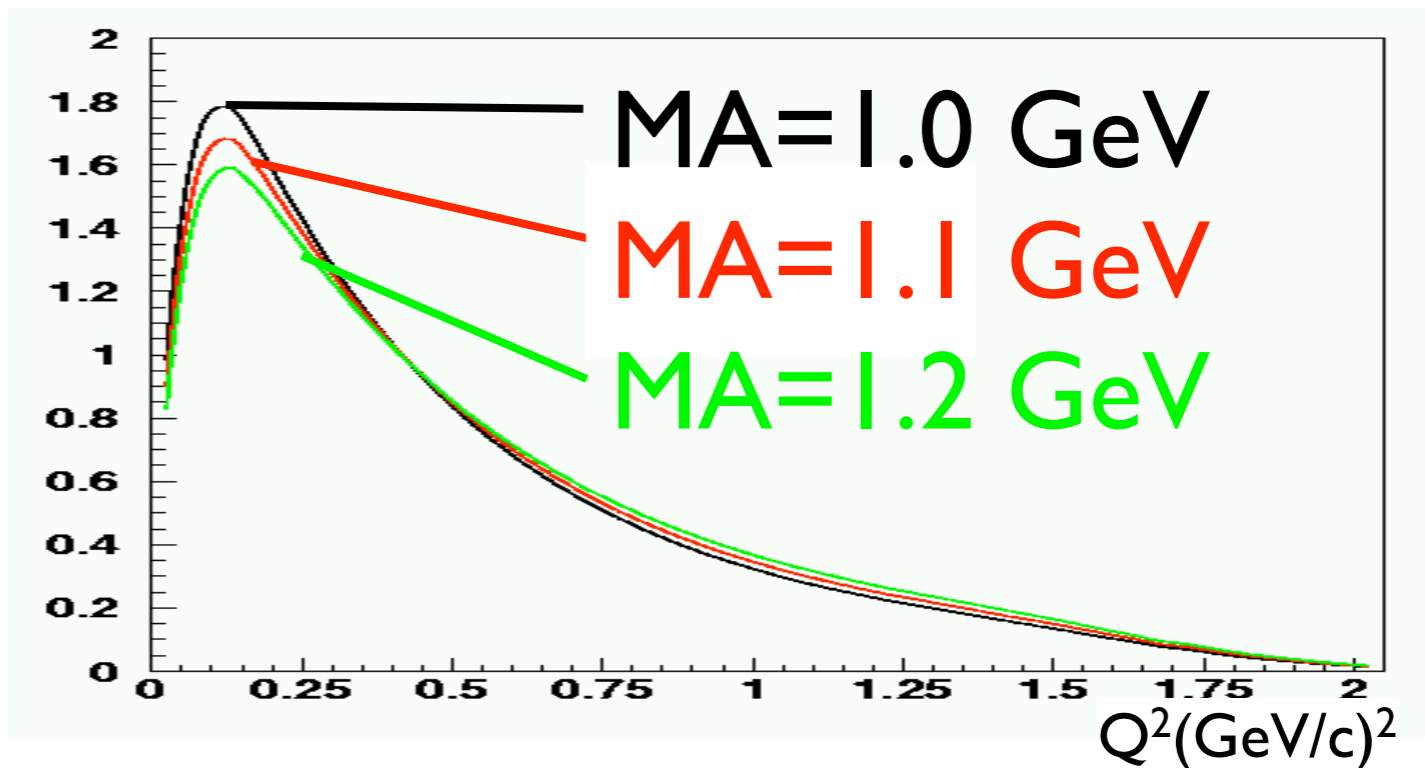
$$F_A(Q^2) = \frac{g_A}{(1 + Q^2/M_A^2)^2}$$

# Importance of $M_A$

Absolute  
Cross-section  
(includes  
normalization)



Shape only





# Basic Data Reduction

Timing and fiducial volume cuts

Number of muons

Number of tracks

Particle identification

Energy deposit  
around the vertex

Raw Data Sample



Neutrino Data Sample



Charged, Neutral Current



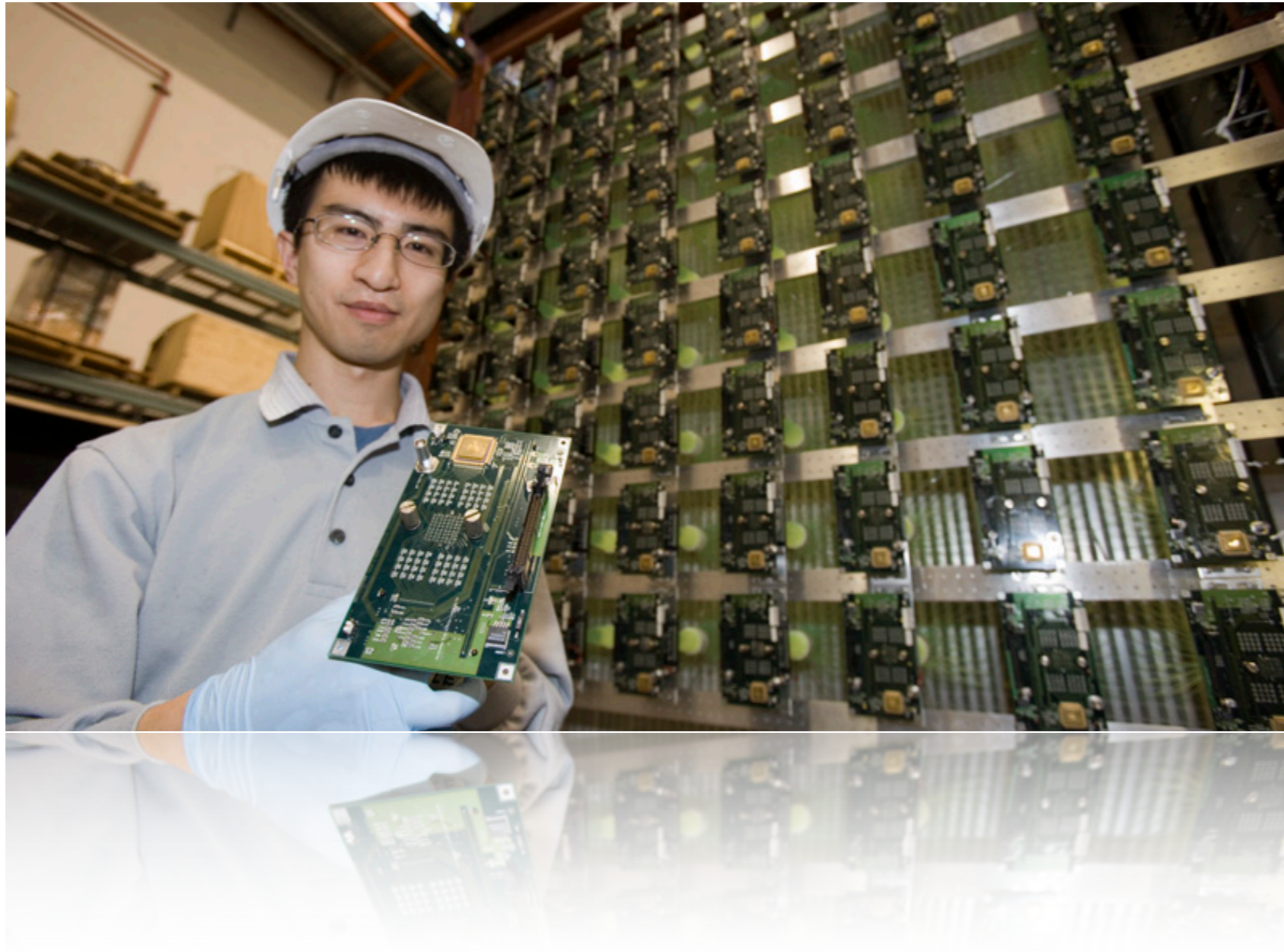
1,2, multi tracks



MIP, shower, proton



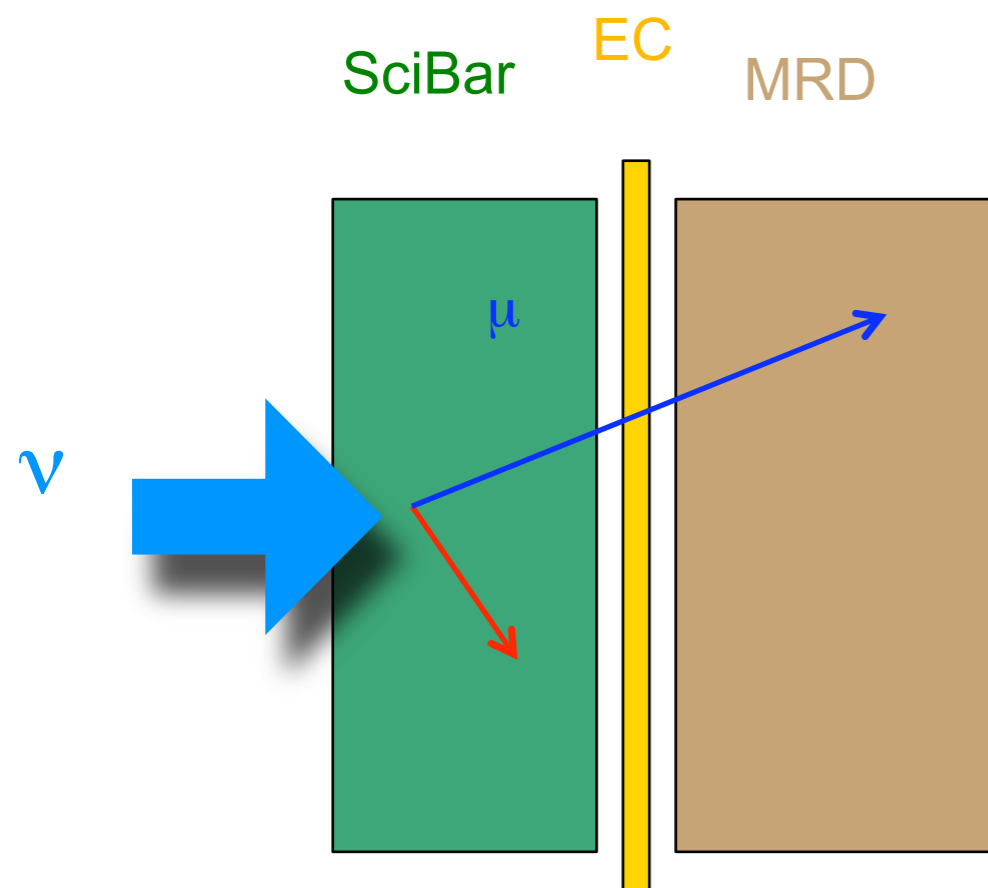
untracked particles?



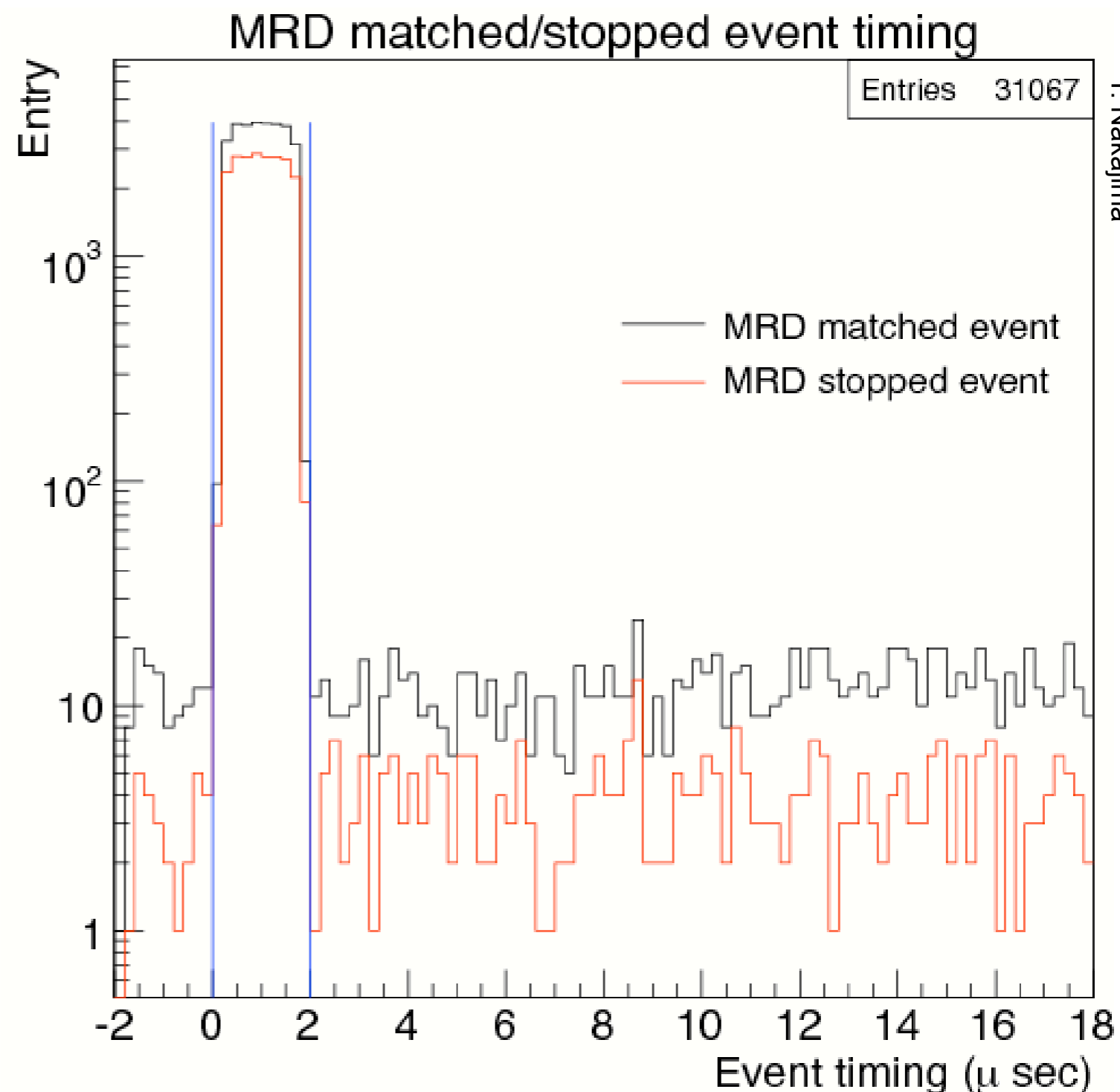
**SciBooNE CCQE**

# CC Inclusive

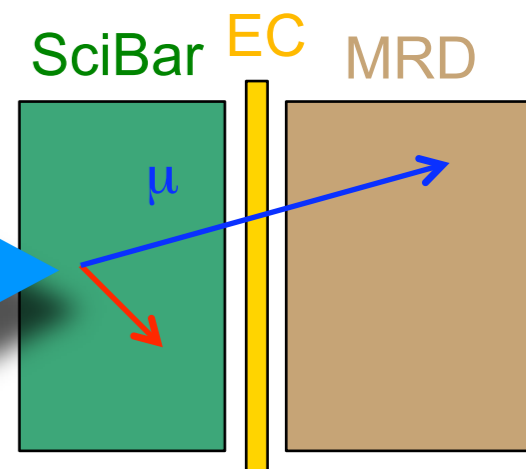
- $\mu$ 's easily identified if penetrate MRD
- 96% pure CC
- 21,431 stopped  $\nu$  events



- *Normalisation set by*
- *MRD-matched events*

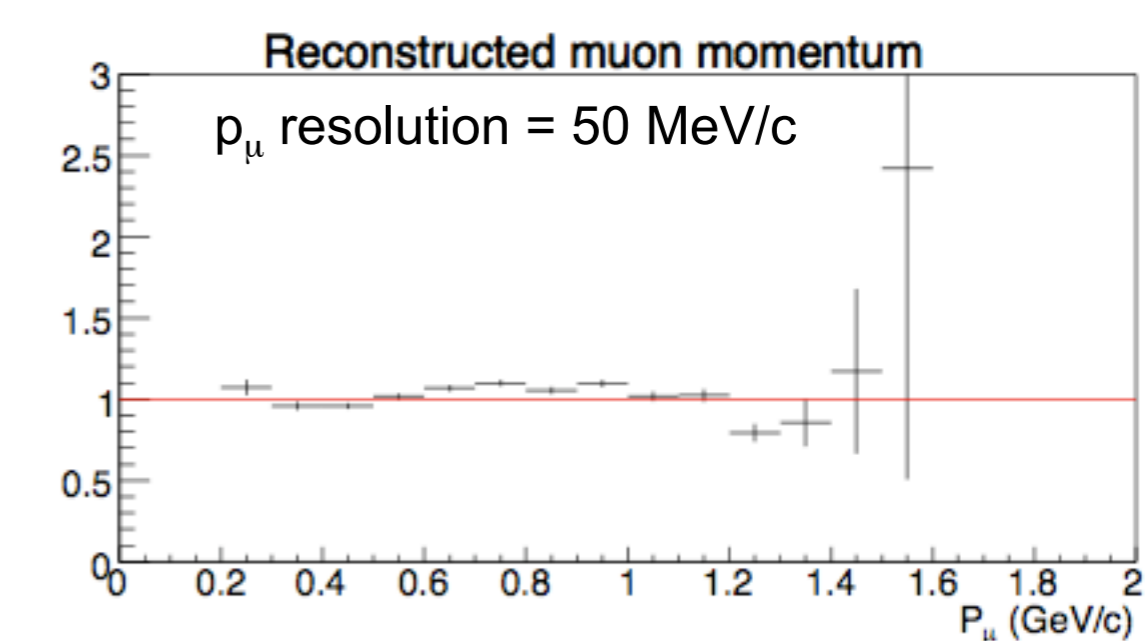
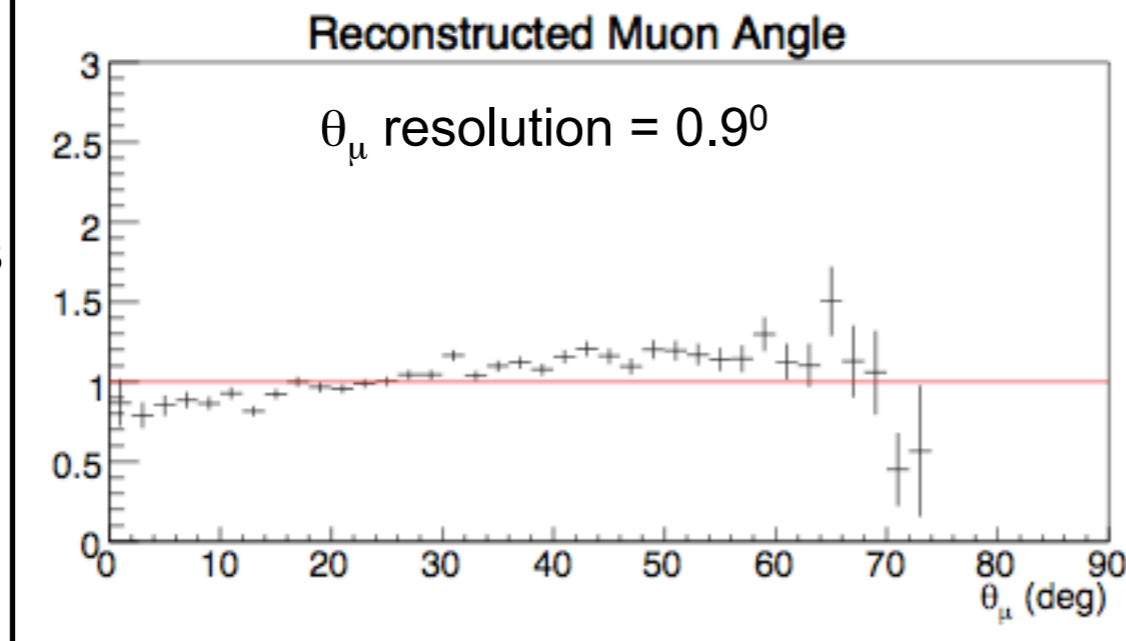
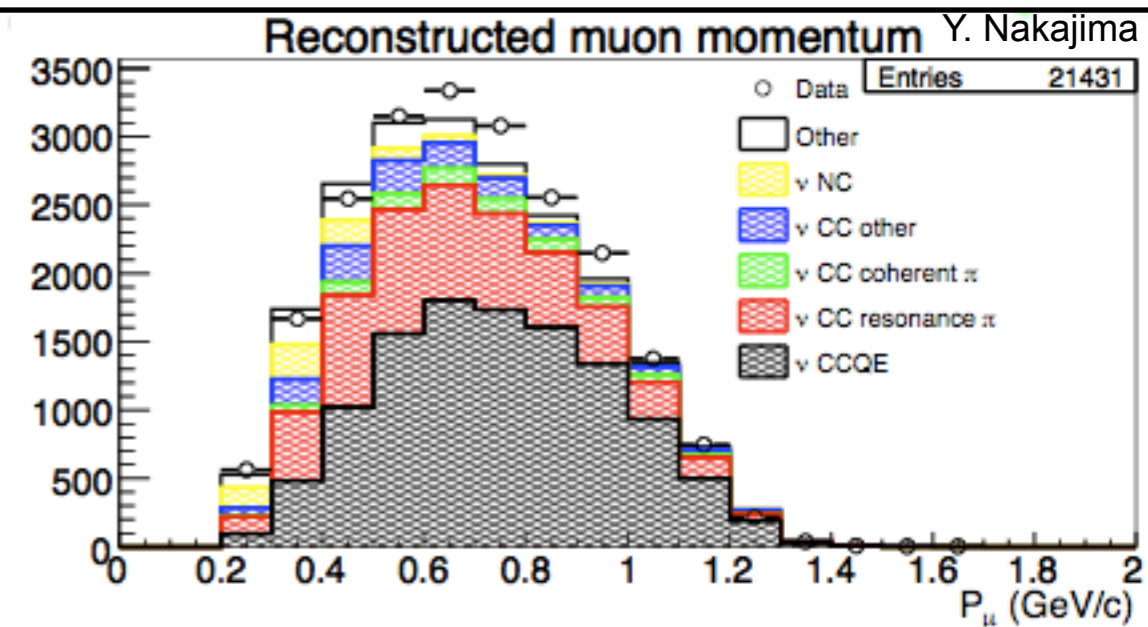
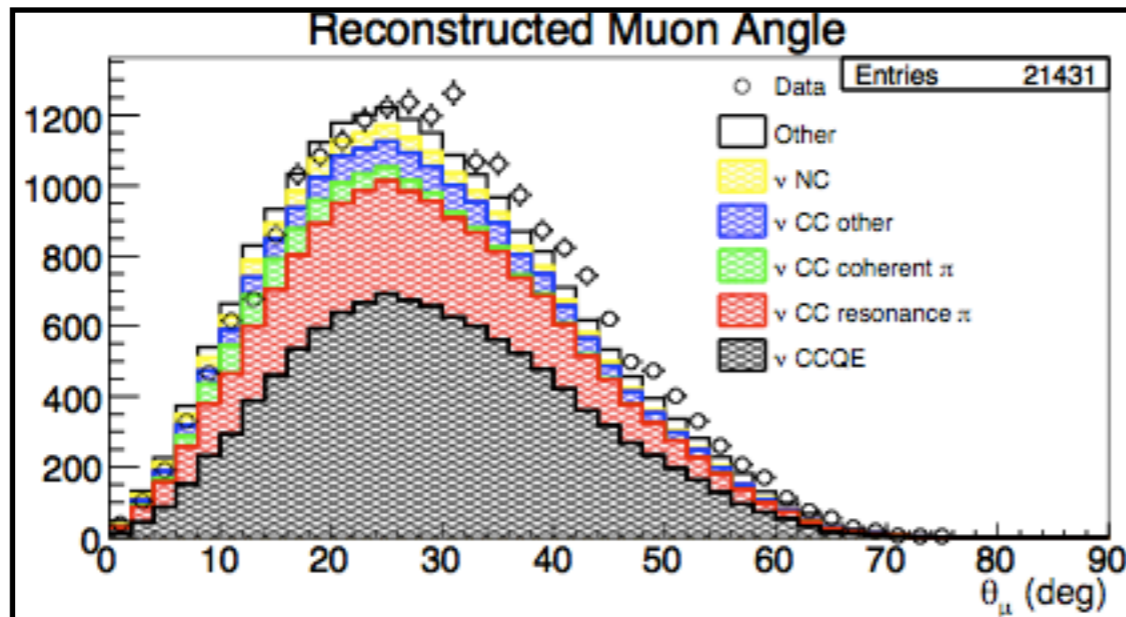


# CC Inclusive



MRD stopped events

Normalised  
to MRD  
matched  
events



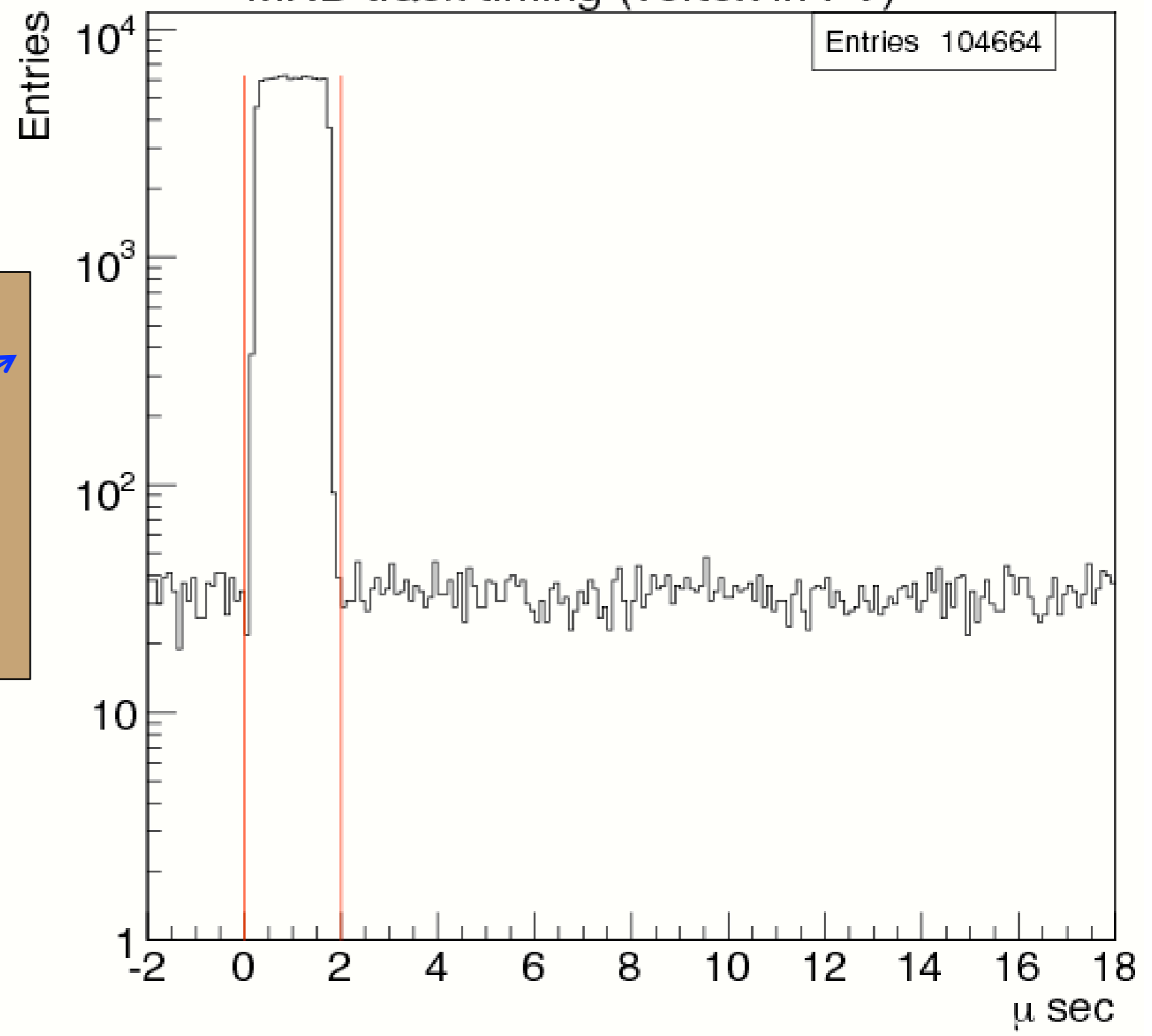
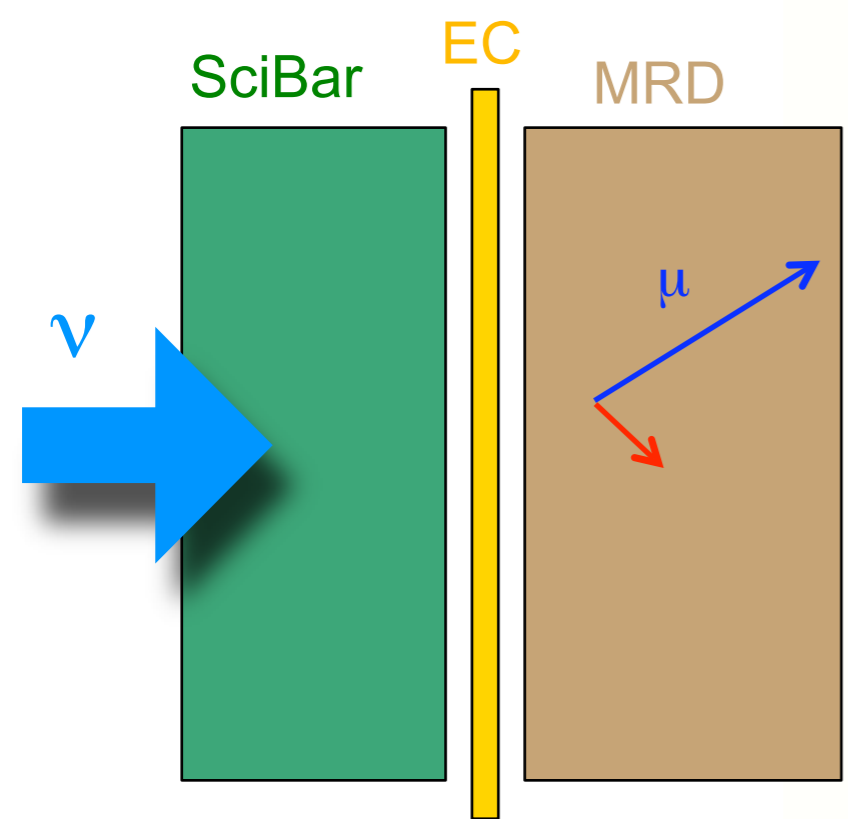
Angular  
discrepancy is  
not detector  
effect  
→ physics?



# CC Inclusive - Fe

Y. Nakajima

MRD track timing (vertex in FV)



# CC event classification

Define MC  
normalization

SciBar-MRD matched sample

MRD-stopped

Number of tracks

1 track

2 track

>2 track

Particle identification

$\mu+p$

$\mu+\pi$

Energy deposit  
around the vertex

w/ activity

w/o activity

MRD-stopped  
CC analysis  
samples





# CC event classification

Define MC  
normalization

SciBar-MRD matched sample

MRD-stopped

MRD-penetrated

Number of tracks

1 track

2 track

>2 track

Particle identification

$\mu+p$

$\mu+\pi$

Energy deposit  
around the vertex

w/ activity

w/o activity

Same selection

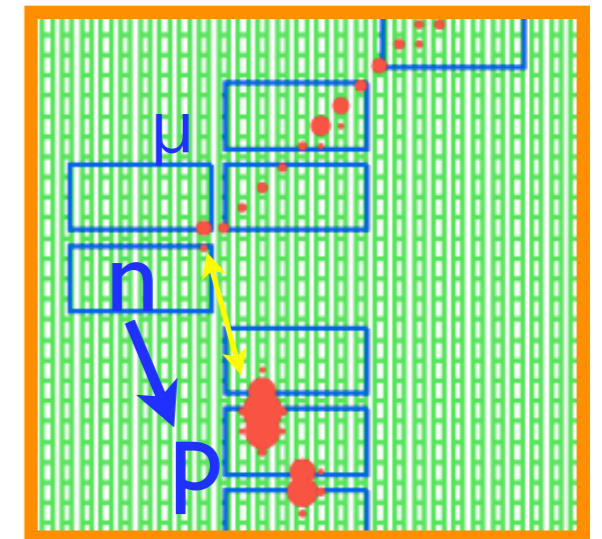
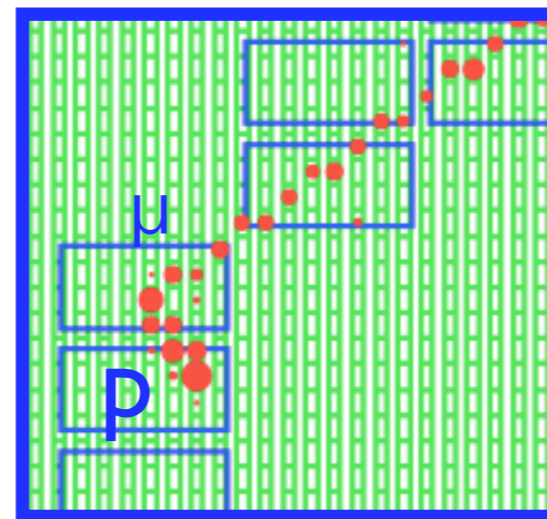
MRD-stopped  
CC analysis  
samples

MRD-penetrated  
CC analysis  
sample

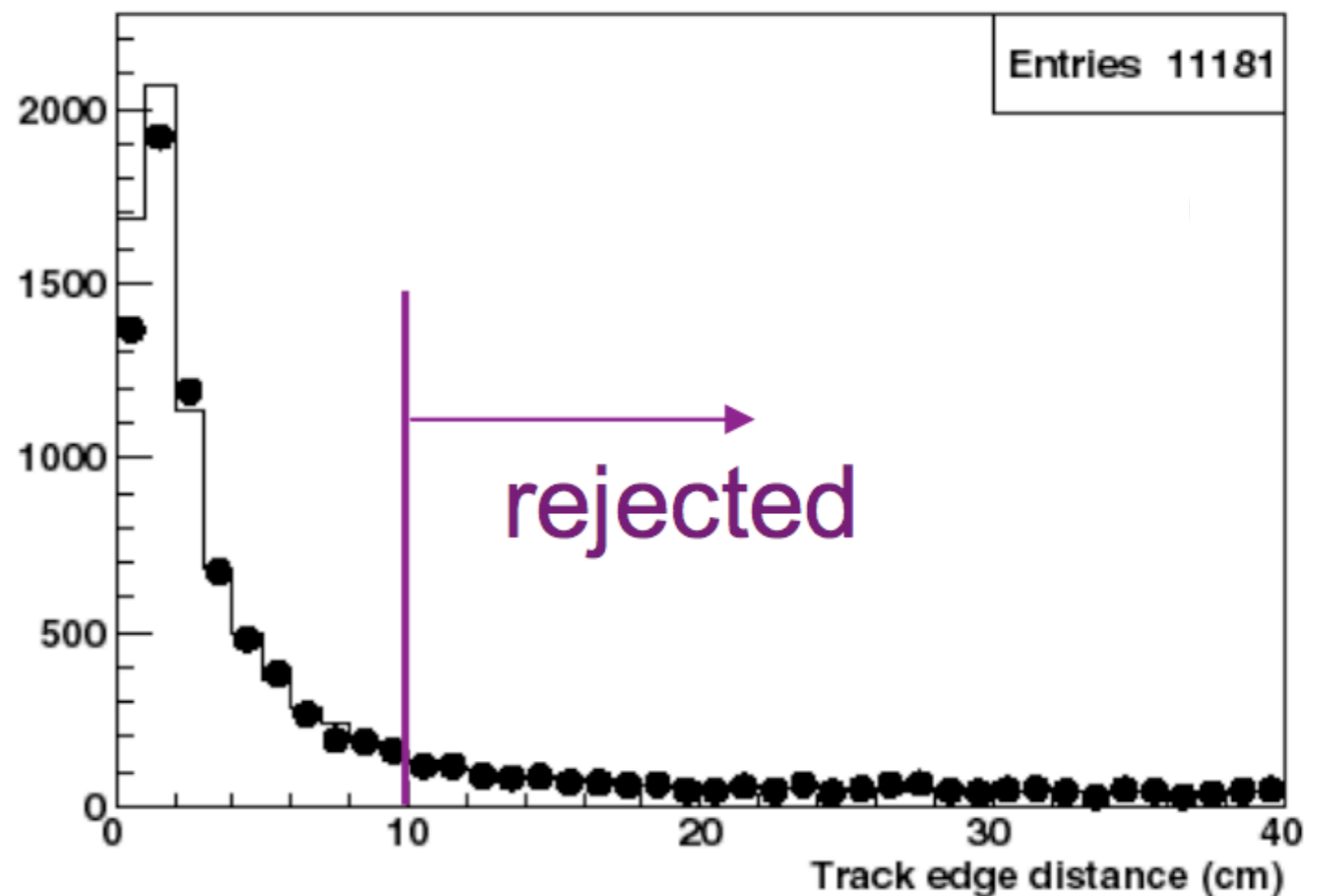


# SciBar Cuts

- Additional track parameters used to distinguish interaction signatures
  - Vertex separation
  - 2nd track angle
    - $\Delta\theta_p$

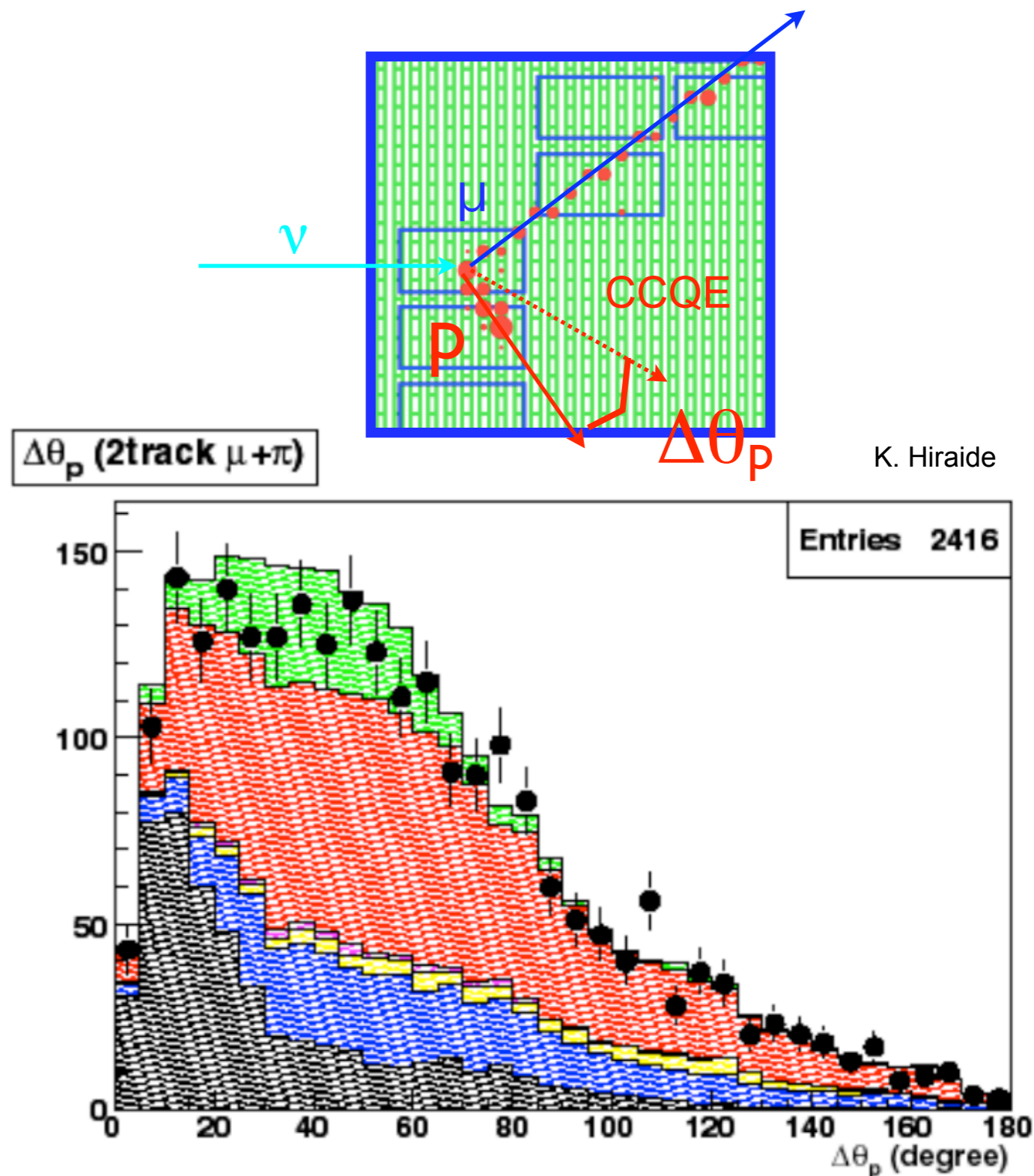


Track edge distance



# SciBar Cuts

- Additional track parameters used to distinguish interaction signatures
  - Vertex separation
  - 2nd track angle
    - $\Delta\theta_p$

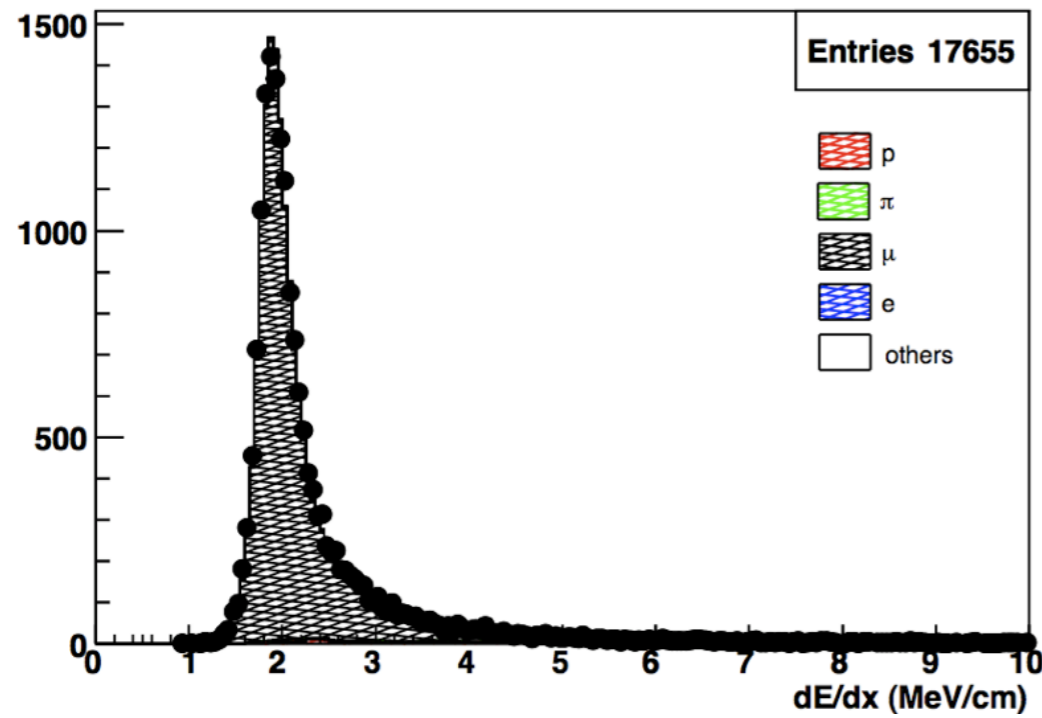


K. Hiraide

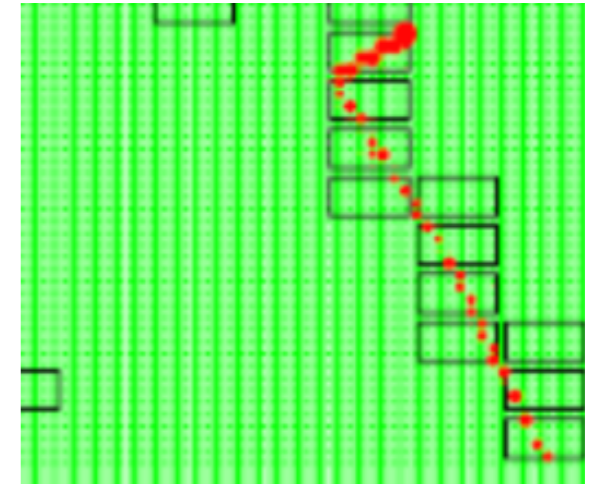
# SciBar PID

dE/dx (muon track sample)

K. Hiraide

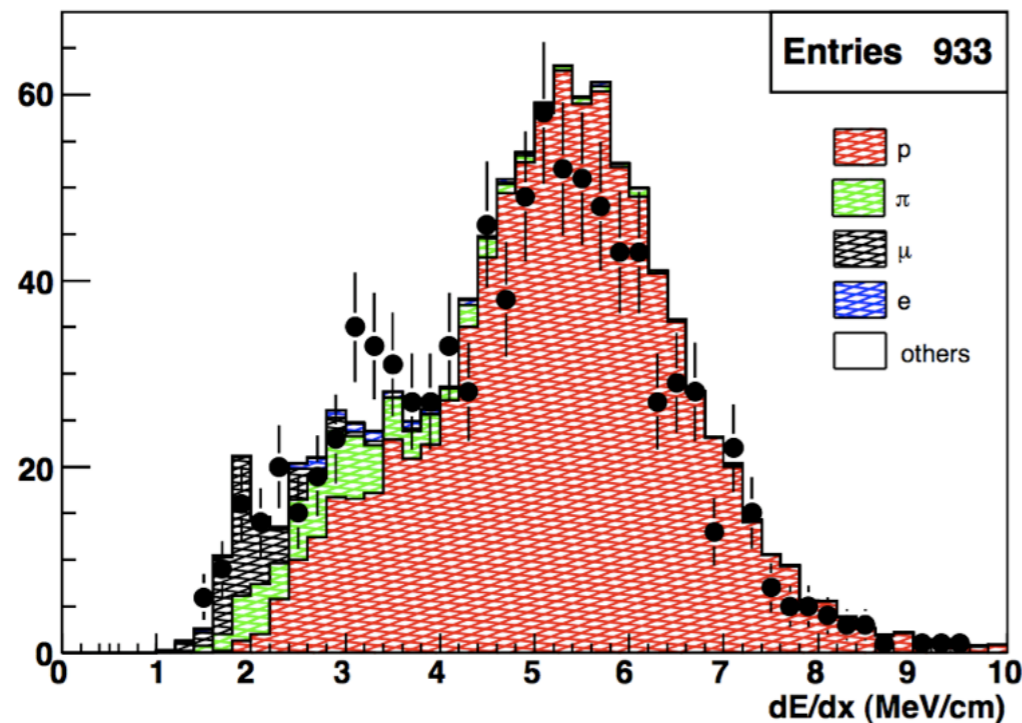


Energy deposit  
used as PID



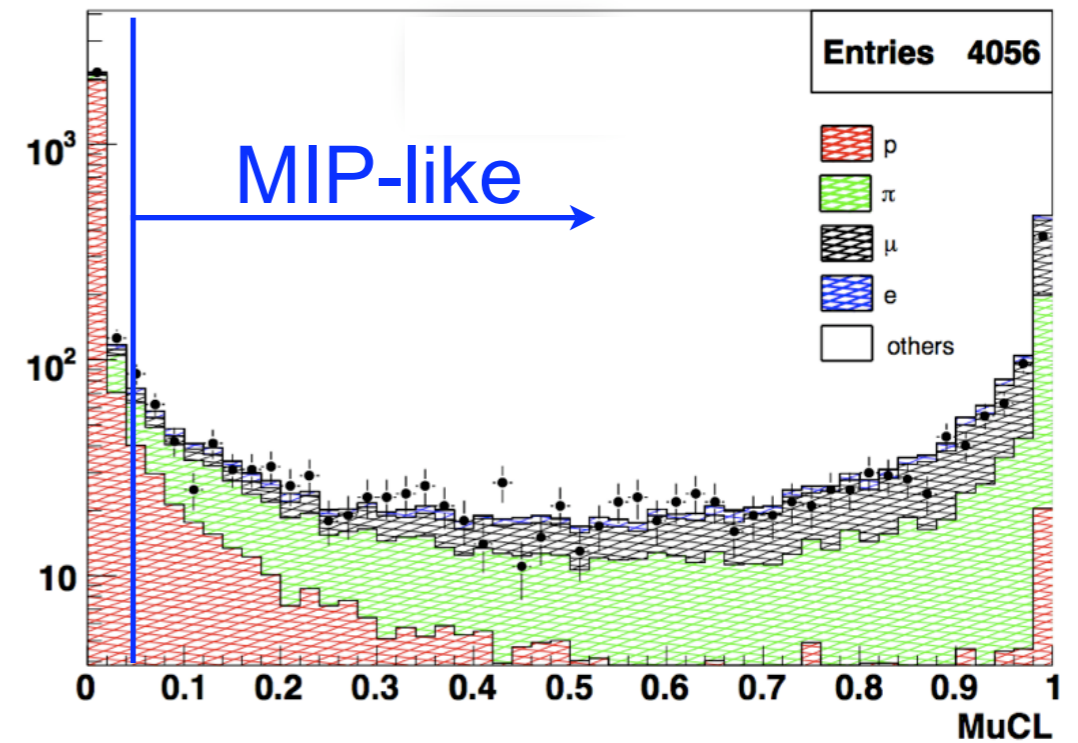
dE/dx (proton track sample)

K. Hiraide



MuCL (2-track sample)

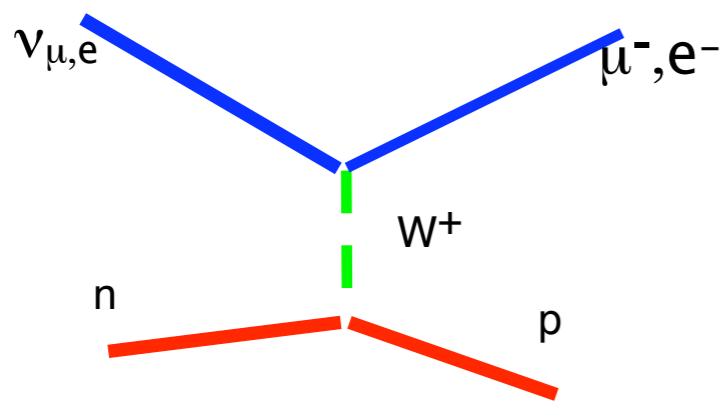
K. Hiraide



Cut at  $\text{MuCL} > 0.05$  for 2<sup>nd</sup> tracks:  
84%  $\pi^+$  efficiency  
~90% p rejection



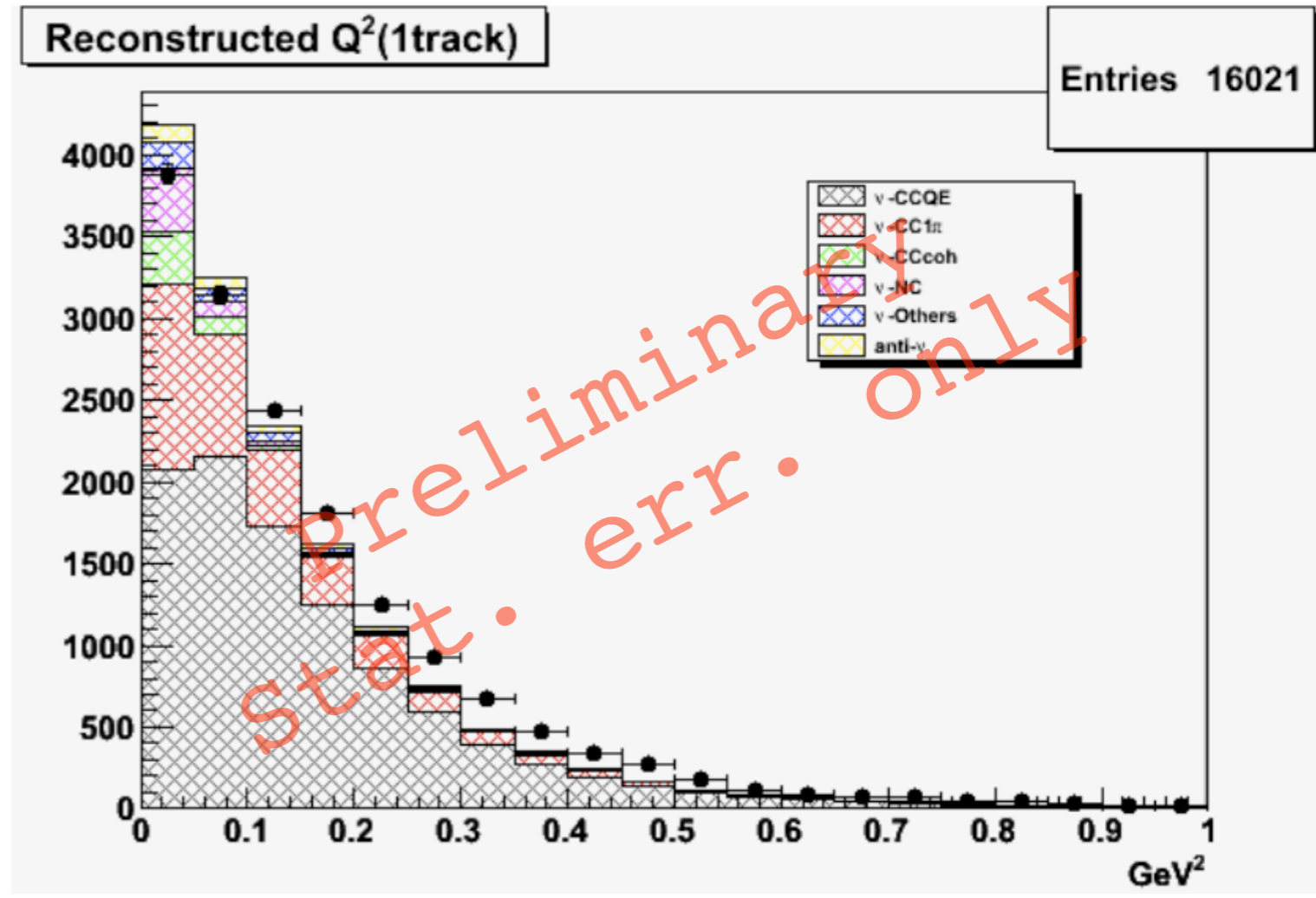
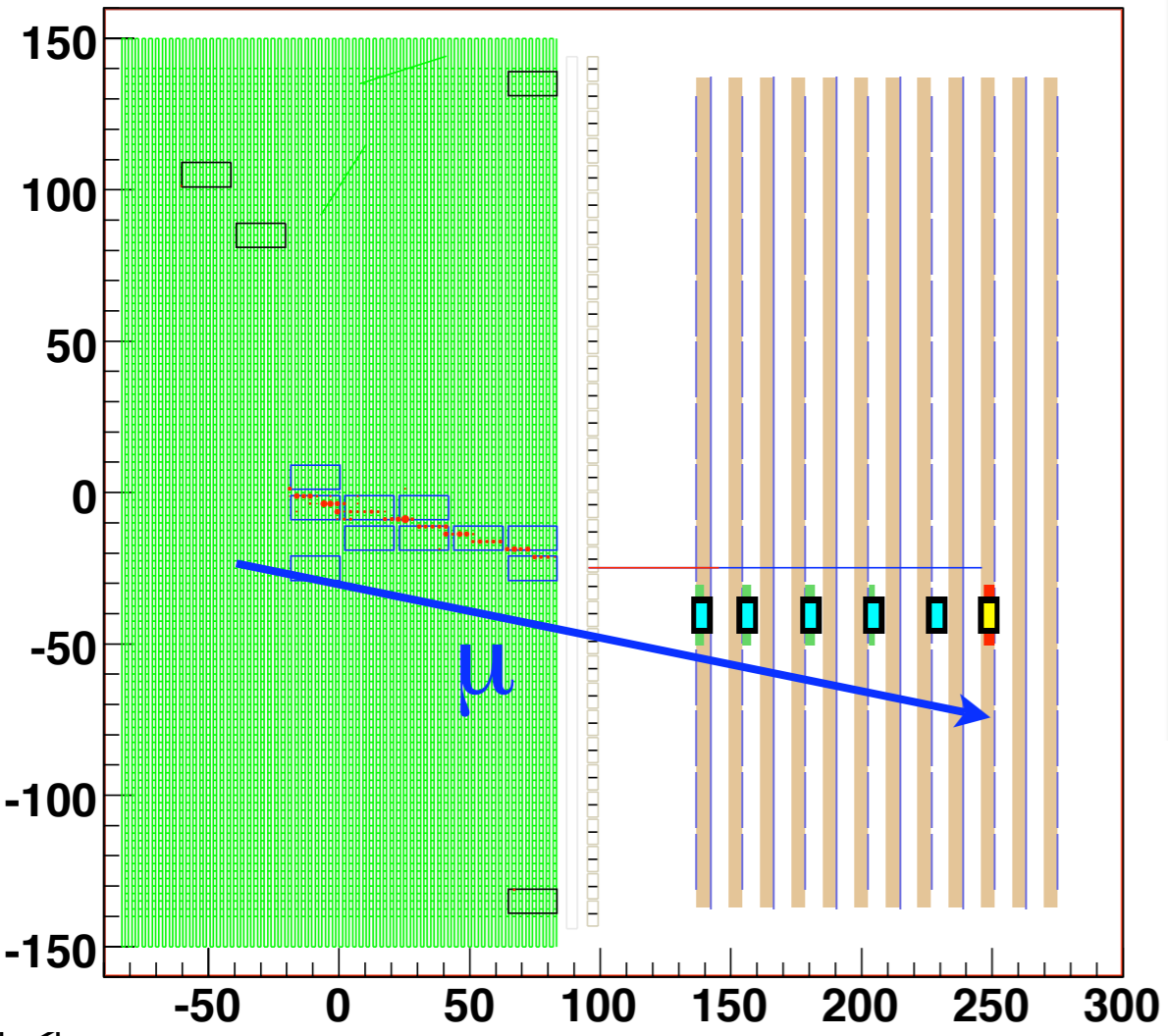
# CCQE - 1 track



$$Q_{rec}^2 = 2E_{\nu}^{rec} (E_{\mu} - p_{\mu} \cos\theta_{\mu}) - m_{\mu}^2$$

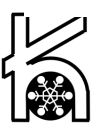
J. Alcaraz-Aunión

SciBooNE data

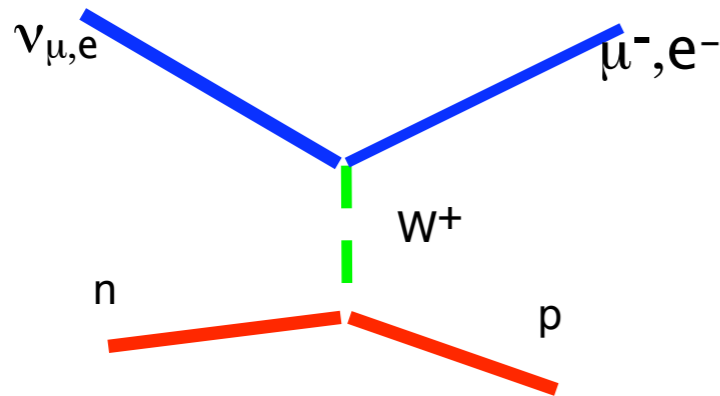


1 track events 67% pure  
CCQE

using NEUT ( $M_A=1.1$  GeV)



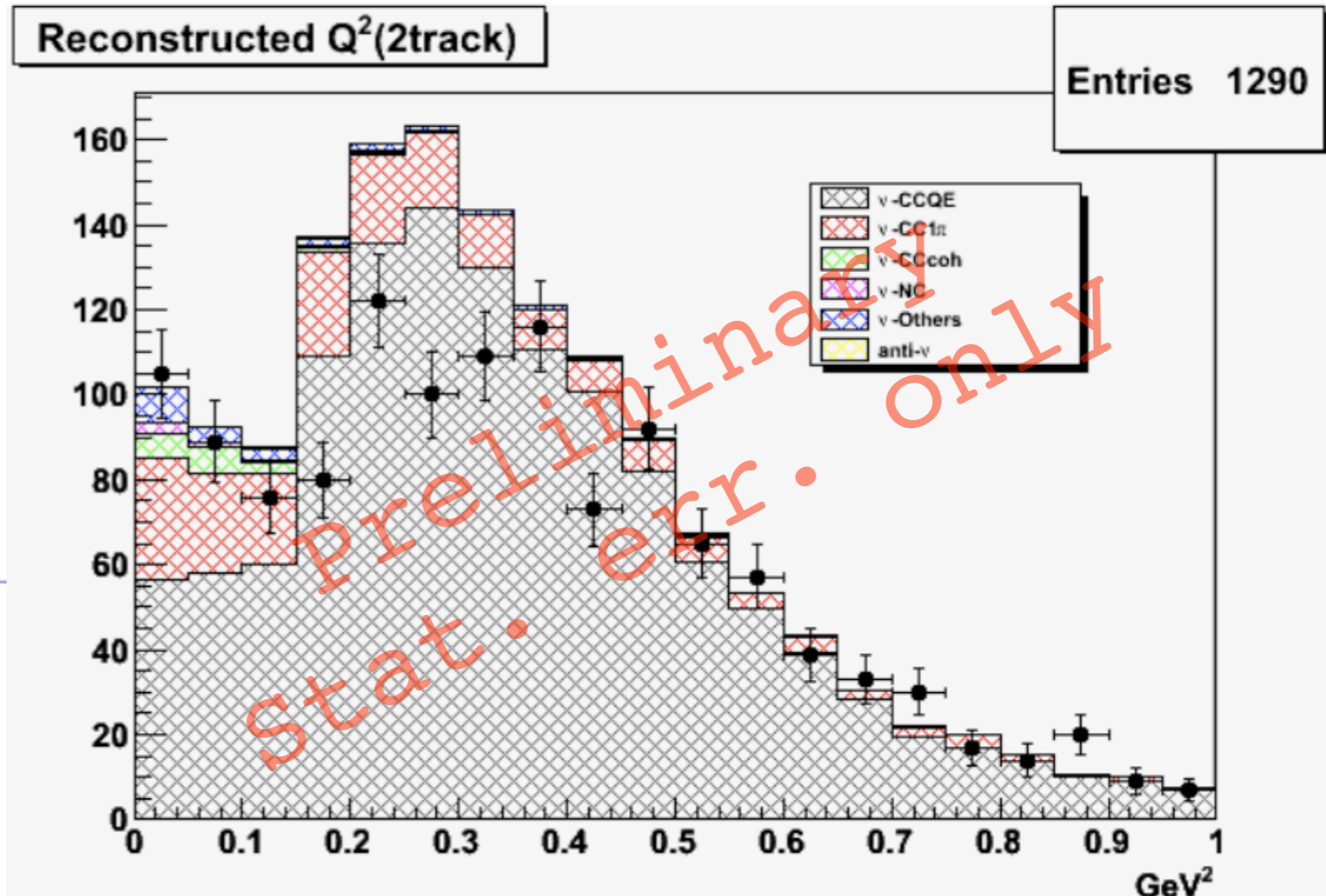
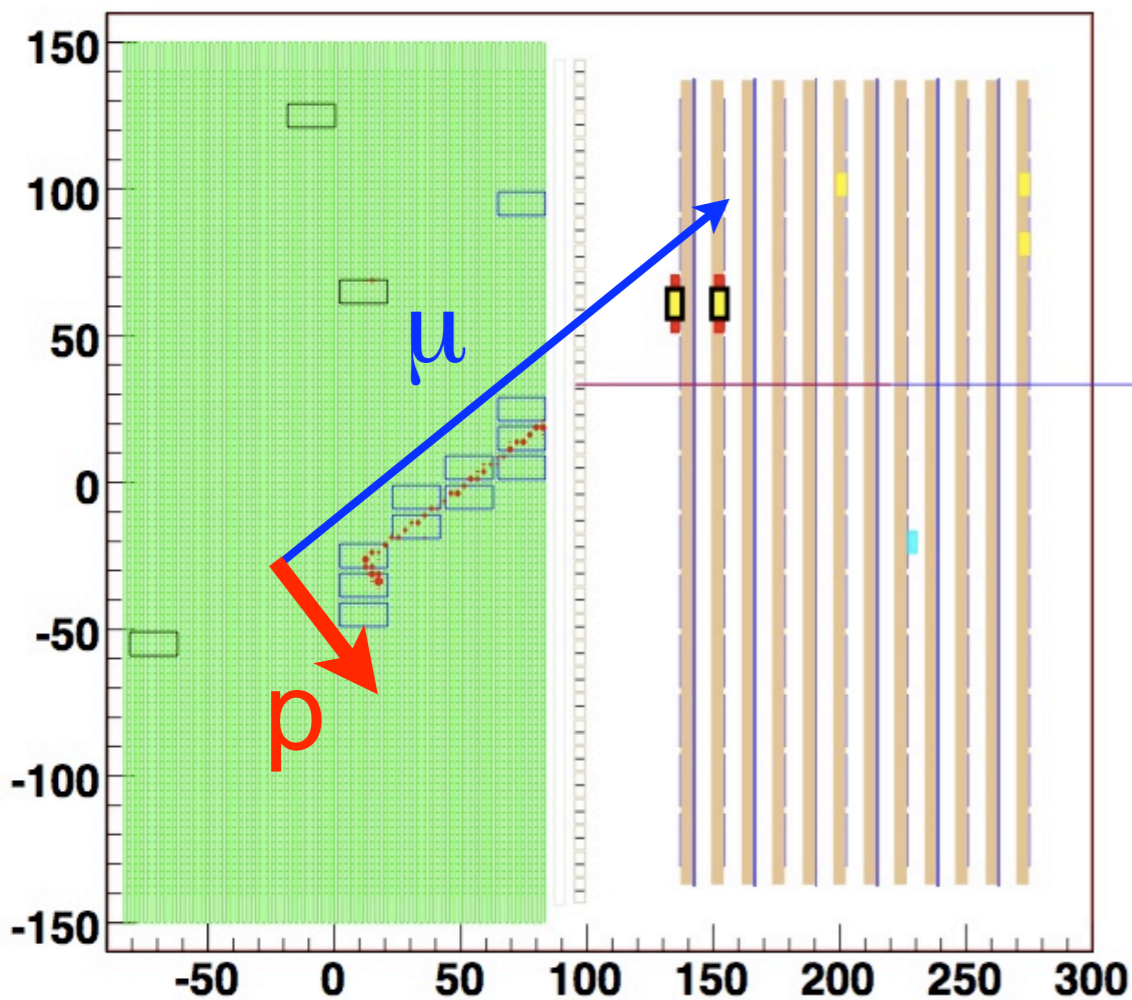
# CCQE - 2 track



$$Q_{rec}^2 = 2E_{\nu}^{rec} (E_{\mu} - p_{\mu} \cos\theta_{\mu}) - m_{\mu}^2$$

J. Alcaraz-Aunión

SciBooNE data



2 track events 81% pure CCQE  
( $\mu$  + proton using PID)

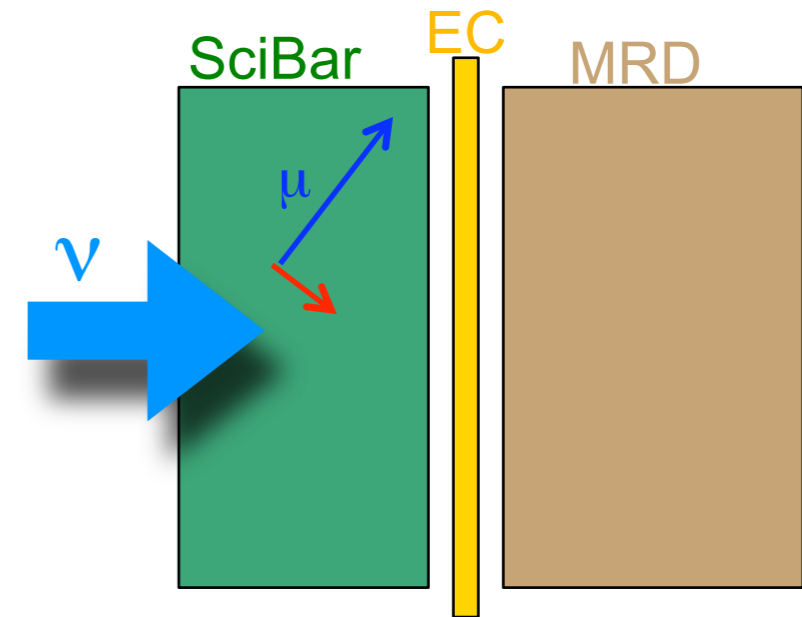
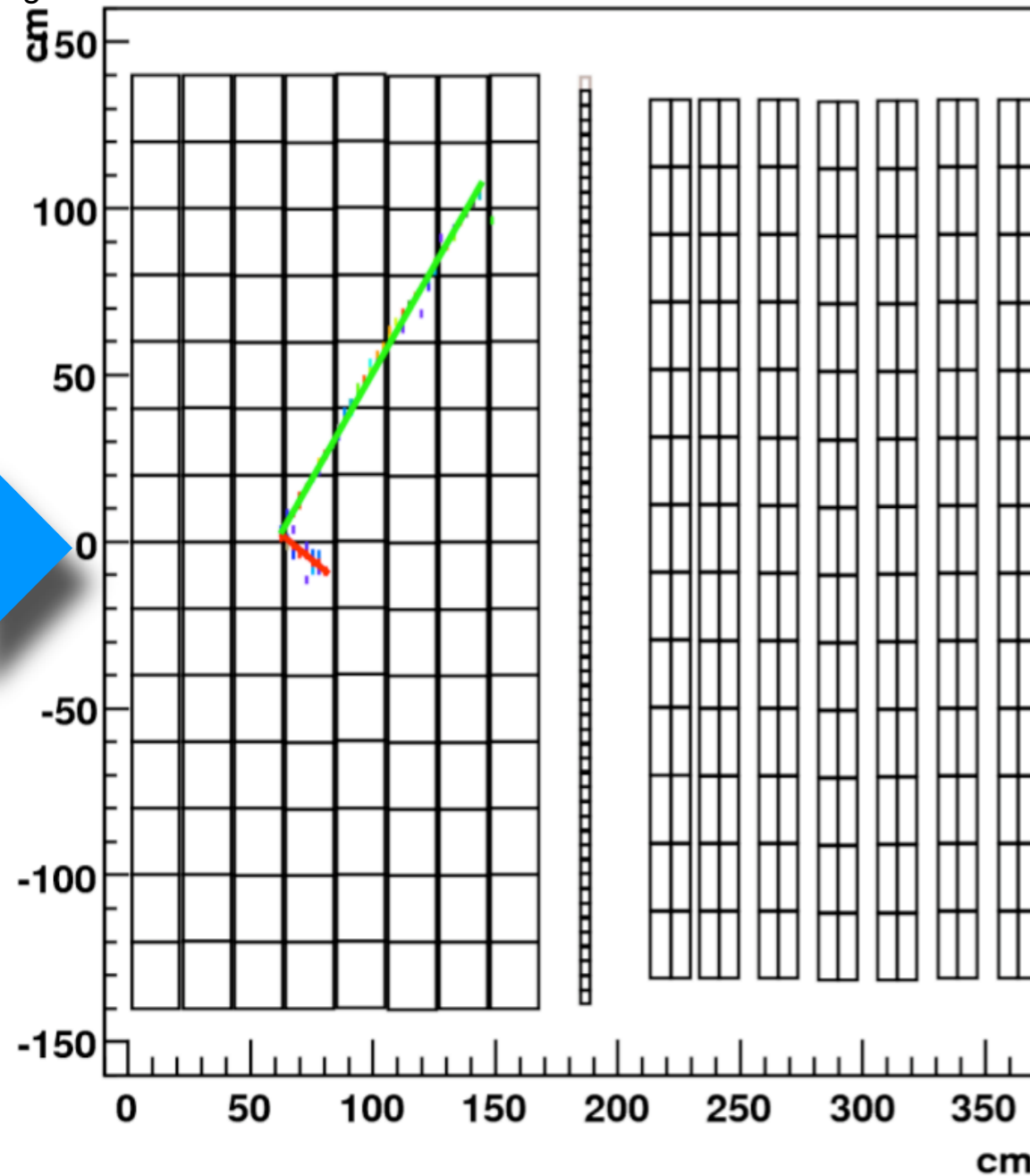
using NEUT ( $M_A=1.1$  GeV)





# CCQE - SciBar only

J. Walding



- Events can remain in SciBar only
- Look for muon decay to tag the muon tracks

*Different kinematic regions*

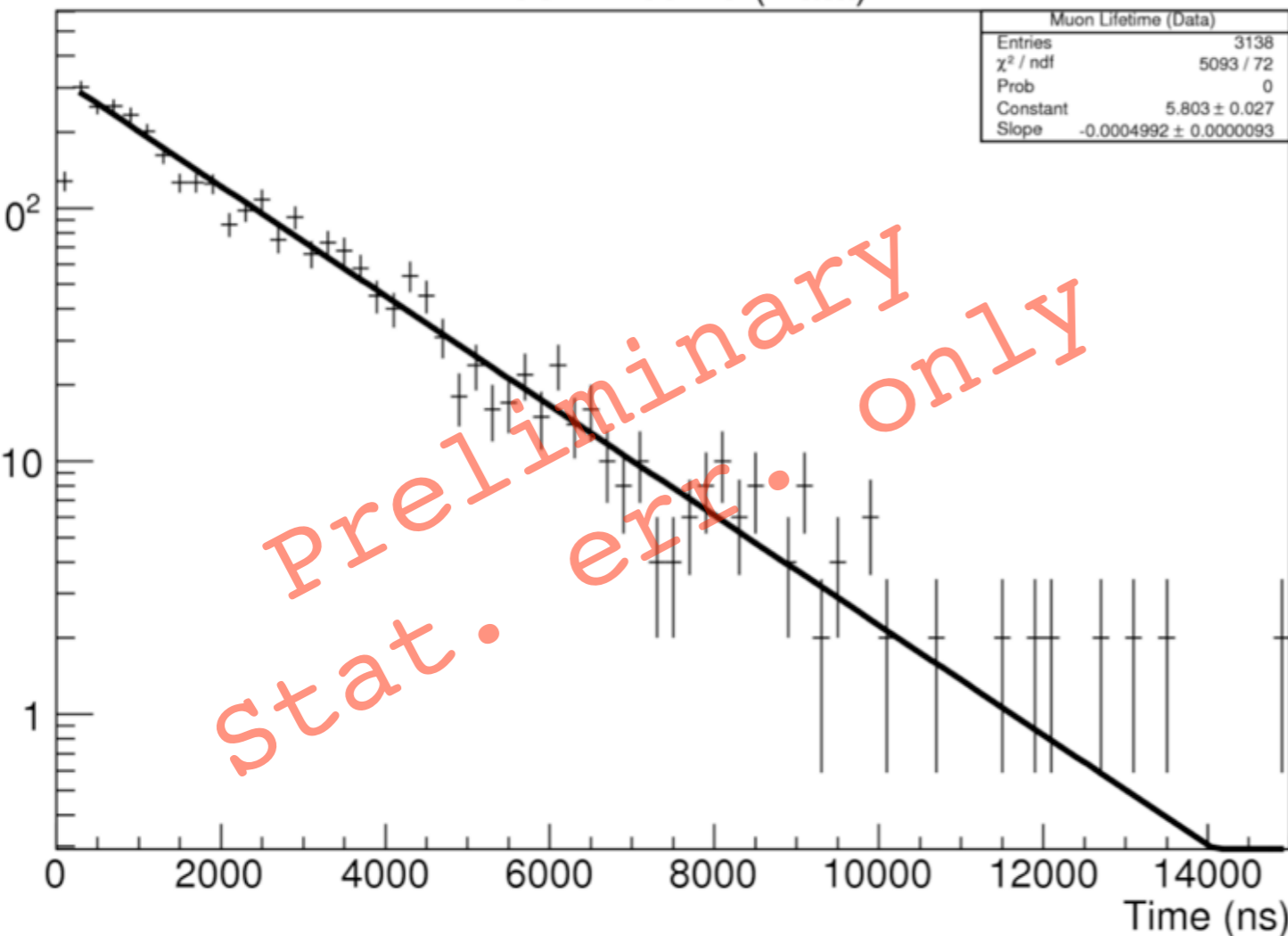
*Different systematics on  $p_\mu$  measurement*

# CCQE - SciBar only

J. Walding

Tue May 20 01:50:26 2008

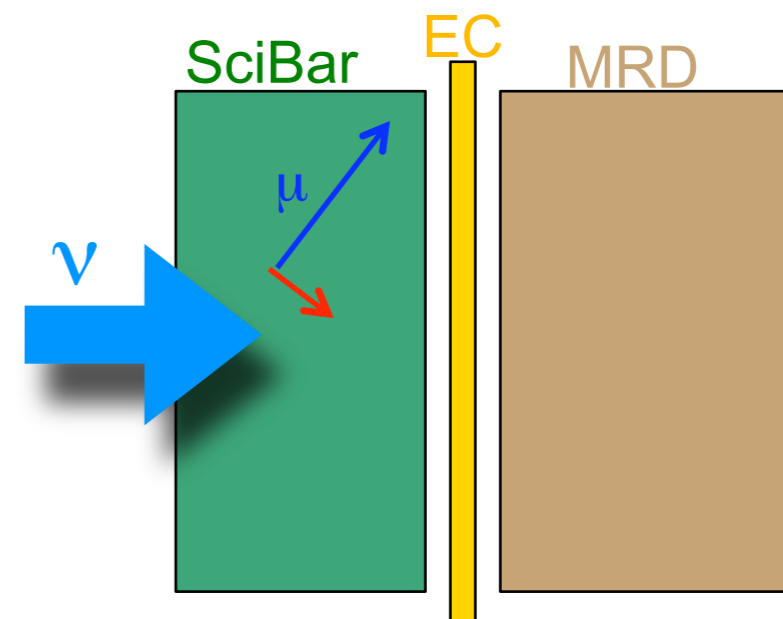
Muon Lifetime (Data)



$$\tau_{\mu} = 2.003 \pm 0.047 \text{ (stat)} \mu\text{s}$$

$$\text{expected} = 2.026 \pm 0.001 \mu\text{s}$$

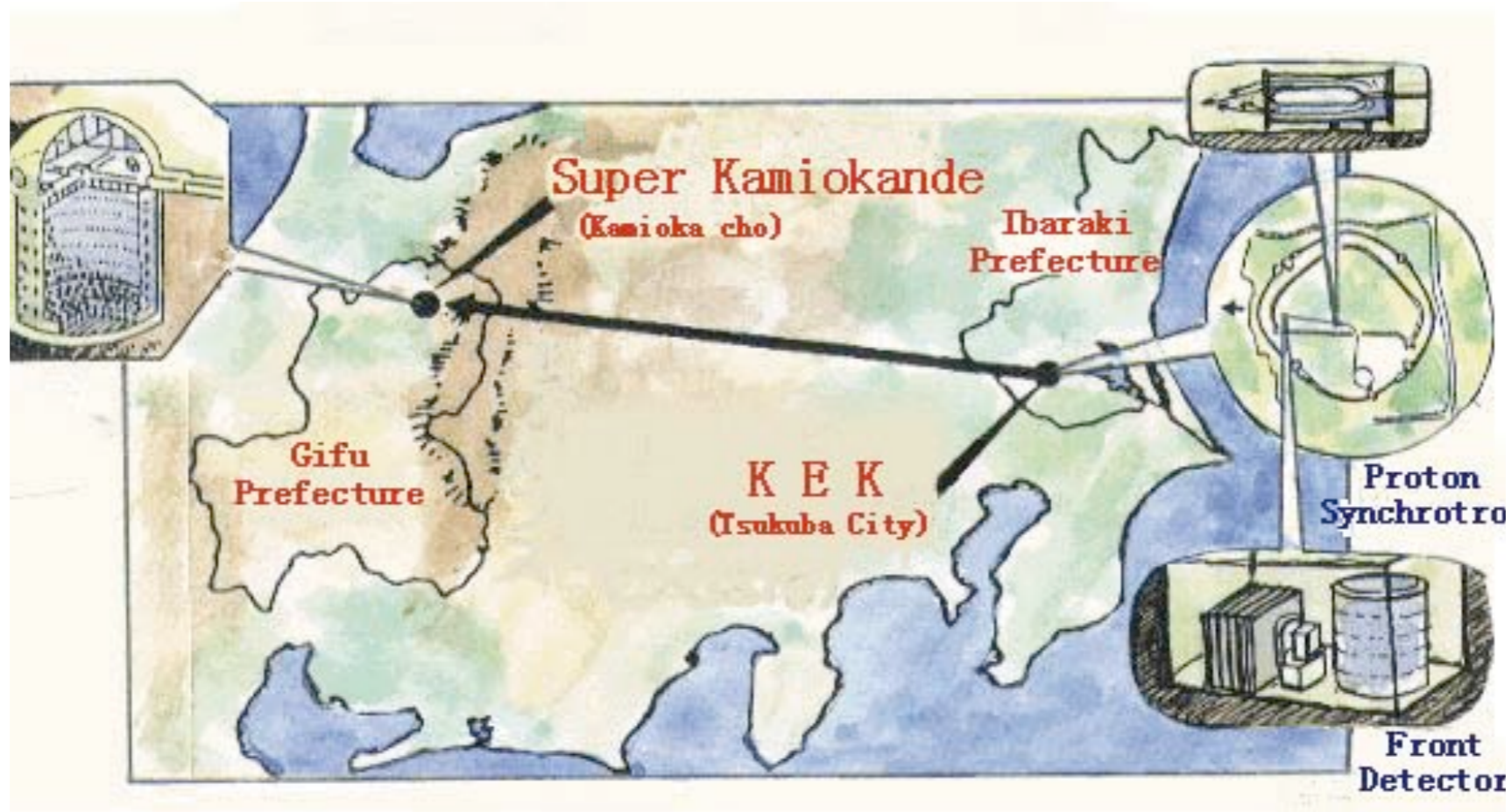
Suzuki, et al., PRC35, 2122 1987



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*Different kinematic regions*

*Different systematics on  $p_{\mu}$  measurement*

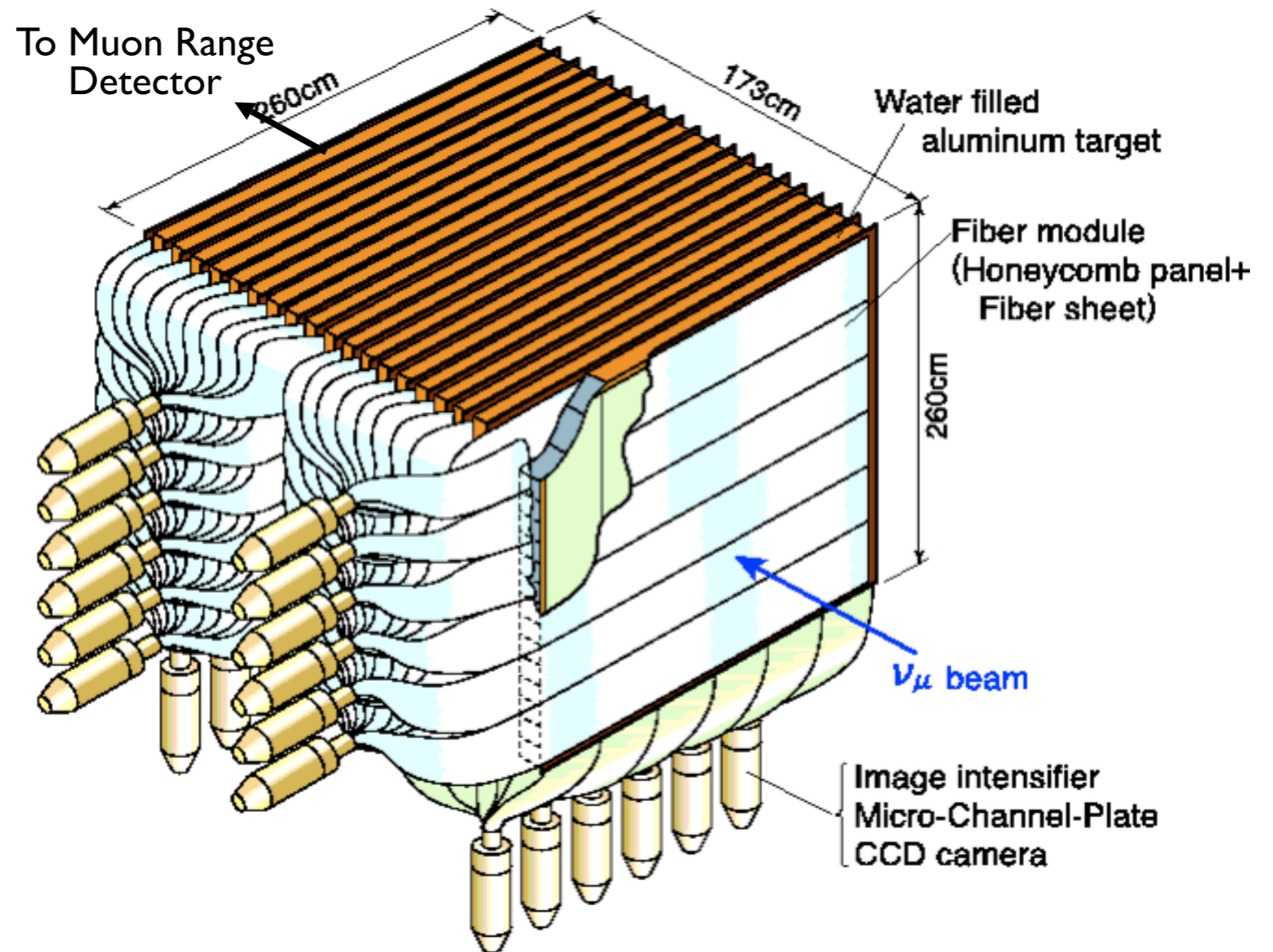


**K2K CCQE**

# SciFi CCQE

Muon in the Muon Range  
Detector must have  
 $p_{\text{muon}} > 600 \text{ MeV}/c$

Recoil proton threshold is  
three layers in SciFi  
 $p_{\text{proton}} > \sim 600 \text{ MeV}/c$

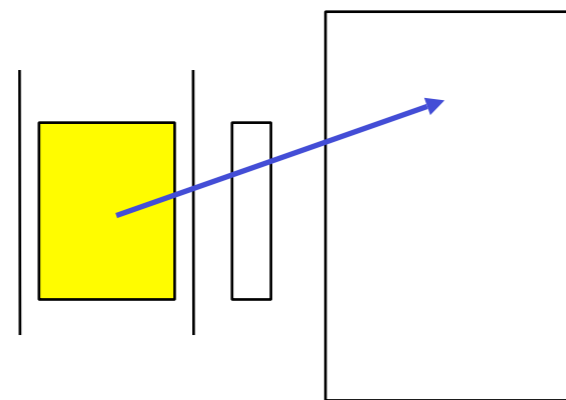
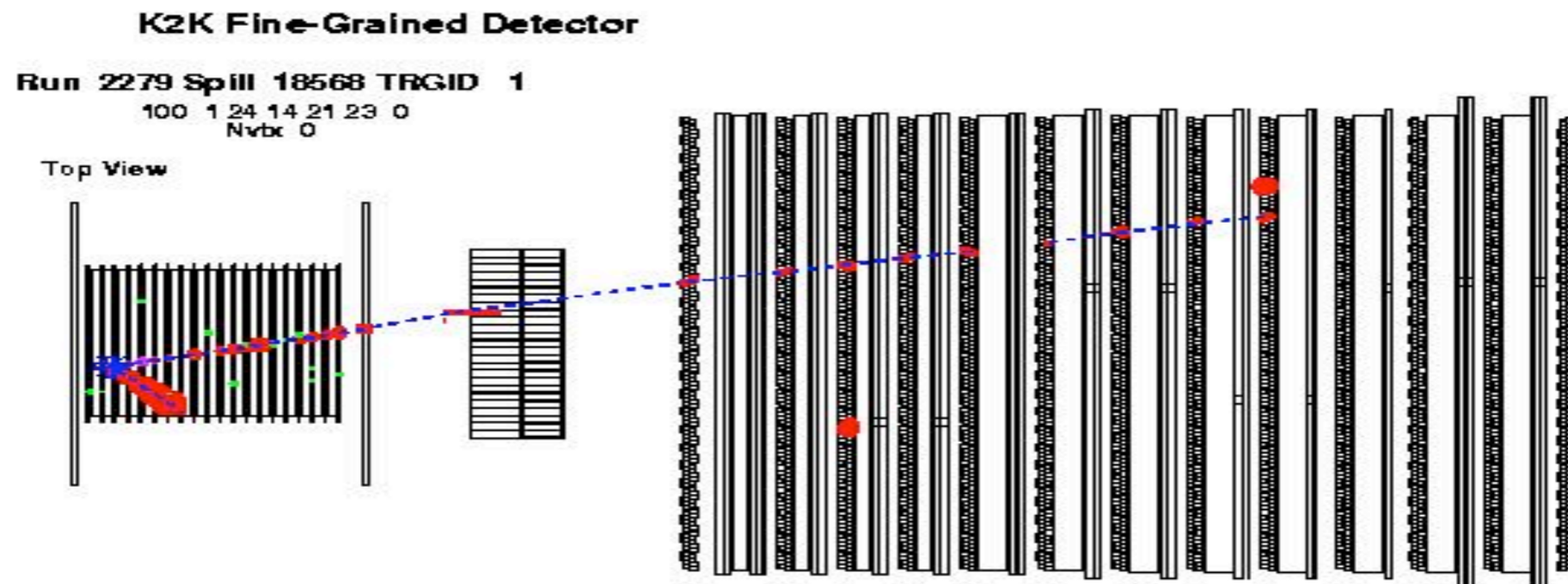


1-track events with muon only  
2-track events with muon plus either proton or pion

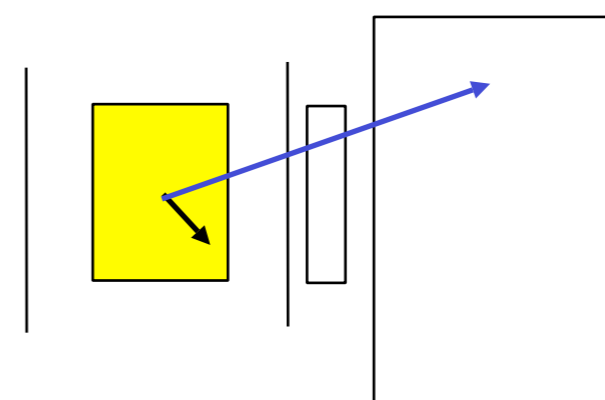


# Event Selection

Typical two-track event showing the muon and second track



1 track event



2 track event

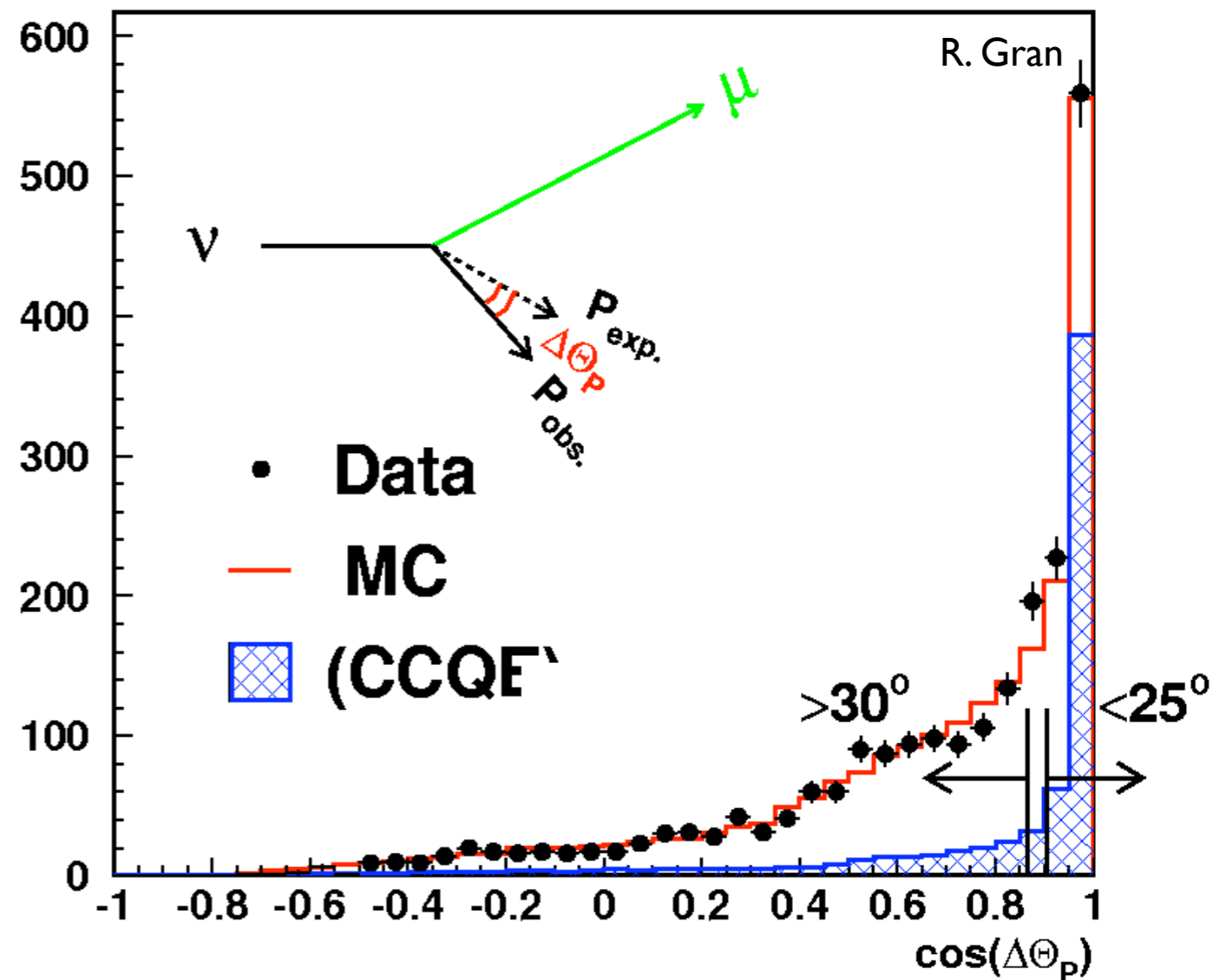
Neutrino interaction on  $\text{H}_2\text{O}$  target (+ 20% Aluminum)

# 2 track events

use the location of proton track  
to separate events  
into three subsamples:

1-track (no proton) 60% QE  
 2-track QE enhanced 60% QE  
 2-track nQE **85% nonQE**, 15% QE  
 (NEUT)

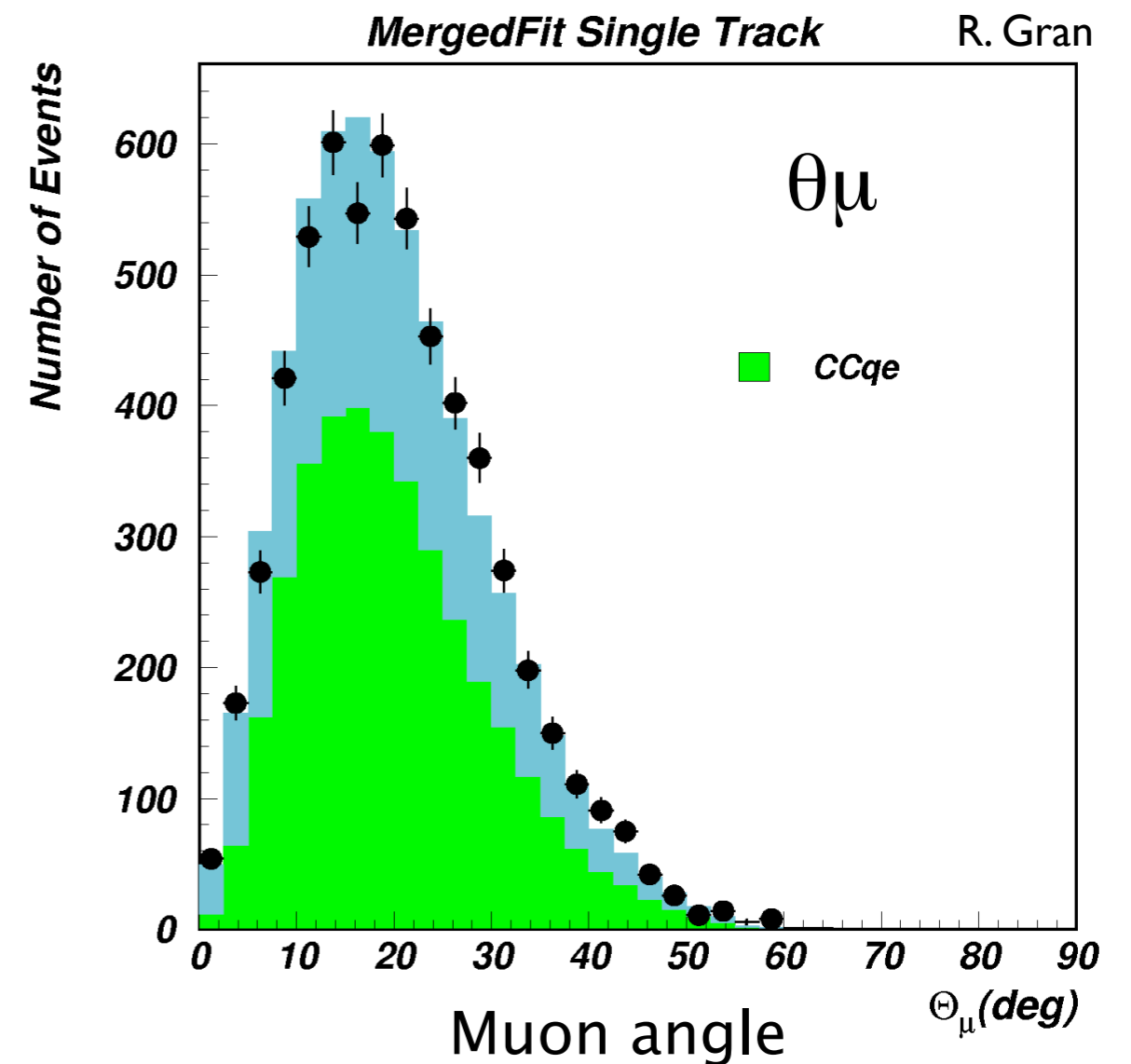
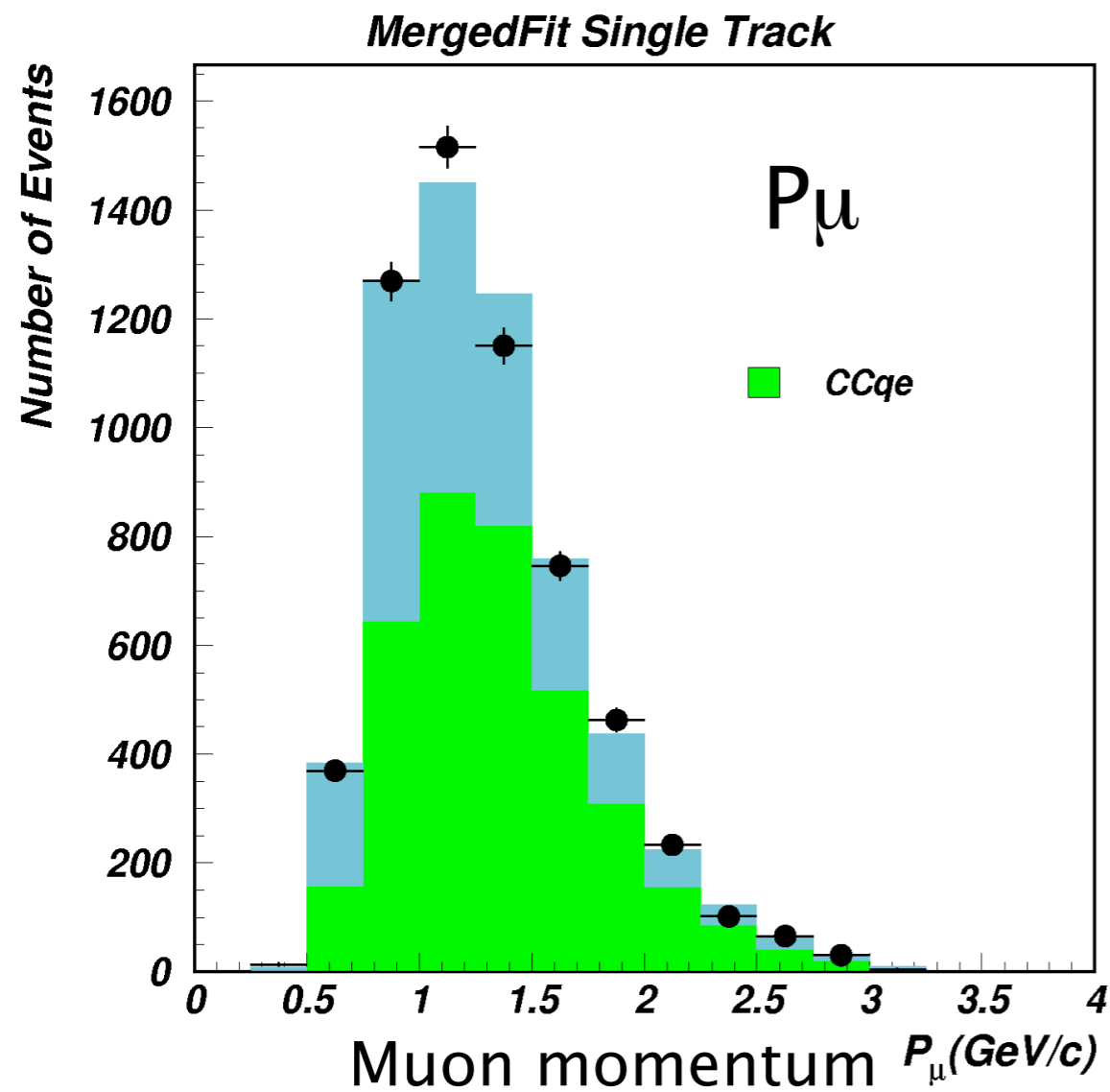
## SciFi 2 track $\cos(\Delta\Theta_p)$ distribution





# Basic Distributions, $P_\mu$ , $\theta_\mu$ for Scifi Detector

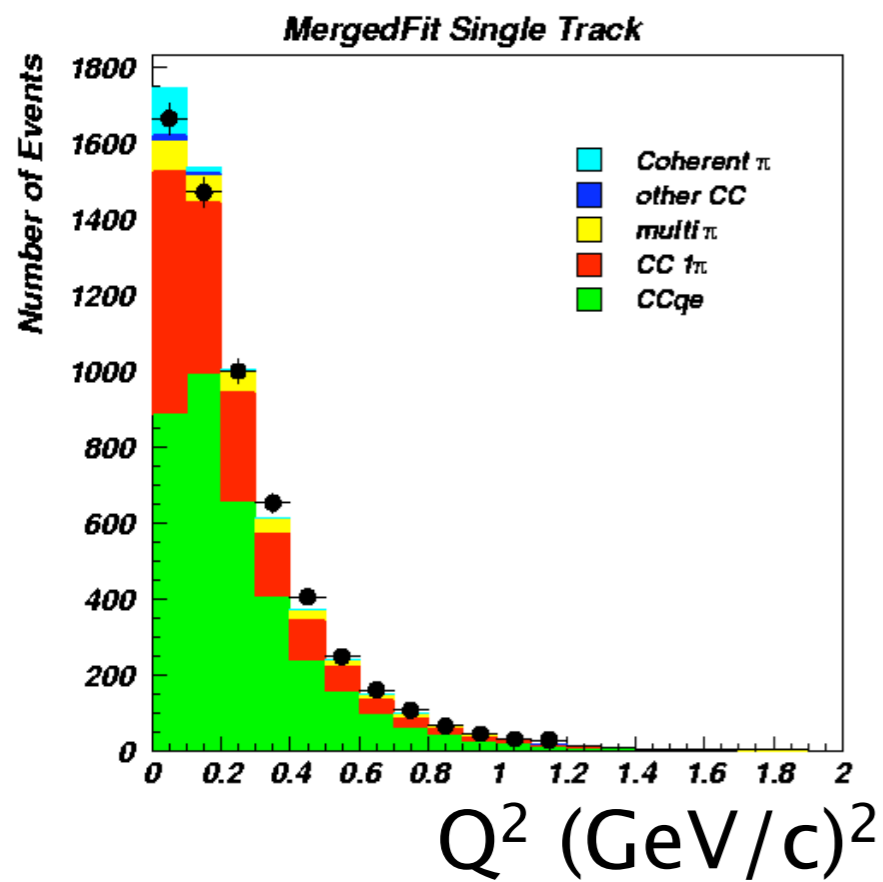
Overall agreement is good



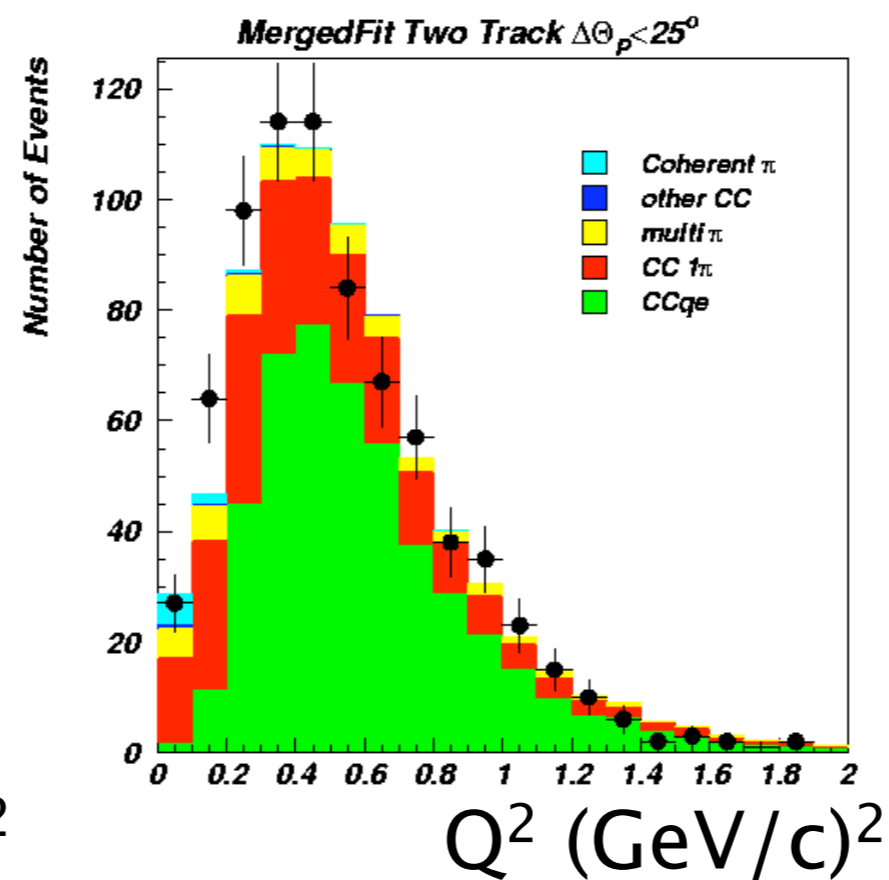
One-track events (60% QE, NEUT)

# Reconstructed $Q^2$ distribution in SciFi detector

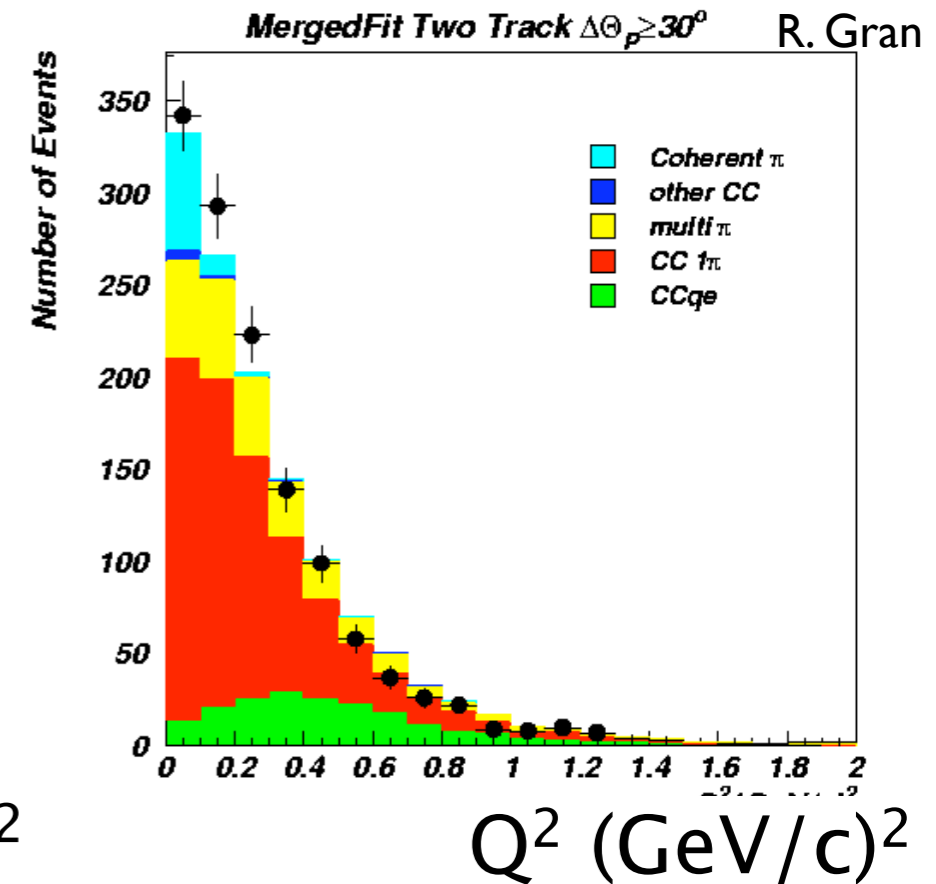
1 track sample



2 track QE enhanced



2 track non-QE

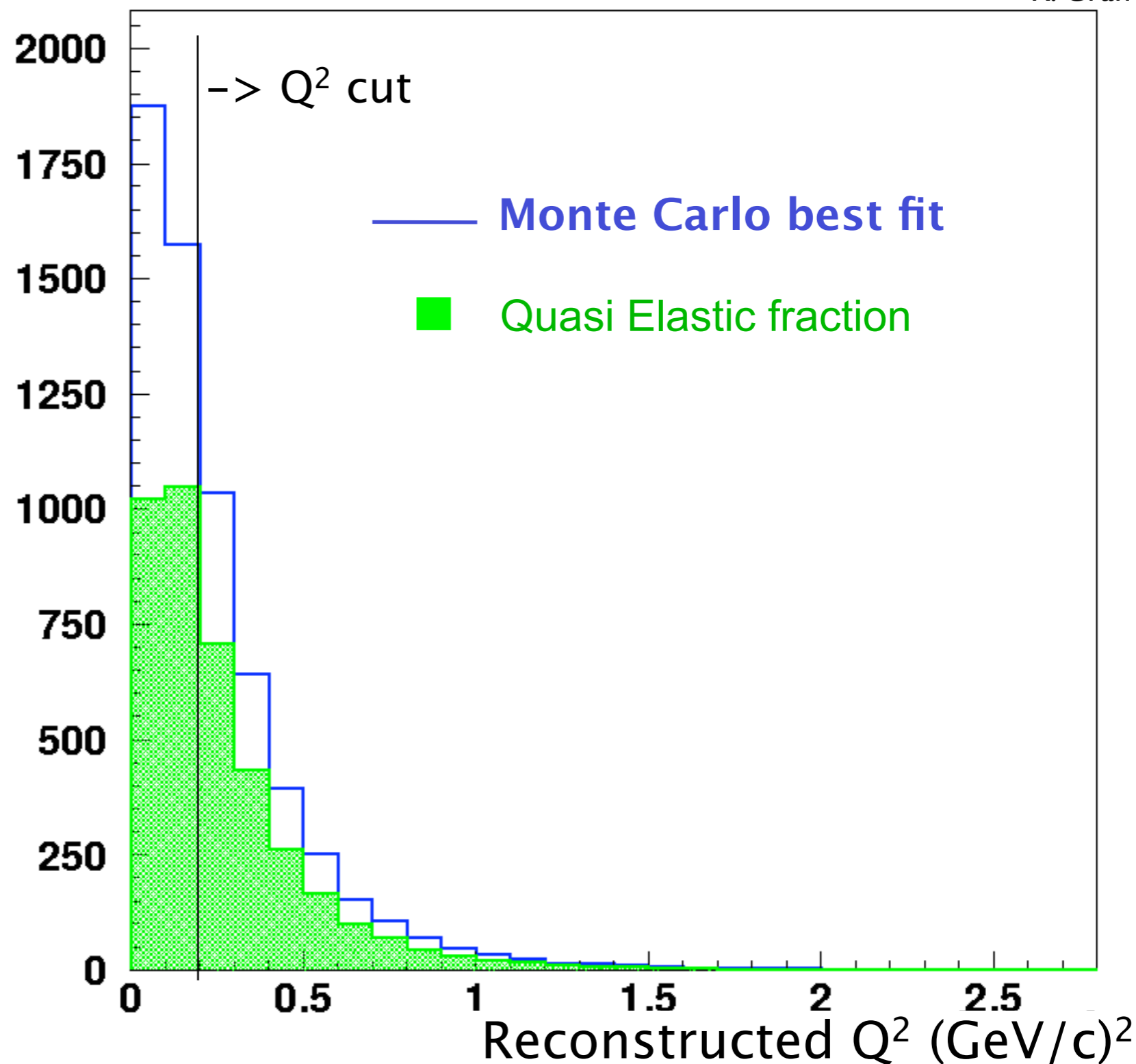


# Fit only $Q^2 > 0.2$ region

R. Gran

Most significant uncertainties due to Pauli blocking and choice of nuclear model, coherent pion, correction to DIS

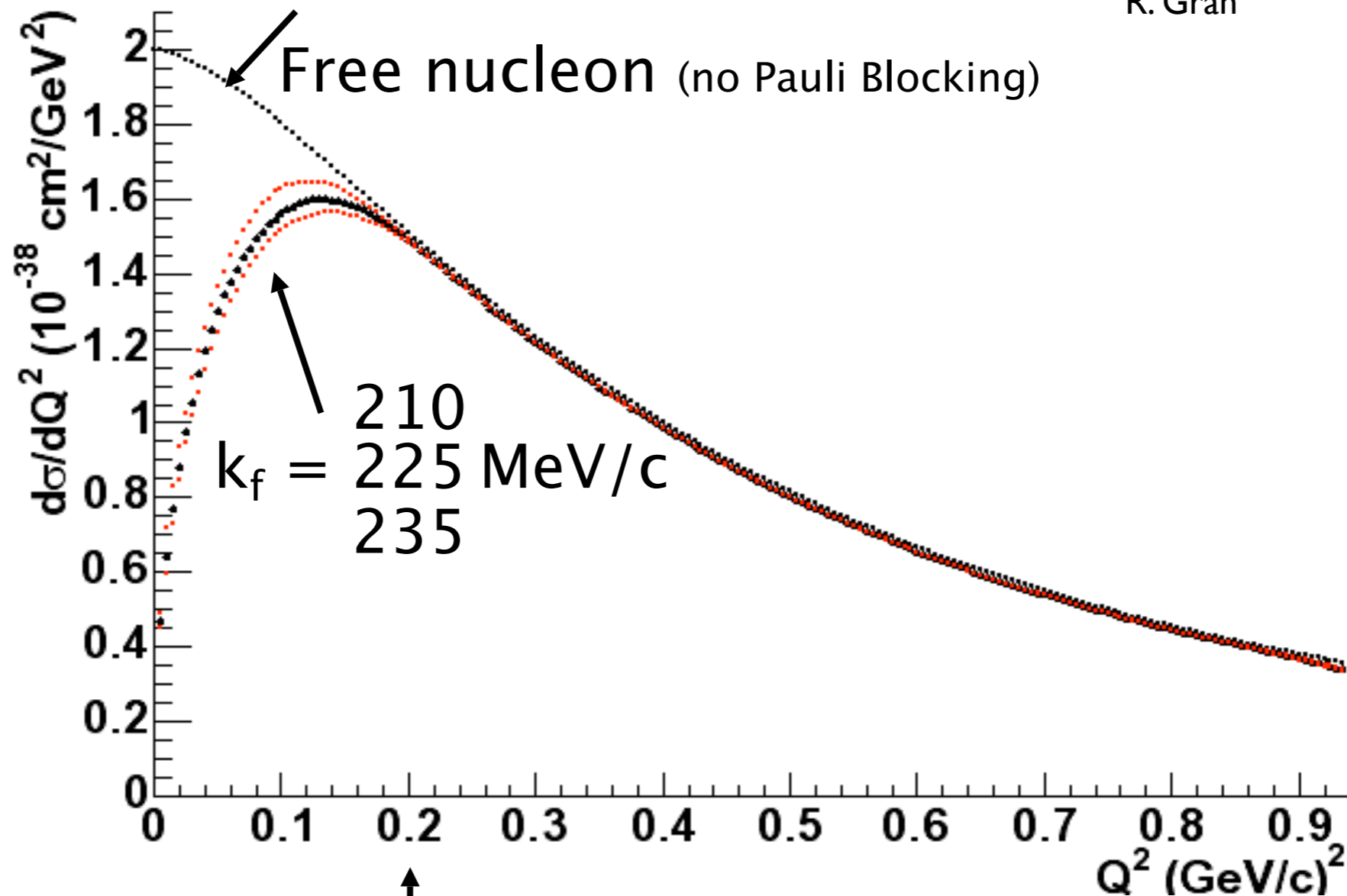
QE signal and inelastic background are treated the same way



# Uncertainty in QE cross section due to Pauli Blocking

in the  $Q^2 < 0.2$  region  
a Fermi-gas model with different Fermi-momenta  $k_f$

R. Gran



We Cut here

# K2K SciFi $M_A$ fit

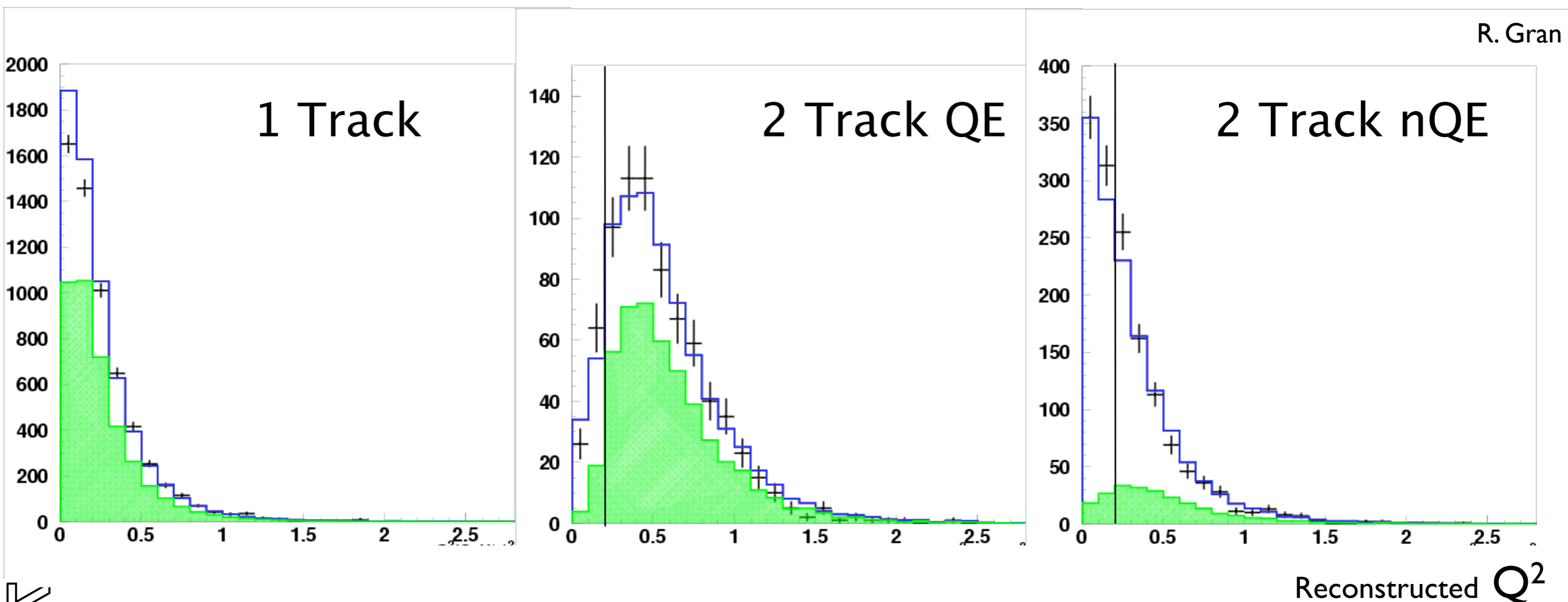
Fit the 1track, 2track (QE), and 2track (nonQE) simultaneously

K2K-I: 8114 events total 4310  $Q^2 > 0.2$  in fit

K2K-IIa: 5967 events total 2525  $Q^2 > 0.2$  in fit

$$M_A = 1.20 \pm 0.03 \text{ stat} \pm 0.12 \text{ syst}$$

Bodek/Yang DIS correction and Marteau Coherent Pi cross-section





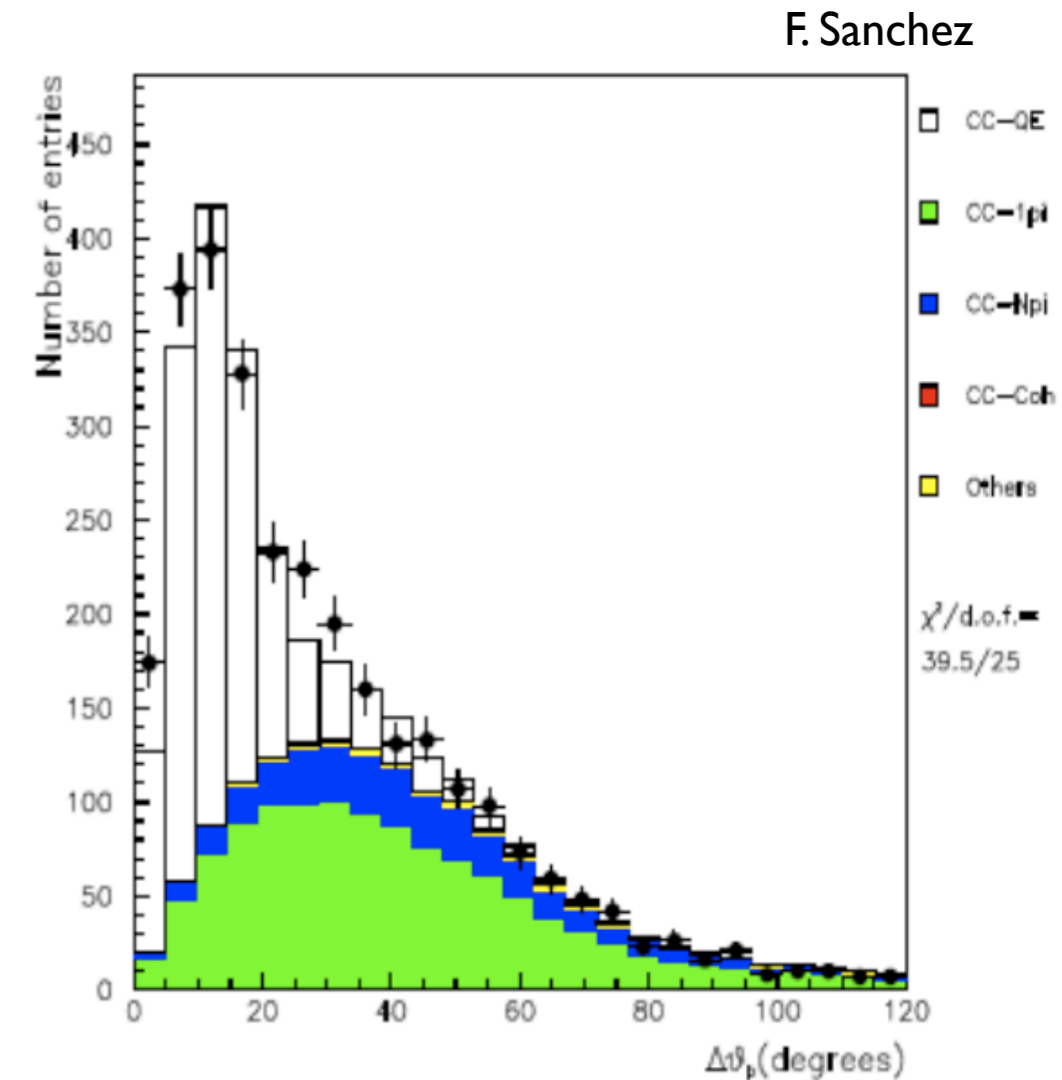
# Systematic Errors

Source	Uncertainty
Energy scale	0.08
LG density	0.02
Escale/LC correlation	0.04
Escale-MA correlation	0.03
MA- $I_{pi}$	0.03
nQE/QE	0.03
Statistics	0.012
<b>TOTAL</b>	<b>0.12</b>

# K2K: SciBar

- Event selection similar to SciBooNE's
  - (actually, SciBooNE's was based on K2K's)

Sample	$Q^2 > 0.0$	Purity	$Q^2 > 0.2$	Purity
1-trk	7405	54%	4032	59%
2-trk QE	1264	77%	1142	80%
2-trk non-QE	1537	19%	923	28%
<b>TOTAL</b>	<b>10206</b>	<b>52%</b>	<b>6097</b>	<b>59%</b>



# K2K: SciBar

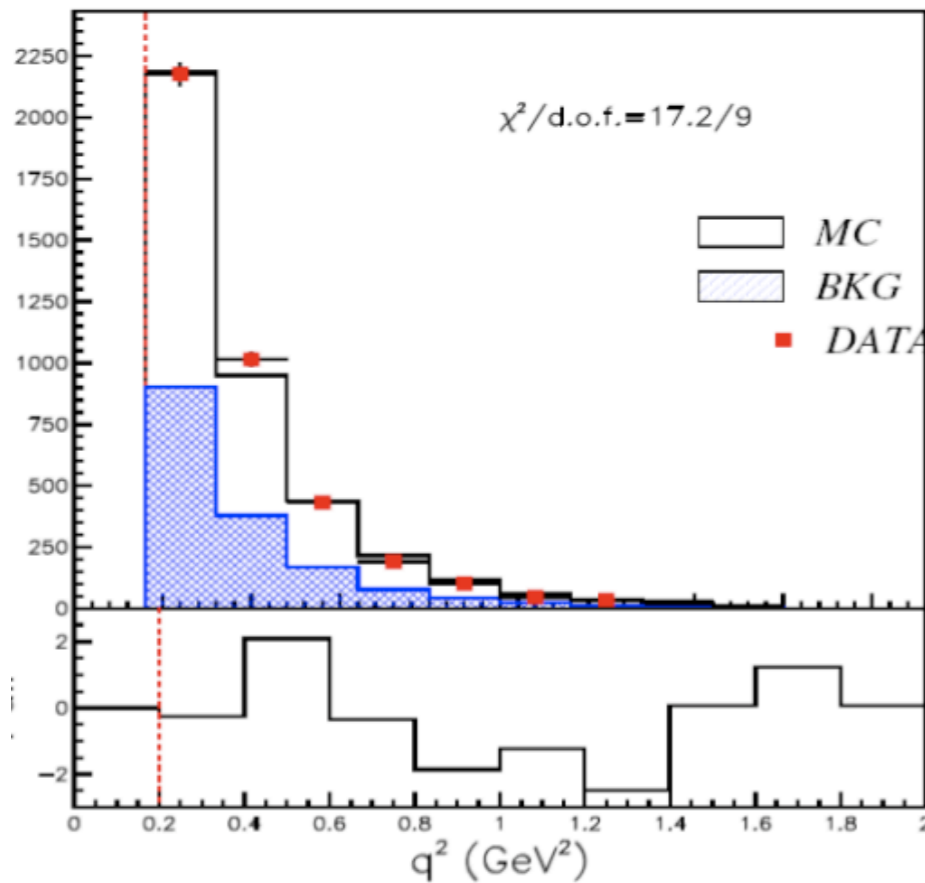
- Fit 3 data samples, allowing these parameters to float:
  - Overall normalization
  - $M_A$
  - Ratio of nonQE/QE
  - Ratio of 2-trk/1-trk
  - Ratio of 2-trk nonQE/2-trk QE
  - 4 energy bins constrained by PIMON data



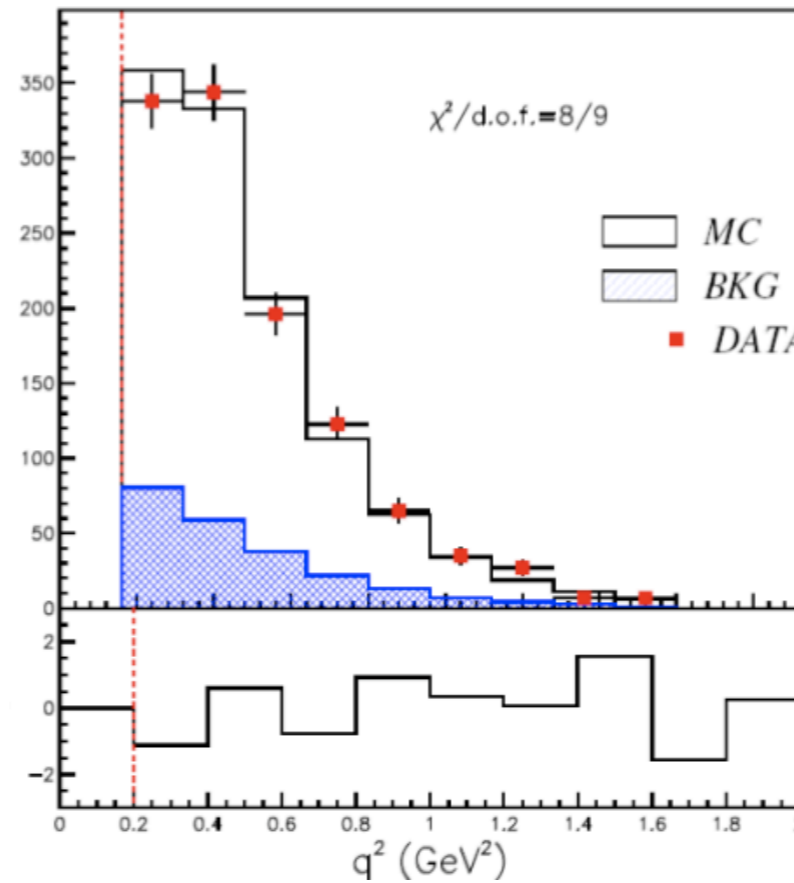
# K2K: SciBar

F. Sanchez

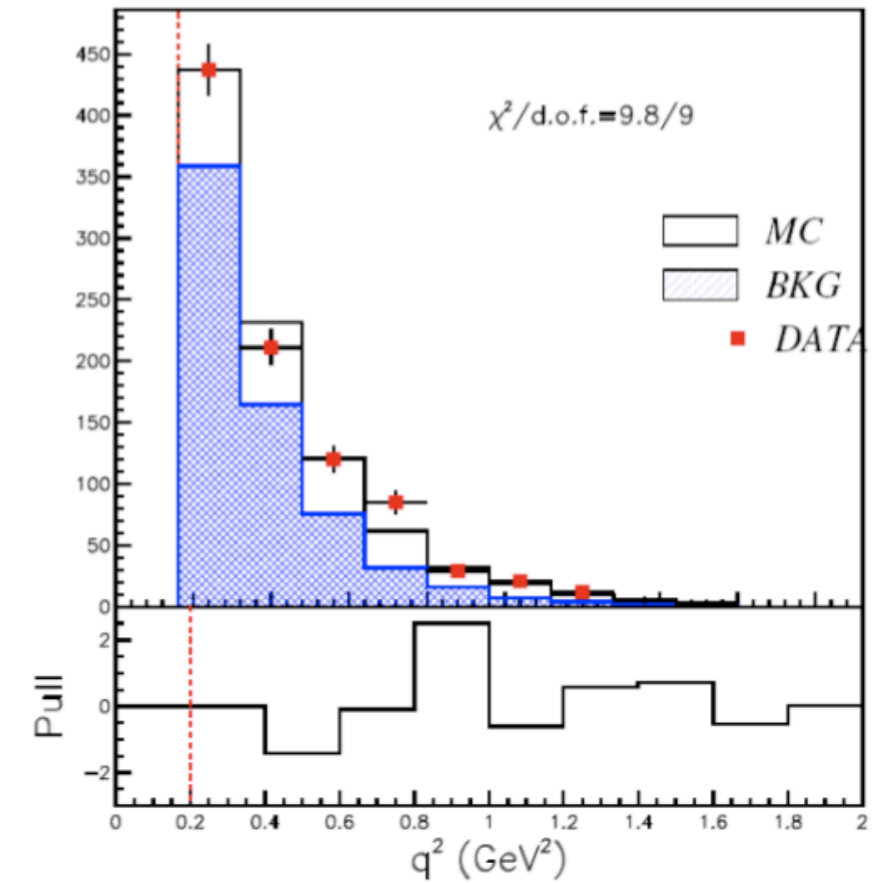
1 Track samples



2 Track-QE samples



2 Track-NQE samples



$$M_A = 1.144 \pm 0.077 \text{ (fit)} +0.078 -0.072 \text{ (syst)}$$

# K2K: SciBar Systematics

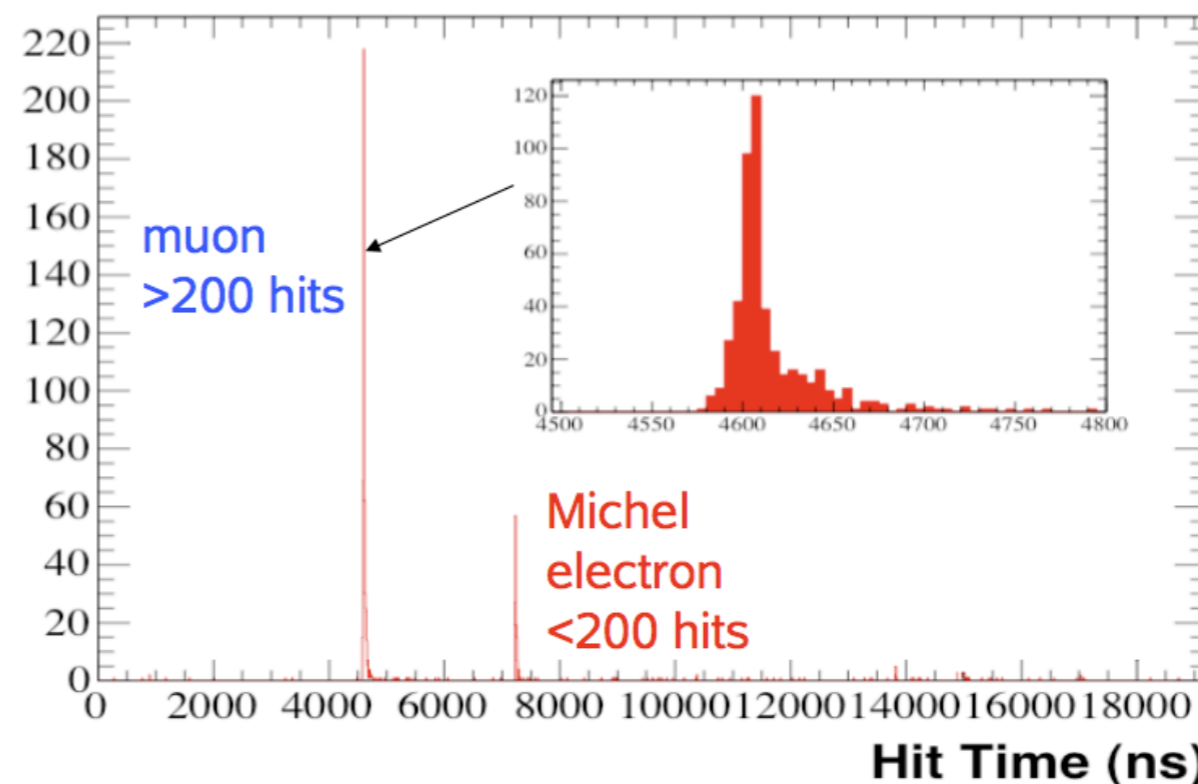
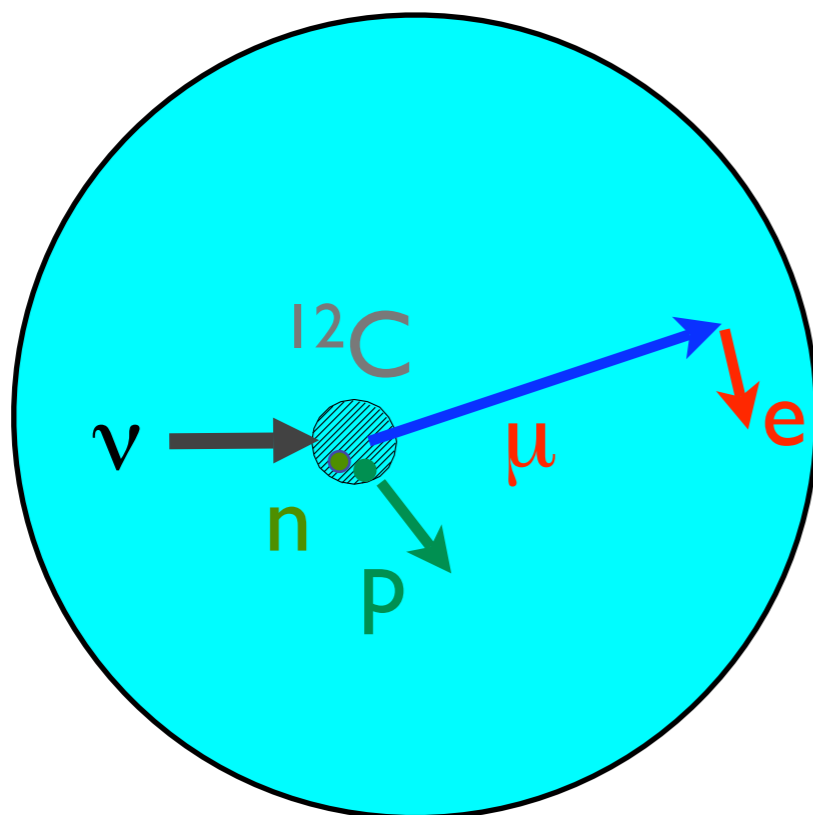
Sources of uncertainty	Error in $M_A$	Error in $R^{nQE/QE}$
Momentum Scale	+0.030 -0.030	+0.014 -0.014
Cross section and nuclear effects	+0.035 -0.058	+0.09 -0.15
Detector	+0.051 -0.027	+0.024 -0.030
Analysis	+0.012 -0.037	+0.0 -0.34
Total	+0.078 -0.072	+0.094 -0.37





**MiniBooNE CCQE**

# MiniBooNE Cuts

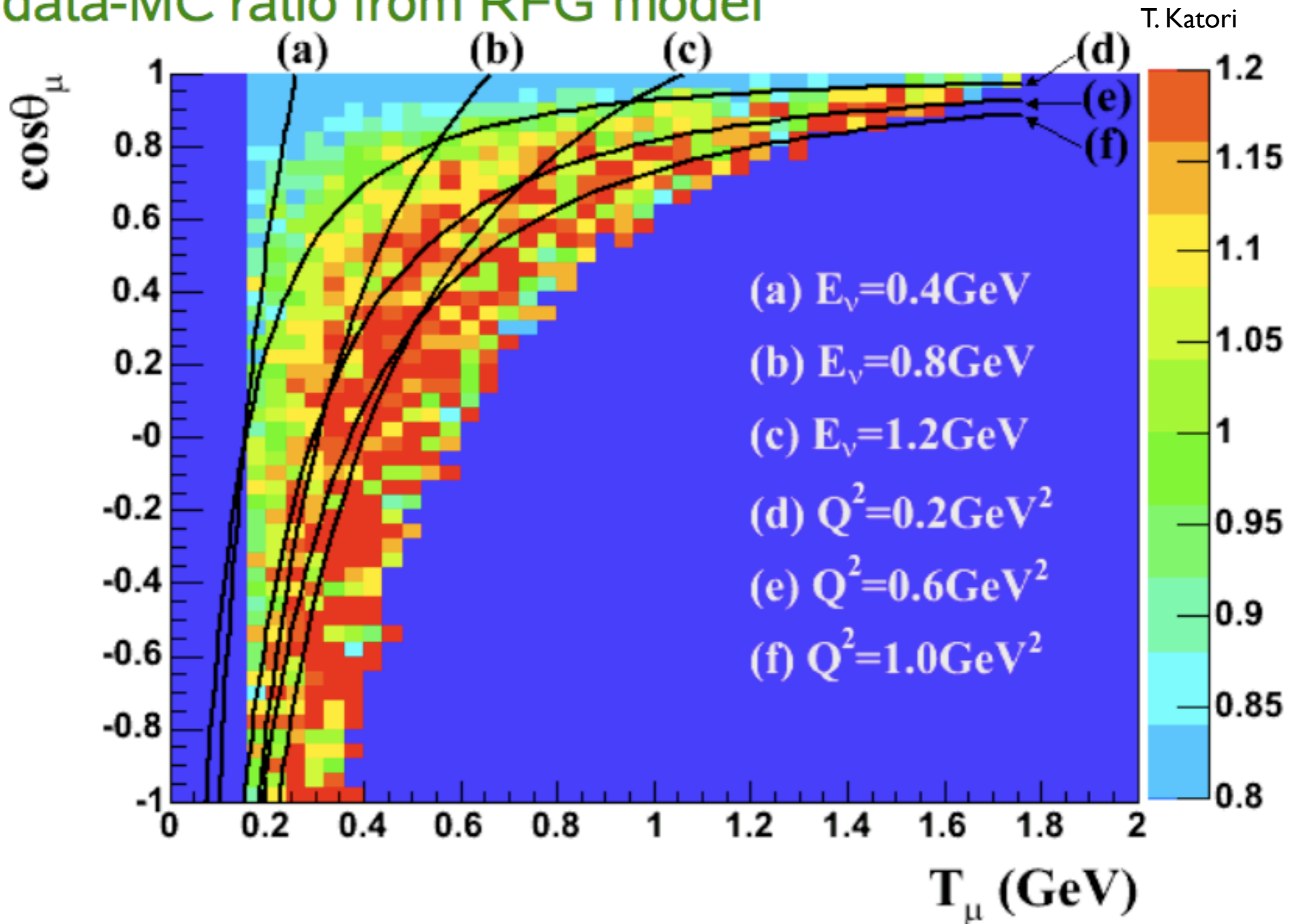


total 2 subevents	54.2%
muon in beam window (4400ns < Time < 6400ns)	52.9%
muon veto hits < 6 and Michel electron veto hits < 6	46.4%
muon tank hits > 200 and Michel electron tank hits < 200	41.6%
fiducial reconstruction for muon	41.3%
muon and electron distance < 100cm	35.0%

74% pure CCQE (NUANCE)

# MiniBooNE Data/MC

data-MC ratio from RFG model





## 2. Prediction for CCQE events

Smith and Moniz,  
Nucl.,Phys.,B43(1972)605

### Relativistic Fermi Gas (RFG) Model

Carbon is described by the collection of incoherent Fermi gas particles.

All details come from hadronic tensor.

$$(W_{\mu\nu})_{ab} = \int_{E_{lo}}^{E_{hi}} f(\mathbf{k}, \mathbf{q}, w) T_{\mu\nu} dE : \text{hadronic tensor}$$

$f(\mathbf{k}, \mathbf{q}, w)$ : nucleon phase space density function

$T_{\mu\nu} = T_{\mu\nu}(F_1, F_2, F_A, F_P)$ : nucleon tensor

$F_A(Q^2) = g_A / (1 + Q^2 / M_A^2)^2$ : Axial form factor

$E_{hi}$ : the highest energy state of nucleon =  $\sqrt{(p_F^2 + M^2)}$

$E_{lo}$ : the lowest energy state of nucleon =  $\sqrt{(p_F^2 + M^2)} - w + E_B$

3 parameters are especially important to control nuclear effect of Carbon;

$M_A = 1.03\text{GeV}$ : axial mass

$p_F = 220\text{MeV}$ : Fermi momentum

$E_B = 34\text{MeV}$ : binding energy

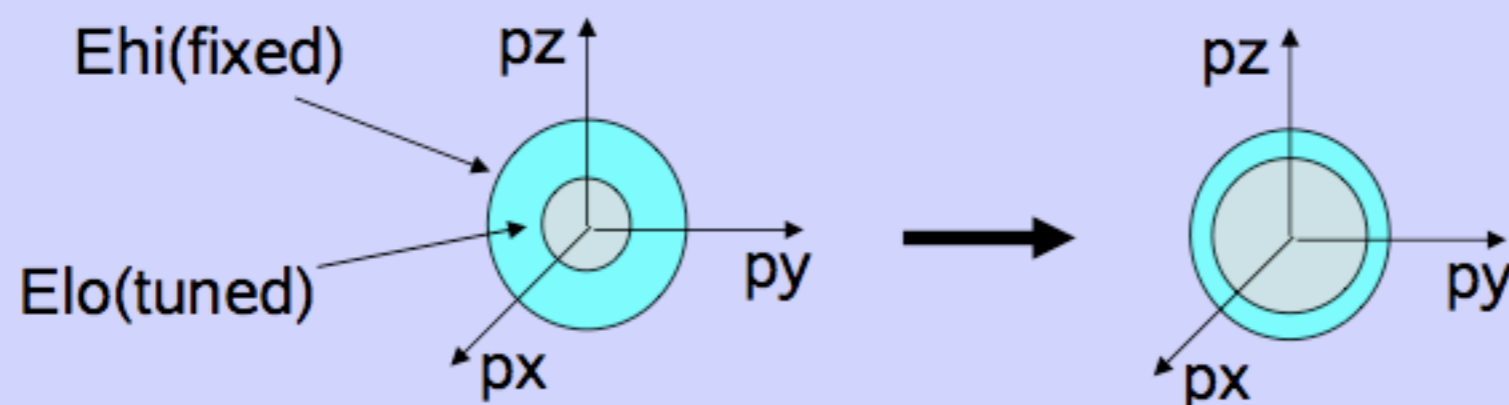


### 3. CCQE data-MC comparison

Pauli blocking parameter "kappa" :  $\kappa$

To enhance the Pauli blocking at low  $Q^2$ , we introduced a new parameter  $\kappa$ , which is the scale factor of lower bound of nucleon sea and controls the size of nucleon phase space

$$E_{lo} = \kappa \left( \sqrt{(p_F^2 + M^2)} - w + E_B \right)$$



This modification gives significant effect only at low  $Q^2$  region

We tune the nuclear parameters in RFG model using  $Q^2$  distribution;

$M_A$  = tuned

$P_F$  = fixed

$E_B$  = fixed

$\kappa$  = tuned

05/31/2007

Teppei Katori, Indiana University, N

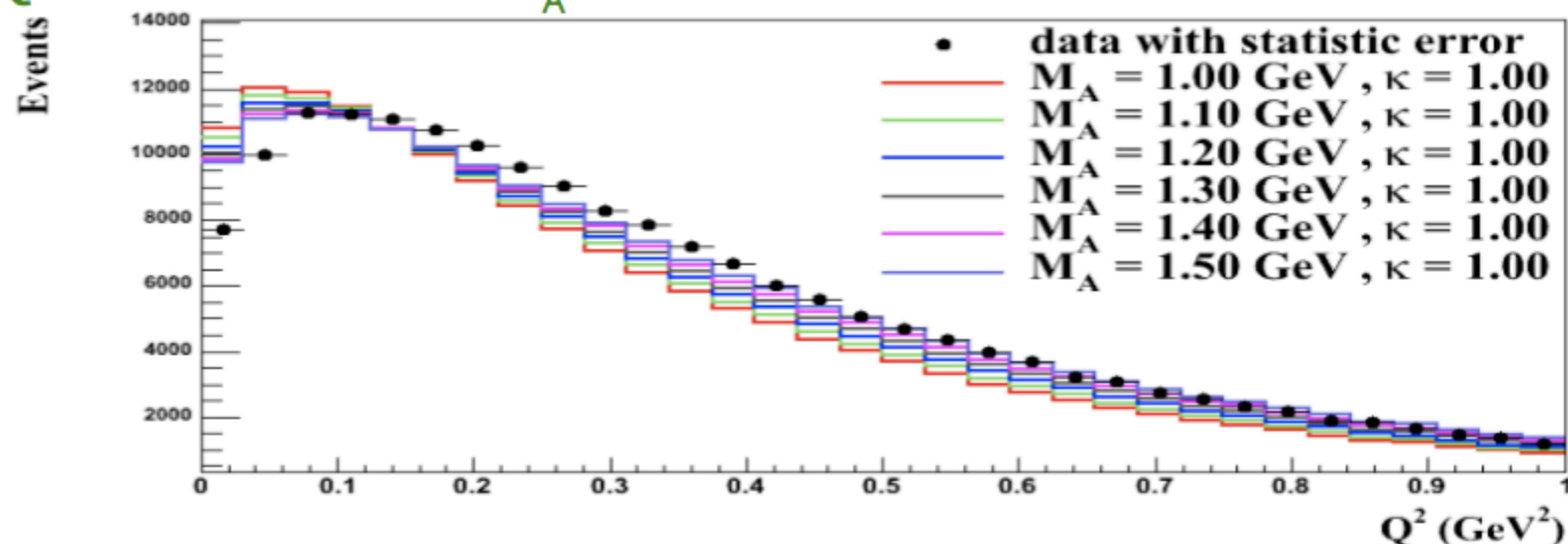
17



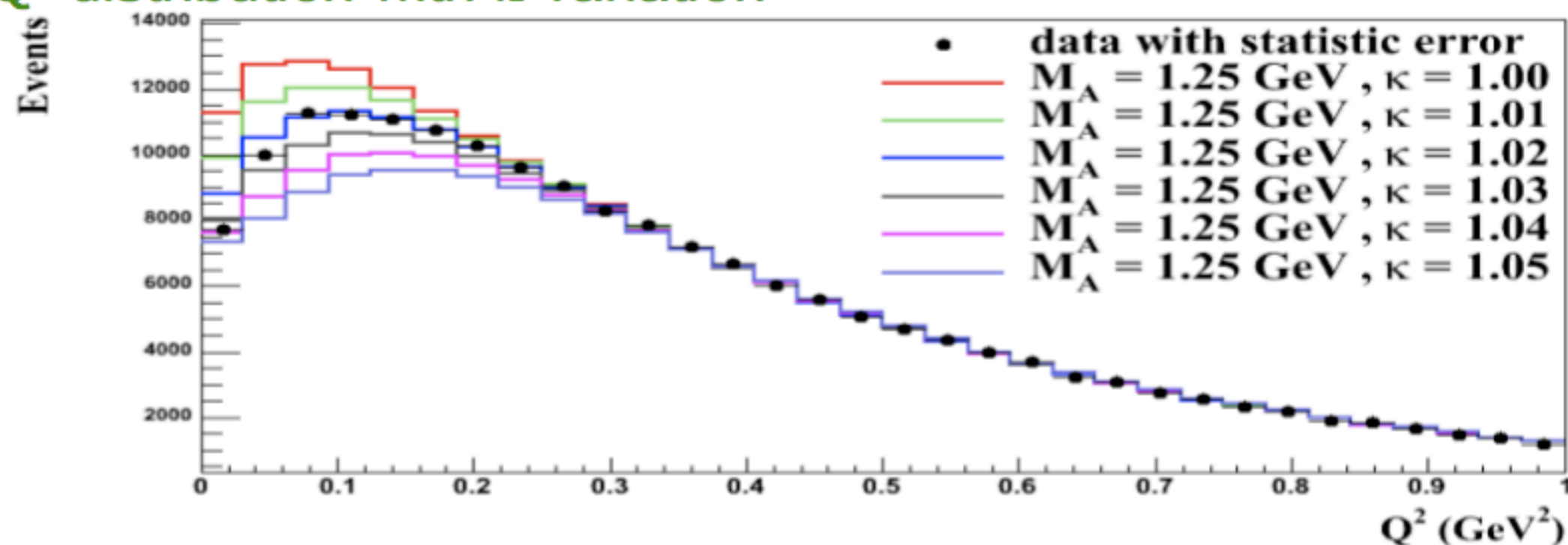
# Effect of $M_A$ and $\kappa$

$Q^2$  distribution with  $M_A$  variation

T. Katori

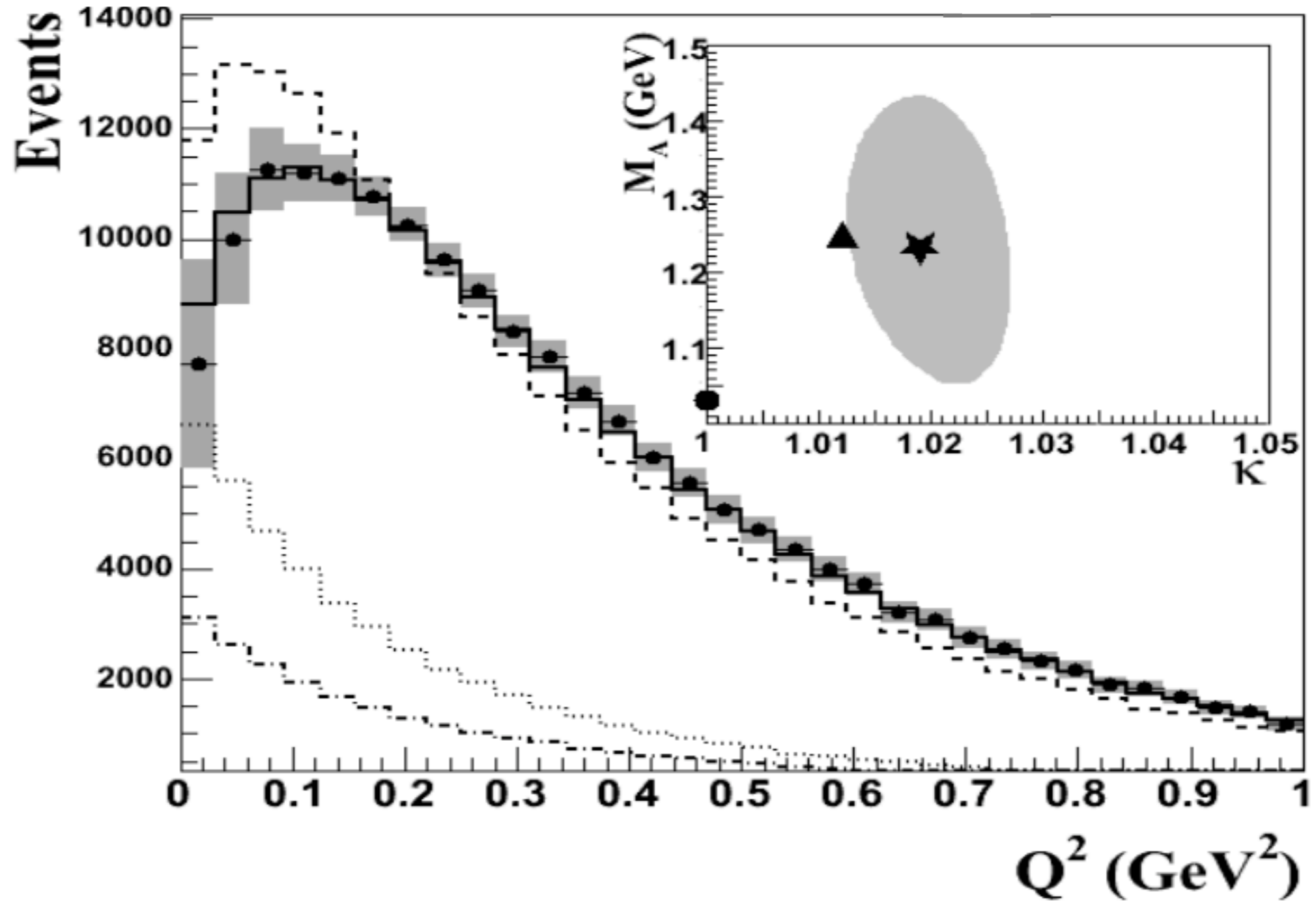


$Q^2$  distribution with  $\kappa$  variation



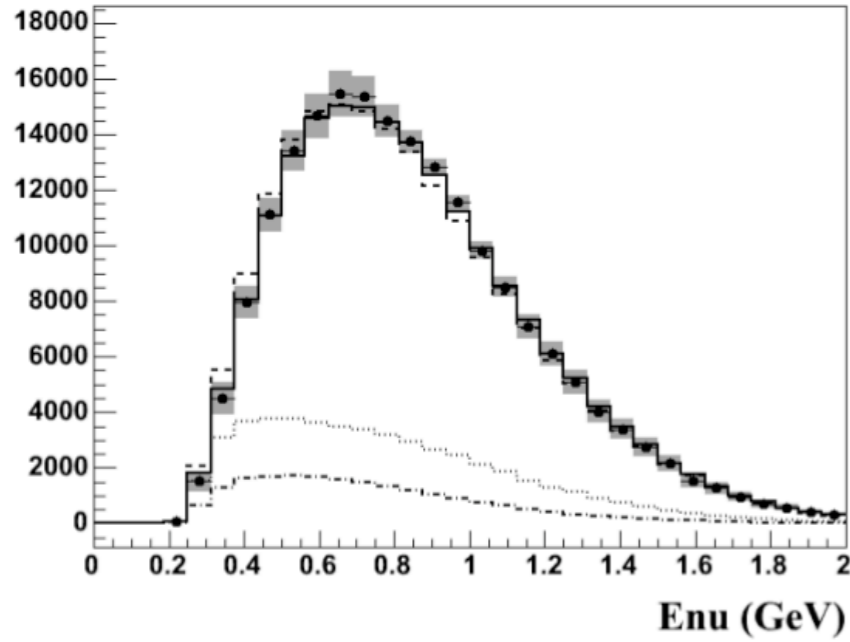
# After Fitting

T. Katori

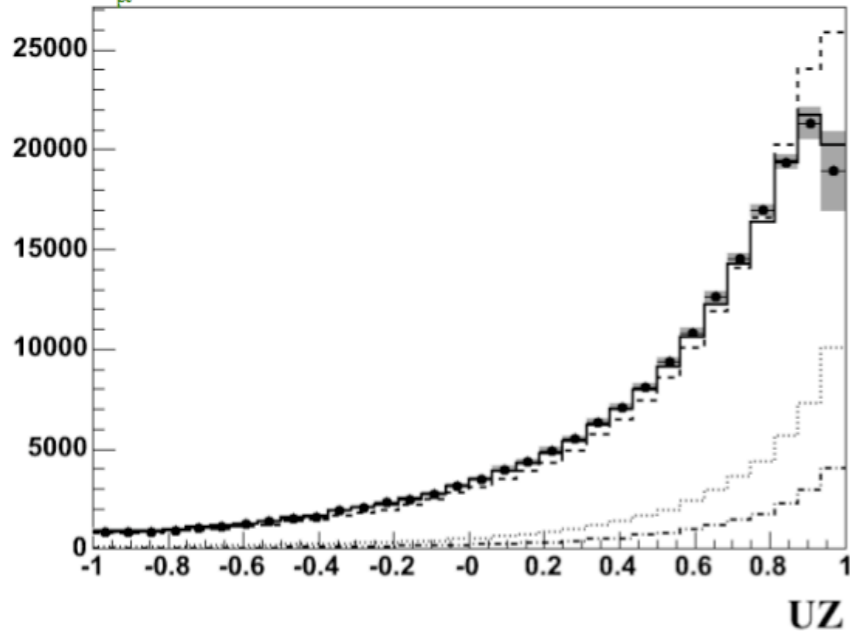


# After fitting

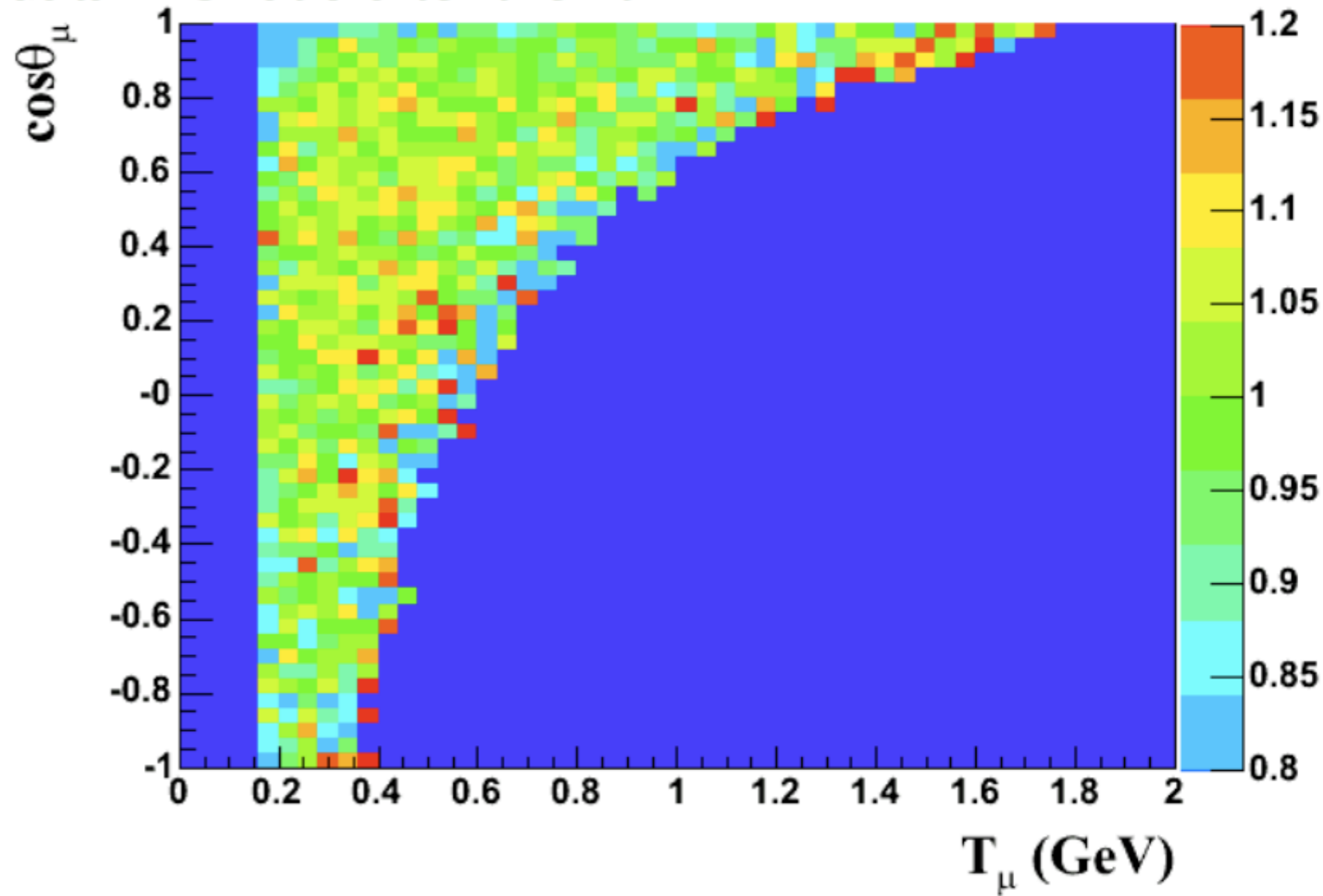
Ev distribution



$\cos\theta_\mu$  distribution



data-MC ratio after the fit

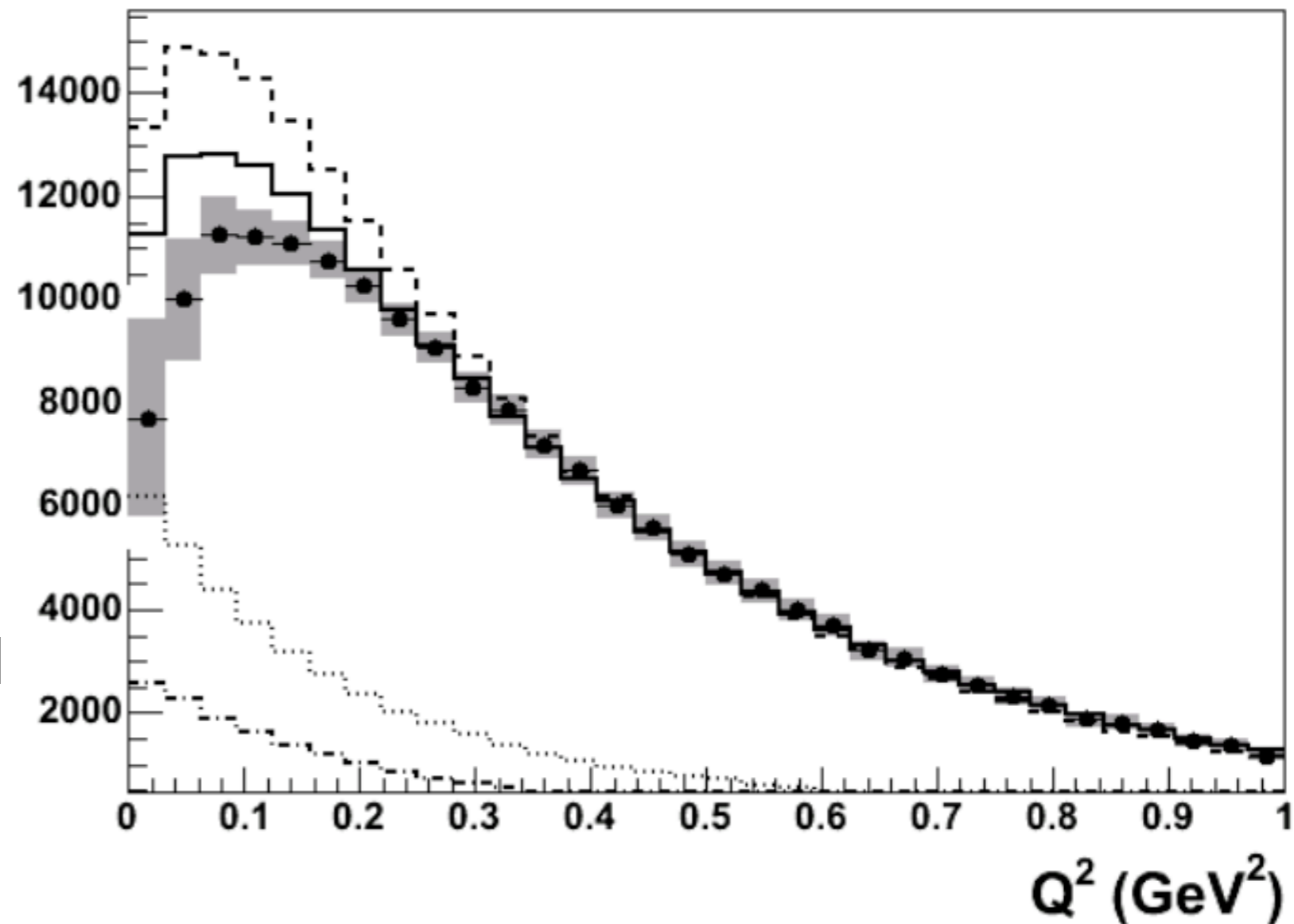


T. Katori

# Is $\kappa$ necessary?

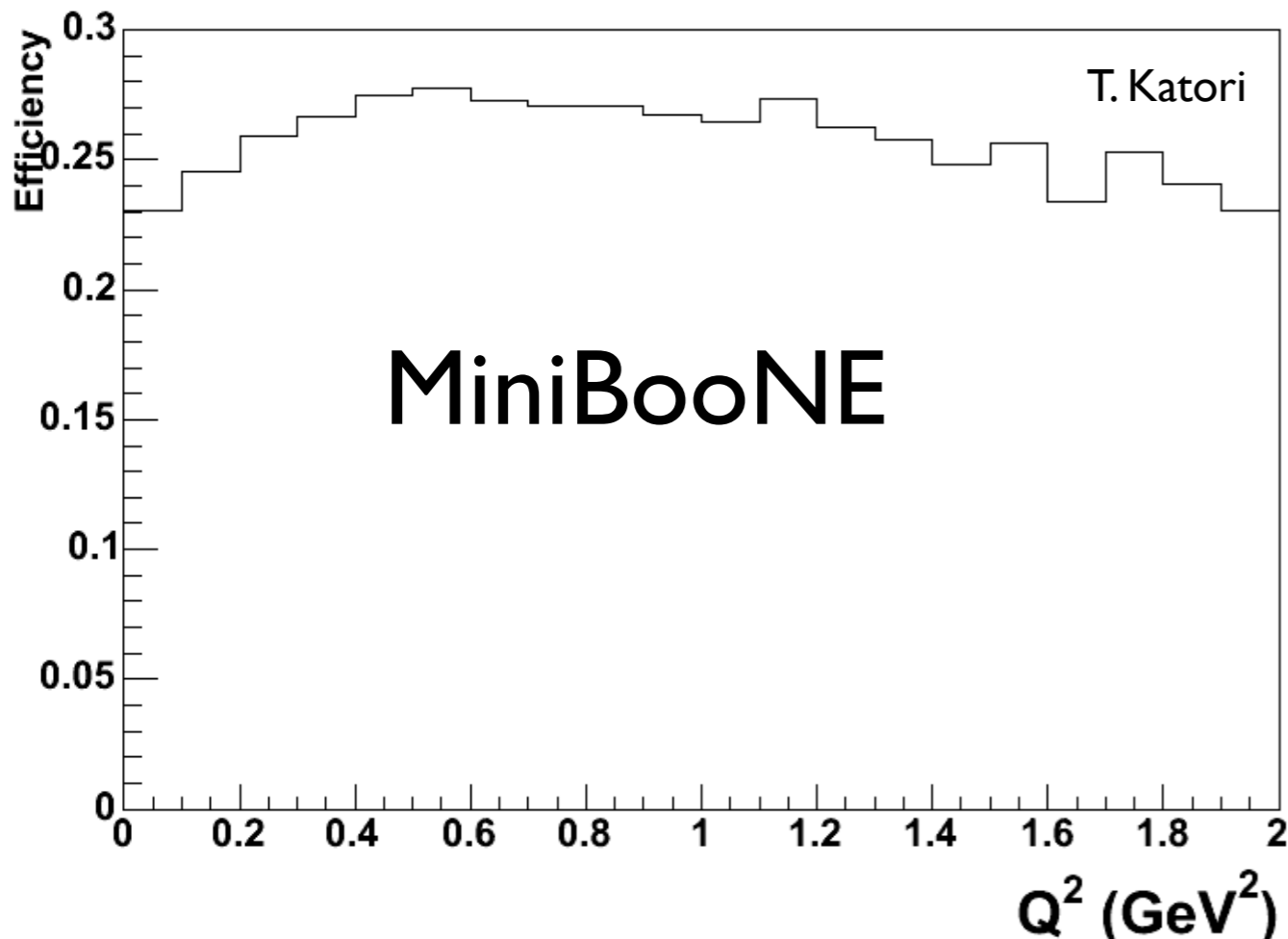
T. Katori

- Only MA is allowed to vary in this fit
- Such a fit cannot improve over all phase space
- (Additional experimental information would allow different tests)



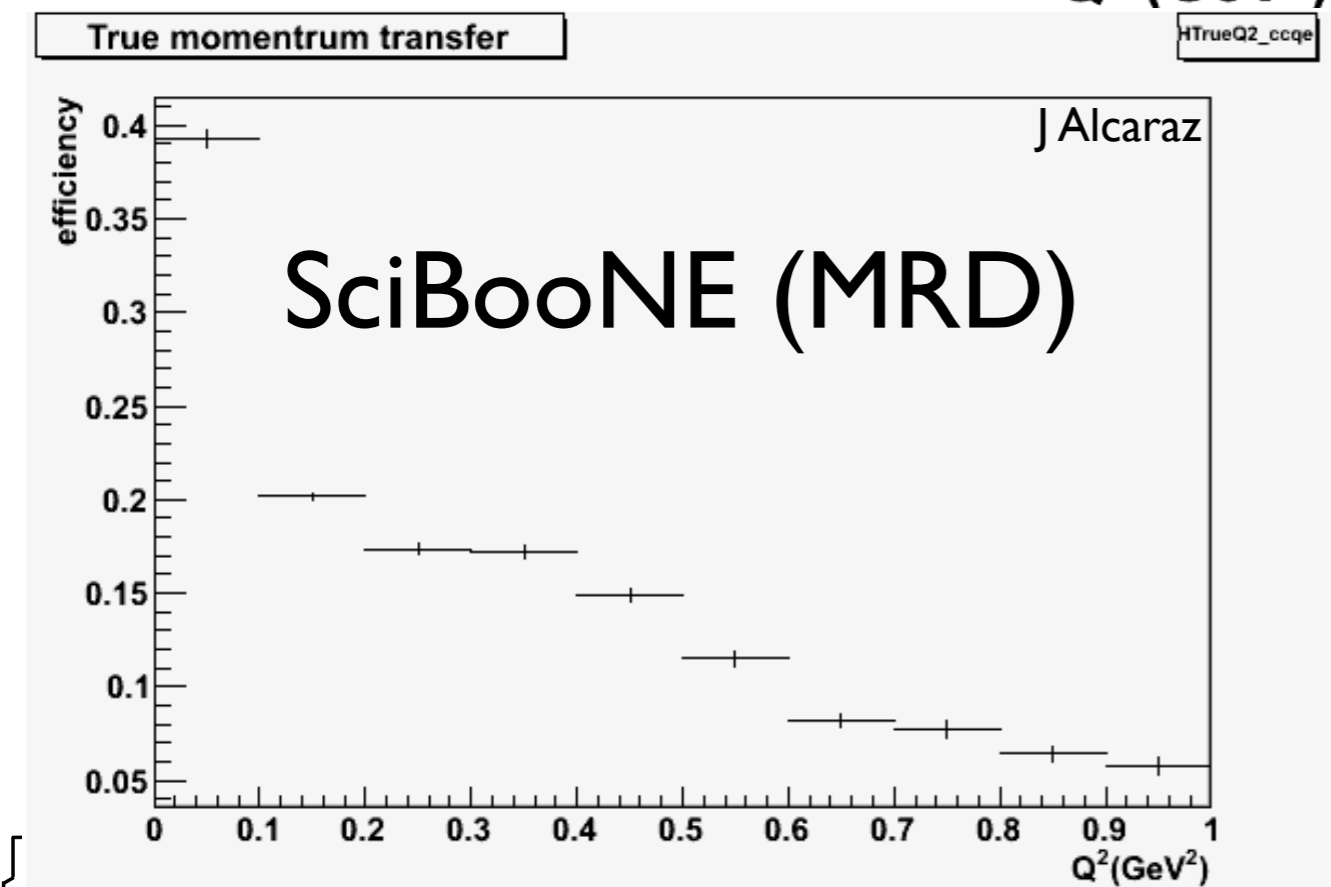
# MB CCQE Systematics

Source	$\delta M_A(\text{GeV})$	$\delta \kappa$
Data statistics	0.03	0.003
neutrino flux	0.04	0.003
neutrino cross section	0.06	0.004
detector model	0.10	0.003
CCpi+ background shape	0.02	0.007
<b>TOTAL</b>	<b>0.20</b>	<b>0.011</b>



# Comparisons

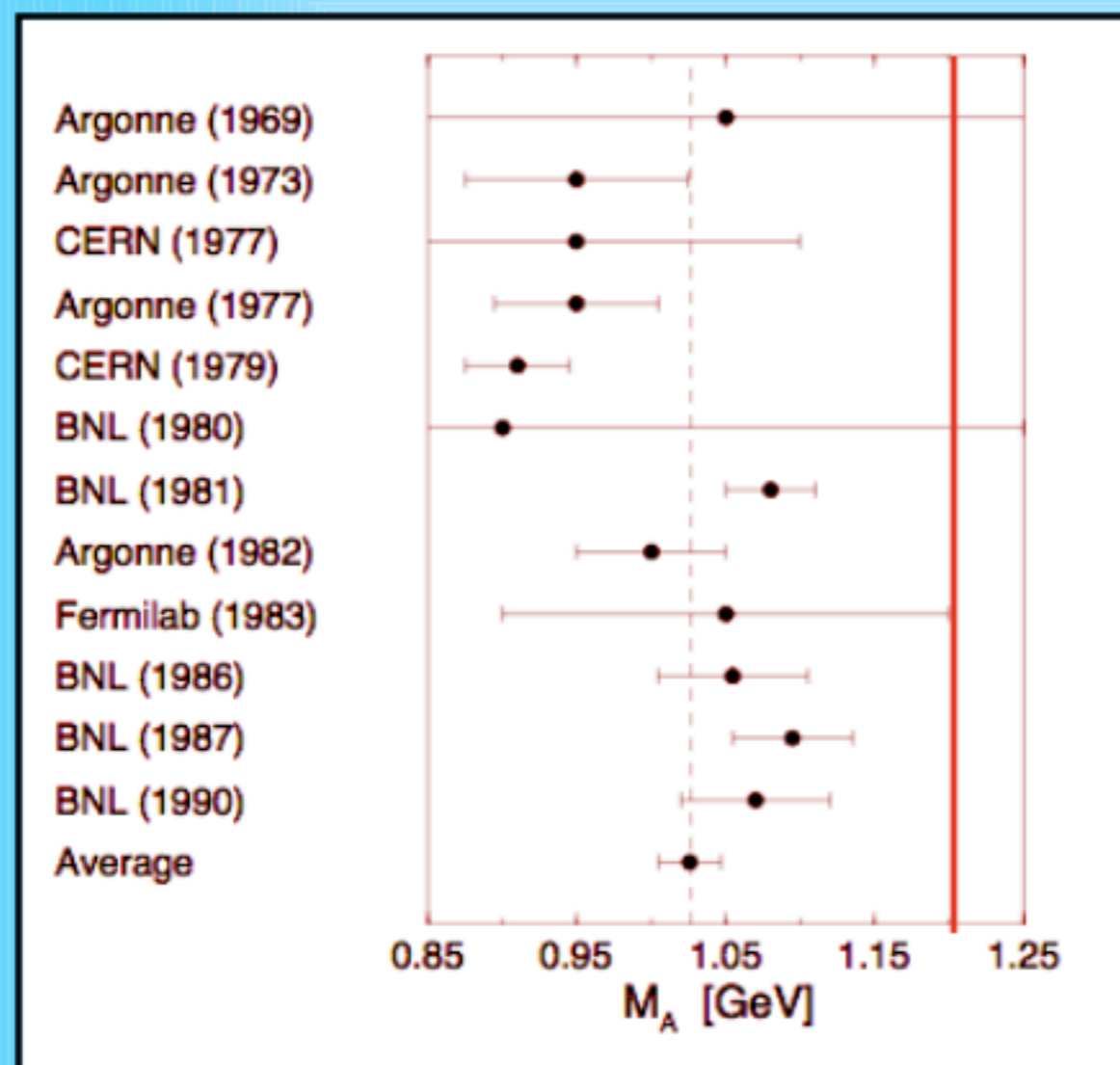
- MiniBooNE has nearly flat acceptance in  $Q^2$
- But no resolution of protons
- SciBooNE (with MRD) falls off quickly because we require a forward going muon
- SciBar contained analysis is needed!





# Summary

## Why is this Interesting?



world avg:  $M_A = 1.03 \pm 0.02$  GeV  
J.Phys.G28, R1 (2002)

- **K2K SciFi** ( $H_2O$ ,  $Q^2 > 0.2$ )  
Phys. Rev. **D74**, 052002 (2006)

$$M_A = 1.20 \pm 0.12 \text{ GeV}$$

- **K2K SciBar** ( $^{12}C$ ,  $Q^2 > 0.2$ )

$$M_A = 1.14 \pm 0.11 \text{ GeV}$$

- **MiniBooNE** ( $^{12}C$ ,  $Q^2 > 0.25$ )

$$M_A = 1.25 \pm 0.12 \text{ GeV}$$

- new results consistent
- 10% measurements of  $M_A$
- modern data measuring systematically higher  $M_A$  (measuring an "effective  $M_A$ ")



# References

- SciFi: Phys.Rev. D74 (2006) 052002, [hep-ex/0603034v1](#)
- SciBar: NuInt07 proceedings
- MinBooNE: Phys.Rev.Lett **100**:032301 (2008) [arXiv:0706.0926v2](#) [hep-ex]

*I didn't mention:*

- NOMAD: [arXiv:0812.4543v3](#) [hep-ex]
  - $M_A = 1.05 \pm 0.02(\text{stat}) \pm 0.06(\text{syst}) \text{ GeV}$ .