### Course Program

Lesson 1 : Elements of QCD for hadron colliders, jets definition and cross section

Lesson 2 : Determination of Parton Distribution Functions (PDF),  $\alpha_{s}$ 

- Lesson 3 : Measurement of b and c quark cross section
- Lesson 4 : top quark cross section measurement
- Lesson 5 : top quark mass measurement
- Lesson 6 : top quark properties measurement
- Lesson 7 : new physics searches
- Lesson 8 : new physics searches

## **Elements of QCD: Introduction**

The material of these lessons is taken from:

Elements of QCD for hadron colliders, G. P. Salam arXiv:1011.5131v2 [hep-ph] 10 Jan 2011

Introduction to High Energy Physics, D. H. Perkins

QCD and Collider Physics, Ellis, Stirling, Webber

## **Elements of QCD: Introduction**

The QCD (Quantum Chromo-Dynamics) is the theory of quarks, gluons and their interactions.

It has similarity and differences with QED:

- electrons have electric charge, quarks have colour charge
- there is only 1 electric charge but 3 colours: red, green and blue
- photons are neutral, gluons carry colour charge and there are 8 possible combinations of colours and anti-colours charge
- the coupling  $\alpha_s$  tend to zero at high momentum scales and it is large at small scale while QED is the opposite.

The QCD is Lagrangian similar to QED one, it can be written with terms that are quark-quark, quark-gluon and gluon-gluon interactions.

## Elements of QCD: tools - 1

How do you use this theory to make predictions?

#### 1. Lattice QCD:

- -The most complete approach.
- build a 4-dimensional lattice with imaginary time by discretizing space-time and considering quark and gluon fields values at all the vertices.
- Monte Carlo sampling over all possible field configurations determines the relative likelihood of different field configurations providing solution to QCD.
- This is very useful for "static" predictions like particle masses
- Not suitable for processes at very high energy like LHC where the number of particles to follow is very high and a huge number of nodes is needed.

## Elements of QCD:tools - 2

#### 2. Perturbative QCD:

- Order-by-order expansion in  $\,\alpha_{\!_{\! s}}$  . An observable f can be written:

$$f = f_1 \alpha_s + f_2 \alpha_s^2 + f_3 \alpha_s^3 + \dots$$

Where only the first two (or three) terms are calculated and the other are assumed to be negligible.

- the f factors are calculated via Feynman diagrams



Note: colour currents

## Elements of QCD: $\alpha_s$

The value of  $\alpha_s = g_s/4\pi$  depends on the scale  $\mu$  at which it is calculated With some approximations we can write:

 $\alpha_{s}(q^{2}) = \frac{1}{b_{0} \ln(\frac{q^{2}}{\Lambda^{2}})}$  where  $\Lambda$  (or  $\Lambda_{QCD}$ ) is the scale at which the coupling Diverges.

Only  $q \gg \Lambda \Rightarrow \alpha_s(q^2) \ll 1$  the perturbation theory is valid.  $\Lambda$  is not well defined since it is non-perturbative quantity, it depends on the approximations made in the  $\alpha_s$  definition. The order of magnitude used is ~200 MeV

## Elements of QCD: running coupling

At high momentum scale  $\alpha_s$  the coupling become weaker, quarks and gluons do not interact, the theory is almost a free theory. At low momentum scale the coupling grows forcing the quarks and gluons to be bound in the hadrons. This is exactly the opposite of QED. Several explanations more or

less intuitive have been tried. The gluon colour charge is the basis. Measurements of  $\alpha_{e}$  will be discussed.



## Elements of QCD: $e+e- \rightarrow hadrons$

- These process have allowed to study and verify QCD predictions
- Hadrons only in the final state
- Plethora of data from LEP and SLC

Very important approximations soft and collinear:

- soft: the gluon emitted by partons (quarks or gluons) has very low energy
- collinear: the gluon emitted by partons is very close in angle to the emitting partons

The amplitude



can be calculated easily.

### $e+e- \rightarrow$ hadrons: particles in the final state

The emitted gluon can emit itself other gluons. The gluons can split in quarks and so forth. These process go on till the  $\Lambda$  scale (a,b).



This process describes a complex final state, still in term of partons. Hadrons are formed in the so called "hadronization" phase, a non-perturbative process (c).

Hadrons properties:

- directions and momenta closely related to the parton's ones
- multiplicity very similar to the parton's

The event (d) (OPAL) shows the same angular distribution of partons.

Hadronization: low momentum-transfer, long-distance regime → non-perturbative effects dominate.

General approach: local parton-hadron duality

The flow of momentum and quantum numbers at hadron level tends to follow the flow established at parton level.

Ex.: the flavour of the quark initiating the shower should be found in a hadron near the jet axis.

Mainly three models of fragmentation are used.

#### Independent fragmentation

- original approach of Field and Feynman
- each parton fragments independently
- designed to reproduce the limited transverse momenta of jets in e+e-
- fragmenting quark is combined with an anti-quark from a  $q\overline{q}$  pair created out of vacuum to give the "first meson" with energy fraction

The leftover quark (1-z energy fraction) is fragmented in the same way and so on until the energy is below the cut-off.

- gluon first splits in qq pair then the above schema is followed

#### - z is the fragmentation function

This model describes quite well  $e+e- \rightarrow two-jets$  and three-jets. Main issues: the fragmentation depends on parton energy this leads to a violation of momentum conservation that has to be adjusted at the end of the fragmentation. In addition, jets are too close in angle.

#### String Model

- quark and anti-quark move out in opposite direction losing energy to colour field which collapses into a string-like configuration
- the string breaks into hadron pieces producing  $q\overline{q}$  pair.
- gluons produce kinks on the string
- gluon splitting into qq produces an other string segment



 kinked strings fragmentation leads to an angular distribution of hadrons in e+e- events in a better agreement with data than the independent fragmentation model.

#### **Cluster Models**

- during the parton branching process we have the so-called "preconfinement of colour" → colour connected neighbouring partons have an asymptotic mass independent from the momentum and universal.
- colour-singlet clusters of partons form through non-perturbative splitting of gluon after the perturbative phase and later decay into particles



- gluons after the parton shower are splitted in  $q\overline{q}$  pairs

## Hadronization Models: MC generator

Monte Carlo programs use the three hadronization models to generate full events from parton shower. Independent fragmentation -ISAJET

String hadronization: - JETSET which is used by PYTHIA

Cluster hadronization:

- HERWIG
- SHERPA

### Jets: Introduction

#### Jet definition: examine a $e+e- \rightarrow jets$



Event in figure a) shows the classic two-jets events.

Event in figure b) is more complicate: it can be interpreted as in b), with  $q\bar{q}$  pair that emits an hard gluon or as in c) with an additional soft gluon Every time the events are reconstructed we should make this kind of inspection!

## Jets Algorithms

Jet definition starts solving two main questions:

- which particles are grouped together. How to group particles define the jet algorithm
- how to combine the momenta of particles inside the jet. This define the kinematics properties of the jet. Usually the 4-momenta of the particles are summed up.

#### Cone Algorithm

- Iterative process:
- 1. make a list of all particles and order them in transverse momentum
- 2. the highest in transverse momentum is the seed particle
- 3. draw a cone of radius R around the seed particle
- 4. calculate the sum of the momenta of all the particles in the cone and find the axis of the jet.

## Jets Algorithms: cone - 1

- 5. if the direction of the jet coincides with the initial one done! If not go back to 3, draw a new cone around the jet-axis and proceed to 4.
- 6. Repeat the process until the sum of the cone content coincides with the previous one.

The particles in the stable cone are removed from the list of particles in the event and the procedure starts again to search for a new jet. Major issue: the Pt ordering for seed particle, it is not collinear safe



Highest Pt particle emits a gluon and it is not the highest Pt particle generating 2 jets

## Jets Algorithms: cone - 2

Take all the particles above a given threshold as seed solve the problem of collinear safe but introduces the infrared safety issue: soft emitted particle can generate new stable cone close to two primary that then are merged



## Jets Algorithms:Kt

Sequential recombination algorithm For each pair of particle define a distance  $d_{ij}$ : where R is a parameter similar to the cone radius and  $d_{iB}$   $d_{iB} = p_{ti}^2$ 

The algorithm proceeds searching for the small d: if it is  $d_{ij}$  the particles i and j are recombined in one particle, if it is  $d_{iB}$  the particle i is called jet and removed from the list of particles. The procedure continues until the list of particles is empty.

Jets from Kt algorithm can be inspected inside and study the substructure of jet since the clustering sequence it is known.

## Jets Algorithms:Kt

Jets from Kt algorithm have irregular edges because many soft particle cluster together at early stage, in pattern that are almost random. The irregular edges is the reason why Kt is not so used, it is difficult to evaluate the acceptance.



### Jets Algorithms:anti-Kt

Sequential recombination algorithm with the "nice" cone properties by modifying the Kt algorithm:

$$d_{ij} = \frac{1}{\max(p_{ti}^2, p_{tj}^2)} \frac{\Delta R_{ij}^2}{R^2},$$
  
$$d_{iB} = \frac{1}{p_{ti}^2}.$$

Jets grow in concentric circle from the "core" until the reach the cone size R. It is collinear and infrared-safe. It does not provide information on sub-structure of jets.



## Jets Algorithms Comparison



Which jet algorithm use , which R depends on the physics measurement.

### Hadron Interaction

Cross section of an hard process in proton-proton collision



$$\sigma = \int dx_1 f_{q/p}(x_1) \int dx_2 f_{\bar{q}/p}(x_2) \hat{\sigma}_{q\bar{q} \to ZH}(x_1 x_2 s)$$
  
Hard X-section  
Parton distribution function

 $s = (p_1 + p_2)^2$  Center of mass energy xi= fraction of the proton momentum carried by the parton-i We will discuss how to measure the PDF

## Jet Production - 1

Cross section can be written as sum of terms

$$\frac{d^{3}\sigma}{dy_{3}dy_{4}dp_{T}^{2}} = \frac{1}{16\pi s^{2}} \sum_{i,j,k,l=q,\bar{q},g} \frac{f_{i}(x_{1},\mu^{2})}{x_{1}} \frac{f_{j}(x_{2},\mu^{2})}{x_{2}}$$
$$\times \overline{\sum} |\mathcal{M}(ij \to kl)|^{2} \frac{1}{1+\delta_{kl}}$$

Where:

i.j are the two incoming partons and k,l the outcoming ones.

 $\textbf{Y}_{_{3,4}}$  are the rapidity of the outcoming partons in the laboratory system.  $\mu$  is the scale

 $M(ij \rightarrow kl)$  the matrix element

### Jet Production - 2

	Process	$\overline{\sum}  \mathcal{M} ^2/g^4$	$\theta^* = \pi/2$
	$q q' \rightarrow q q'$	$\frac{4}{9}  \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$	2.22
(a)	$q \ \overline{q'}  o q \ \overline{q'}$	$\frac{4}{9}  \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2}$	2.22
ê ê	$q \ q  o q \ q$	$\frac{4}{9} \left( \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} + \frac{\hat{s}^2 + \hat{t}^2}{\hat{u}^2} \right) - \frac{8}{27} \frac{\hat{s}^2}{\hat{u}\hat{t}}$	3.26
	$q \ \overline{q}  ightarrow q' \ \overline{q'}$	$\frac{4}{9}  \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2}$	0.22
	$q \ \overline{q}  ightarrow q \ \overline{q}$	$\frac{4}{9} \left( \frac{\hat{s}^2 + \hat{u}^2}{\hat{t}^2} + \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2} \right) - \frac{8}{27} \frac{\hat{u}^2}{\hat{s}\hat{t}}$	2.59
Jee ge	$q \ \overline{q}  ightarrow g \ g$	$\frac{32}{27}  \frac{\hat{t}^2 + \hat{u}^2}{\hat{t}\hat{u}} - \frac{8}{3} \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2}$	1.04
(c)	$g \ g \  o q \ \overline{q}$	$\frac{1}{6}  \frac{\hat{t}^2 + \hat{u}^2}{\hat{t}\hat{u}} - \frac{3}{8} \frac{\hat{t}^2 + \hat{u}^2}{\hat{s}^2}$	0.15
le se servere reepes le se	$g \ q  o g \ q$	$-\frac{4}{9}  \frac{\hat{s}^2 + \hat{u}^2}{\hat{s}\hat{u}} + \frac{\hat{u}^2 + \hat{s}^2}{\hat{t}^2}$	6.11
source under and	$g \ g  o g \ g$	$rac{9}{2} \; (3 - rac{\hat{t}\hat{u}}{\hat{s}^2} - rac{\hat{s}\hat{u}}{\hat{t}^2} - rac{\hat{s}\hat{t}}{\hat{u}^2})$	30.4
(b)			

## Jets Cross Section vs. Et - 1

It is interesting to compare data and theory in :

- -Et distribution
- -jets angular distribution



Jet

### Jets Cross Section vs. Et - 2



- Final state partons are revealed through collimated flows of hadrons called jets
- Measurements are performed at hadron level & theory is parton level (hadron → parton transition will depend on parton shower modeling)
- Precise jet search algorithms necessary to compare with theory and to define hard physics

### Jets Reconstruction

 Reconstruct jets using one of the "jet algorithms" Required features in a jet finding algorithm: Detector independence: the performance of the jet algorithm should not be dependent on detector segmentation, energy resolution, ... Stability with luminosity: jet finding should not be strongly affected by multiple hard scatterings at high beam luminosities. Fast

*Efficient*: the jet algorithm should find as many physically interesting jets as possible

2) Need to correct for all the effects that do not guarantee the described criteria

# Jets Energy Correction

Jets energy must be corrected for:

Level 0 - "Online/Offline calibrations"

Covert the ADC counts in energy

#### Level 1 - "Eta-dependent"

Usually experiments cover regions in eta with different calorimetry The flow of particles changes as eta increases.

Level 2 - "Multiple Interactions"

Energy from different interactions falls inside the jet cluster increasing the measured energy. This additional energy evaluated using minimum bias events is subtracted

Level 3 - "Absolute"

The jet energy measured in the calorimeter needs to be corrected for any non-linearity and energy loss in the un-instrumented regions of each calorimeter.

# Jets Energy Correction

#### Level 4 - "Underlying Event"

The underlying event is defined as the energy associated with the spectator partons in a hard collision event. Depending on the details of the particular analysis, this energy needs to be subtracted from the particle-level jet energy.

The UE energy was measured from minimum bias data requiring events only one vertex.

#### Level 5 - "Out-of-cone"

It corrects the particle-level energy for leakage of radiation outside the clustering cone used for jet definition, taking the "jet energy" back to "parent parton energy".

### **Results on Jets Cross Section vs. Et**

After selecting events with at least two jets by mean of an unfolding procedure we can compare the inclusive jet cross section with the QCD expectations



## Jets angular distribution - 1

Jets angular distribution is sensitive to the form of  $2 \rightarrow 2$  matrix element in the parton-parton center of mass and to quark sub-structure. The point-like quarks produce:

$$\frac{d\,\sigma}{d\cos\theta^*} \approx \frac{1}{\sin^4\theta^*/2} \qquad \chi = \frac{1+\cos\theta^*}{1-\cos\theta^*} \qquad \frac{d\,\sigma}{d\,\chi} \approx constant$$

If quarks have a sub-structure the Lagrangian has to include:

 $L = \pm (g^2/2\Lambda^2(\bar{q}_L\gamma_\mu q_L)(\bar{q}_L\gamma^\mu q_L)),$  a contact color singlet term.

The coupling constant  $g^2/4\pi$ = 1 and 1/ $\Lambda$  is a measure of the quark size. This additional term will enhance the di-jets cross section around 90° in the di-jets center of mass. The amplitude is proportional to  $\hat{s}/\Lambda$  which increase with the jet-jet invariant mass. The experiment is sensitive to  $(\hat{s}/\Lambda)^2$ 

#### Jets angular distribution - 2



### Jets angular distribution - 3



Data in agreement with MC with quark without sub-structure

We can set a limit on the sub-structure coupling:  $\Lambda > 2.4$  TeV

### Hadron Interaction