Heavy Flavour Cross Sections Measurements

$$m_u \approx 3 \text{ MeV}$$

 $m_d \approx 5 \text{ MeV}$ very light m< Λ_{QCD}
 $m_s \approx 100 \text{ MeV}$
 $m_c \approx 1300 \text{ MeV}$ Flavours considered
 $m_b \approx 4200 \text{ MeV}$ very heavy

The leading-order process for the production of heavy quark Q of mass m in hadron collisions:

 $\begin{array}{ll} (a) & q(p_1) + \overline{q}(p_2) \to Q(p_3) + \overline{Q}(p_4) \\ (b) & g(p_1) + g(p_2) \to Q(p_3) + \overline{Q}(p_4) \end{array}$

Where the four momenta of the partons are given in brackets. The Feynman diagrams are:





The invariant matrix elements squared averaged over initial and final color and spin

$$\begin{array}{|c|c|c|c|c|} \hline \mathsf{Process} & \overline{\Sigma} |\mathcal{M}|^2 / g^4 \\ \hline q \ \overline{q} \to Q \ \overline{Q} & \frac{4}{9} \Big(\tau_1^2 + \tau_2^2 + \frac{\rho}{2} \Big) \\ \hline g \ g \to Q \ \overline{Q} & \Big(\frac{1}{6\tau_1 \tau_2} - \frac{3}{8} \Big) \Big(\tau_1^2 + \tau_2^2 + \rho - \frac{\rho^2}{4\tau_1 \tau_2} \Big) \end{array}$$

Where it has been introduced the notation:

$$\tau_1 = \frac{2p_1 \cdot p_3}{\hat{s}}, \ \tau_2 = \frac{2p_2 \cdot p_3}{\hat{s}}, \ \rho = \frac{4m^2}{\hat{s}}, \ \hat{s} = (p_1 + p_2)^2$$

The short-distance cross section is obtained from the invariant matrix element:

$$d\hat{\sigma}_{ij} = \frac{1}{2\hat{s}} \frac{d^3 p_3}{(2\pi)^3 2E_3} \frac{d^3 p_4}{(2\pi)^3 2E_4} (2\pi)^4 \delta^4 (p_1 + p_2 - p_3 - p_4) \overline{\sum} |\mathcal{M}_{ij}|^2.$$

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In terms of rapidity $y = \frac{1}{2} \ln((E + p_z)/(E - p_z))$ and of transverse momentum P_T the relativistically invariant space volume element of the final state heavy quark is :

$$\frac{d^3p}{E} = dy \ d^2p_T$$

The invariant cross section may be written at LO:

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$$\frac{d\sigma}{dy_3 dy_4 d^2 p_T} = \frac{1}{16\pi^2 \hat{s}^2} \sum_{ij} x_1 f_i(x_1, \mu^2) x_2 f_j(x_2, \mu^2) \overline{\sum} |\mathcal{M}_{ij}|^2$$

 x_1 and x_2 are fixed if transverse momenta and rapidity of the outgoing heavy quarks are known. In the CM of the incoming hadrons we can write

$$p_{1} = \frac{1}{2}\sqrt{s}(x_{1}, 0, 0, x_{1})$$

$$p_{2} = \frac{1}{2}\sqrt{s}(x_{2}, 0, 0, -x_{2})$$

$$p_{3} = (m_{T} \cosh y_{3}, p_{T}, 0, m_{T} \sinh y_{3})$$

$$p_{4} = (m_{T} \cosh y_{4}, -p_{T}, 0, m_{T} \sinh y_{4})$$

$$4$$

Applying the energy and momentum conservation

$$x_{1} = \frac{m_{T}}{\sqrt{s}} (e^{y_{3}} + e^{y_{4}})$$

$$x_{2} = \frac{m_{T}}{\sqrt{s}} (e^{-y_{3}} + e^{-y_{4}})$$

$$\hat{s} = 2m_{T}^{2} (1 + \cosh \Delta y).$$

With this notation the matrix elements

$$m_T = \sqrt{m^2 + p_T^2}$$
 transverse
mass of the
heavy quarks

 $\Delta y = y_3 - y_4$ rapidity difference between heavy quark

$$\overline{\sum} |\mathcal{M}_{q\overline{q}}|^2 = \frac{4g^4}{9} \Big(\frac{1}{1 + \cosh(\Delta y)} \Big) \Big(\cosh(\Delta y) + \frac{m^2}{m_T^2} \Big) , \quad \textbf{~costant}$$

$$\overline{\sum} |\mathcal{M}_{gg}|^2 = \frac{g^4}{24} \Big(\frac{8 \cosh(\Delta y) - 1}{1 + \cosh(\Delta y)} \Big) \Big(\cosh(\Delta y) + 2 \frac{m^2}{m_T^2} - 2 \frac{m^4}{m_T^4} \Big) \sim \exp(-\Delta y)$$

Low contribution at high Δy and dominant contribution for $\Delta y < 1$ Heavy quarks produced by light quark are more correlated in rapidity respect to those produced by gluon-gluon fusion.

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Applicability of Perturbation Theory

The propagators in the diagrams:

 $(p_1 + p_2)^2 = 2p_1 \cdot p_2 = 2m_T^2 (1 + \cosh \Delta y) ,$ $(p_1 - p_3)^2 - m^2 = -2p_1 \cdot p_3 = -m_T^2 (1 + e^{-\Delta y}) ,$ $(p_2 - p_3)^2 - m^2 = -2p_2 \cdot p_3 = -m_T^2 (1 + e^{\Delta y}) .$

Are off-shell by a quantity of the order of m^2 so the perturbation theory should be applicable.

This is valid until the mass m is larger of Λ_{QCD} .

The question is if the bottom and charm mass are large enough.

At NLO, $O(\alpha_s^3)$, the production cross section of the heavy flavor quark of mass m: $\sigma(S) = \sum_{i,j} \int dx_1 dx_2 \ \hat{\sigma}_{ij}(x_1 x_2 S, m^2, \mu^2) F_i(x_1, \mu^2) F_j(x_2, \mu^2)$

Where $\hat{\sigma}_{i,j}(\hat{s}, m^2, \mu^2) = \sigma_0 c_{ij}(\hat{\rho}, \mu^2)$ $\hat{\rho} = 4m^2/\hat{s}, \bar{\mu}^2 = \mu^2/m^2, \sigma_0 = \alpha_S^2(\mu^2)/m^2$

Examples of higher order diagrams



Real emission diagrams



Virtual emission diagrams

There are several dependences.

1) Scale, µ:

- PDF following the DGLAP equations
- running coupling constant
- short-distance cross section: if we perform a calculation to $O(\alpha_s^3)$, the variation of the scale contributes: $\mu^2 \frac{d}{d\mu^2} \sigma = O(\alpha_S^4)$.

The above variations combine in a such a way that the scale dependence is formally small because of higher order in α_s (α_s^4) This does not guarantee that the numerical value of the cross section is smaller for higher series when varying the scale.



LO cross section is almost scale independent because of α_s behavior and increased gluon distribution with μ NLO is almost 2xLO \rightarrow large uncertainties on the cross section Sept. 20, 2013 Dottorato 2013 9

2) Heavy quark mass m :

1.2 < m_c < 1.8 GeV

 $4.5 < m_{b} < 5.0 GeV$

- explicit dependence on $1/m^2$ in the short-distance cross section
- PDF, as m decreases the x value at which the PDF are calculated become smaller and the cross section increases because the parton flux increase
- α_s depends on the the scale μ and $\Lambda \quad \alpha_s(\mu^2) = \frac{1}{b_0 \ln(\frac{\mu^2}{\Lambda^2})}$ if we take m/2 < μ <2m we have problems $b_0 \ln(\frac{\mu^2}{\Lambda^2})$ with the charm because we arrive at μ < 1 GeV where the perturbation theory is not valid \rightarrow for charm the lower limit for $\mu = 2m_c$

Heavy Quarks Fragmentation

Heavy quarks after the production fragment in hadrons. The model is different of those used for light quarks the attachment of a light quark to and heavy one Q produce a small deceleration of the heavy quark Q.



Heavy Quarks Fragmentation

An heavy guark Q of momentum P generates a hadron H=Qg of momentum zP. To model this process the energy difference before and after the fragmentation is needed

$$\Delta E = E_Q - E_H - E_q = \sqrt{m_Q^2 + P^2} - \sqrt{m_H^2 + z^2 P^2} - \sqrt{m_q^2 + (1 - z)^2 P^2}$$

$$\approx \frac{m_Q^2}{2P} \left[1 - \frac{1}{z} - \frac{\epsilon_Q}{1 - z} \right] \quad \text{with} \quad \epsilon_Q = \frac{m_q^2}{m_Q^2} \quad \text{and} \quad m_H = m_Q$$

The transition amplitude is $T \sim \frac{1}{\Delta E}$, squaring the amplitude and including a factor 1/z for phase space we obtain the Peterson function for the heavy quark fragmentation

$$D_{Q}^{H}(z) = \frac{N_{H}}{z} \left[1 - \frac{1}{z} - \frac{\epsilon_{Q}}{1 - z} \right]^{-2}$$

 N_{μ} is a normalization factor

$$\sum \int dz \, D_Q^H(z) = 1$$

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Heavy Quarks Fragmentation



$$\epsilon_{Q} = \frac{m_{q}^{2}}{m_{Q}^{2}}$$

is determined by the ratio of quark masses but it is treated as parameter and the best value is obtained from data.

b and c Meson Decay



Several different decay modes of the b meson based on the spectator Model where the light quark does not participate.

B can be selected based on:

- lepton (e, μ): B \rightarrow lvD
- D meson: $B \rightarrow D\pi$
- J/ψ : $B \rightarrow J/\psi K$

c Meson Decay



Similar diagram governs the charm decay. The procedure to identify charm meson are:

- lepton (e,µ): $D \rightarrow lvK(\pi)$
- K meson: $D \rightarrow K(n)\pi$

b Meson Cross Sections Measurements

The procedure to measure the cross section is simple.

$$\sigma = \frac{N_{Data} - N_{Background}}{Acc \int Ldt}$$

B-mesons are selected exploiting the decay channels. The selection procedure depends on the decay channel as the background evaluation. Examples:



b Meson Cross Sections History

Until 2002 data and theory had a discrepancy, the measured cross section was higher of about factor 3 New Physics?



b Meson Cross Sections Measurements

A lot of work done by the experiments to improve the measurements. A lot of work done by theoreticians to improve the theory: M.Cacciari and P.Nason, PRL 89, 122003 (2002)

new calculation of the cross section to include corrections (instead of NLO NLL) at high order

3

- new tuning of the fragmentation function D(z)
- new PDF

The purpose of this Letter is precisely to implement correctly the effect of heavy quark fragmentation in the QCD calculation. Several ingredients are necessary in order to do this: (i) A calculation with resummation of large transverse momentum logarithms at the next-to-leading level (NLL) should be used for heavy quark production [21], in order to correctly account for scaling violation in the fragmentation function. (ii) A formalism for merging the NLL resummed results with the NLO fixed order calculation (FO) should be used, in order to account properly for mass effects [22]. This calculation will be called FONLL in the following. (iii) A NLL formalism should be used to extract the nonperturbative fragmentation effects from e^+e^- data [23–29].



FIG. 4 (color online). The effect of the different ingredients in the calculation presented in this work, normalized to a fixed order calculation with Peterson fragmentation and $\epsilon = 0.006$. Dashed line: FO, $\epsilon = 0.002$; dotted line: FONLL, $\epsilon = 0.002$; solid line: FONLL, N = 2 fit.

b Meson Cross Sections Measurements



Correlated b-b Cross Section Measurements

b-quark can be identified in jets by using inclusive selections. This allow to reconstruct events with 2 b-jets.

b-b cross section measurement allow to test high order theoretical contributions



LO produced almost back-to-back

Fitting the cross section as function of the angular separation allow to determine the relative contribution of each process

• $\Delta \Phi$ between 2 b-jets

Correlated b-b Cross Section Measurements

Tevatron:

 2μ are required then their impact parameter distribution is fitted to extract c and b components



Correlated b-b Cross Section Measurements

LHC:

ATLAS and CMS identify jets with b exploiting the long b lifetime

100

200

B-tagging: 2 or 3 tracks displaced from the primary vertex the decay length L_{xv} compatible

with the distance traveled by the b-hadron.





Inclusive charm cross section

Identify only one c-meson and measure the cross section with the same procedure described for b-mesons.

Theory predictions have larger uncertainties than the b-meson cross Section.

Charm meson cross section measured in several experiments, fixed target and at collider.



Inclusive charm cross section

Also in this case a lot of work done by theoreticians Charm cross sections for the Tevatron Run II Journal of High Energy Physics Volume 2003 JHEP09(2003)

- Use the same framework of the b-meson
- Build new fragmentation functions non-perturbative using data; Ex. $F(c \rightarrow D^0) = F_p(c \rightarrow D^0) + F(c \rightarrow D^{*+}) \otimes F(D^{*+} \rightarrow D^0) + F(c \rightarrow D^{*0}) \otimes F(D^{*+} \rightarrow D^0)$ $F(c \rightarrow D^0)$ = directly produced D⁰ fragmentation function $F(c \rightarrow D^{0^*})$ = fragmentation function of D^{0*} that then decay to D⁰ $F(c \rightarrow D^{**})$ = fragmentation function of D^{**} that then decay to D⁰



Inclusive charm cross section



Now at LHCb

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Charm Correlated Cross Sections Measurements



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Charm Correlated Cross Sections Measurements



- Identify the 2 D meson
- Correct for D coming from
 b-hadron
- Evaluated the efficiencies

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Top Quark Introduction

The last quark discovered. Precision SM measurements predict its existence and its mass.

In particular the asymmetry backward-forward of b-jets produced in e+e- annihilation at the Z resonance can be easily explained assuming that the b quark is in an SU(2) doublet with the top quark Precision electroweak fits constrained the mass: 178^{+8+17}_{-8-20} GeV

The top discovery dates 1995 by the two experiments at the Tevatron Collider.

We are now in the era of precision top measurements



Top Quark Cross Sections

$$\sigma(pp \to t\bar{t} + X) = \sum_{i,j} \int dx_i dx_j \times F_i(x_i,\mu) F_i(x_j,\mu) \hat{\sigma}_{ij}(x_i,x_j,m_{top}^2,\mu^2)$$

 $m_{_{top}}/2 < \mu < 2m_{_{top}}$ since the mass is so large the calculation can be performed with the perturbative QCD

At LO the diagrams that contribute are



LHC: 80% gluon fusion 20% $q\overline{q}$ Tevatron: 85% $q\overline{q}$ 15% gluon fusion

NLO calculations available.

Top Quark Cross Sections high order

NLO calculations are important: ~50%

Since not everything is in agreement with the theoretical expectations theoreticians are calculating also the NNLO corrections



Top Quark Decay

Quark top decay before it can form a bound state



Top Quark Reconstruction



Events classified depending on the W decay:

- Di-lepton: low yield, low background, well defined leptonic signature, neutrinos → MET
- Lepton+jets: higher yield, moderate background, lepton signature + MET + jets
- All hadronic: highest yield, huge background, only jets

Top Quark Events Reconstruction: Common tools

Final states always with jets and b-quark in jets.

- 1. Reconstruct jets
- 2. Use b-tag algorithm to determine if the jet is originated by a b-quark



Jet Energy Scale (JES) is one of the major source of uncertainty (see discussion on jet reconstruction) Top analysis now use a new method to determine the energy scale: the "in situ" calibration.

Common Tools: "In situ" Energy Calibration

In the decay channels where both Ws decay in hadrons it is possible to leave the JES as free parameter and fit the W mass. Templates with different JES are produced and the W mass is fitted



Top Quark Reconstruction: Common tools

2. Use b-tag algorithm to determine if the jet is originated by a b-quark



- Select tracks with high impact parameter respect to primary vertex
- Request at least 2 tracks
- Fit the tracks to identify a secondary vertex
- Cut on decay lenght L_{xy} to be compatible with the distance traveled by a b-hadron

Top Quark Decay Selections



Requirements:

- two high P_T opposite charge isolated leptons
- > at least 2 high E_{τ} jets
- at least one vertex b-tag
- Significant MET

Major Backgrounds

Process with 2 leptons in the final state: Drell-Yan Z/γ*, WW,WZ,ZZ
 QCD: fake leptons



Requirements:

- \succ one high P_{τ} isolated leptons
- > at least 4 high E_T jets
- ➤ at least one b-tag
- Significant MET

Major Background

- Process with 1 lepton + jets in the final state: W+jets
- Other contributions from non-W

Top Quark Decay Selections



Requirements:
> at least 6 high E_T jets
> at least one b-tag
> Small MET
> No leptons
Dominant Background: QCD multi-jets



Top Quark Event count

In order to count the number of top-anti-top event candidates the number of events is plotted versus the n umber of jets per event. In each bin the contribution of signal and background is different.



Top Quark Event count - 2

In order to increase the purity of the sample the number of b-tagged jets are counted or at least 2 b-jets are required.



Top Quark Cross Section



Inserting the number of signal and background events in the formula and knowing luminosity and efficiency on signal we have the cross section



Good agreement with the expectations

Single Top Quark

Top can be produced also via electroweak interaction involving a vertex Wtb. There are three different production models depending on the Q^2 of the W:

- 1. t-channel: a virtual W-boson interact with b-quark (sea quark) (a)
- 2. s-channel: a virtual W boson $q^2 (m_{top} + m_b)^2$ is produced by the fusion

of 2 quark of SU(2) isospin doublet (b)

3. W-associated production: top quark is produced with a real W-boson starting from a sea b-quark and gluon (c)





N. Kidonakis, DIS 2011, Newport News, Virginia, April 2011



PRD74,114012,(2006)



Single top cross section: Wt associated production

Not enough sensitivity at Tevatron

