



$|q/p|$ Measurement from $B^0 \rightarrow D^{}V$*

Partial Reconstruction

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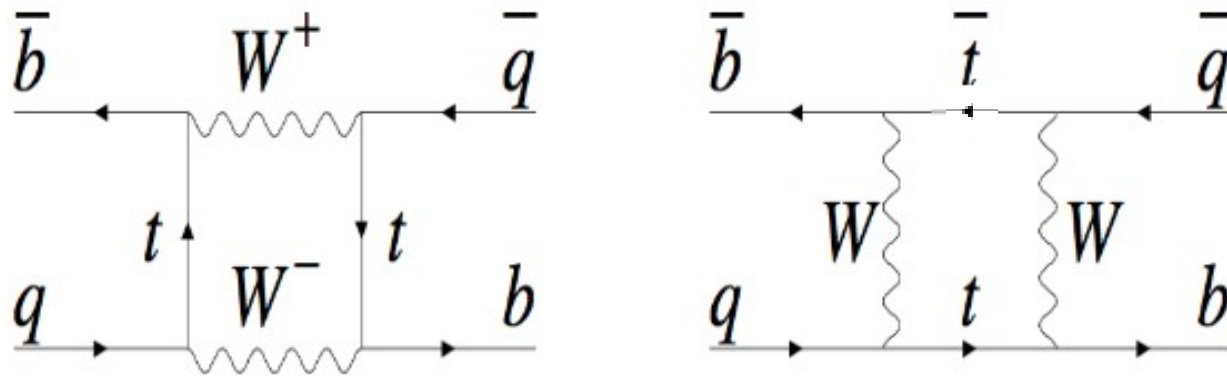
(on behalf of the BaBar Collaboration)

- Motivation
- Analysis Method
- Validation on MC
- Real Data Results
- Systematic Uncertainties
- Conclusions



Motivation

CPV in B^0 mixing



• New Particles in the boxes could modify SM expectations

• $B_q^0 - \bar{B}_q^0$ oscillations & decay governed by an Effective Hamiltonian:

$$i \frac{d}{dt} \begin{pmatrix} B_q \\ \bar{B}_q \end{pmatrix} = \left[\begin{pmatrix} M_{11}^q & M_{21}^{q*} \\ M_{21}^q & M_{11}^q \end{pmatrix} - \frac{i}{2} \begin{pmatrix} \Gamma_{11}^q & \Gamma_{21}^{q*} \\ \Gamma_{21}^q & \Gamma_{11}^q \end{pmatrix} \right] \begin{pmatrix} B_q \\ \bar{B}_q \end{pmatrix}$$

$[M_{ij}^q]$ = mass matrix

$[\Gamma_{ij}^q]$ = decay matrix

• Physical Eigenstates with defined masses and widths:

$$|B_q^{L,H}\rangle = \frac{1}{\sqrt{1 + |(q/p)_q|^2}} (|B_q\rangle \pm (q/p)_q |\bar{B}_q\rangle)$$

→ If $|(q/p)_q| \neq 1$ they would be also CP Eigenstates

• Neglecting $o(m_b^2/M_W^2)$:

$$\Delta m_q = m_H - m_L = 2 |M_{12}^q|; \Delta \Gamma_q = \Gamma_L - \Gamma_H = 2 |\Gamma_{12}^q| \cos \phi$$

$$\phi = \arg(-M_{12}^q / \Gamma_{12}^q) \quad \text{CP violating phase}$$

CPV in B^0 mixing

- $\Upsilon(4S)$ machines & Hadron Colliders: b quarks produced mainly in $b\bar{b}$ pairs

→ CP Asymmetry (time-independent):

$$A_{CP} = \frac{\text{Prob}(\bar{B}^0 \rightarrow B^0, t) - \text{Prob}(B^0 \rightarrow \bar{B}^0, t)}{\text{Prob}(\bar{B}^0 \rightarrow B^0, t) + \text{Prob}(B^0 \rightarrow \bar{B}^0, t)} = \frac{N(B^0 B^0) - N(\bar{B}^0 \bar{B}^0)}{N(B^0 B^0) + N(\bar{B}^0 \bar{B}^0)}$$

- Experimentally: measure charge asymmetry in mixed semileptonic B^0 decays:

$$A_{SL} = \frac{N(\ell^+ \ell^+) - N(\ell \ell)}{N(\ell^+ \ell^+) + N(\ell \ell)} = \frac{1 - |q/p|^4}{1 + |q/p|^4} = \frac{|\Gamma_{12}^q|}{|M_{12}^q|} \sin \phi$$

→ CPV in mixing if:

$$A_{SL} \neq 0 \leftrightarrow |q/p| \neq 1 \leftrightarrow \Phi \neq 0$$

Standard Model predicts

(Lenz, Nierste, arXiv:1102.4274 (2011)):

$$\bullet B_d: A_{SL}^d = (-4.1 \pm 0.6) 10^{-4}$$

$$\Phi_d = -4.3^\circ \pm 1.4^\circ$$

$$\bullet B_s: A_{SL}^s = (1.9 \pm 0.3) 10^{-5}$$

$$\Phi_s = 0.22^\circ \pm 0.06^\circ$$

Beyond Standard Model

- New Physics could modify M_{12}^q and A_{SL} leaving Γ_{12}^q unchanged:

$$M_{12}^{NP, q} = M_{12}^{SM, q} \Delta_q; \Delta_q = |\Delta_q| e^{i\phi_q^\Delta}$$

$$A_{SL}^{NP} = \frac{|\Gamma_{12}^q|}{|M_{12}^{SM, q}|} \frac{\sin(\phi_q^{SM} + \phi_q^\Delta)}{|\Delta_q|}$$

CPV in B^0 mixing

- HFAG average of $\Upsilon(4S)$ results
(arXiv:1207.1158v1 (2011)):

$$|q/p|_d = 1.0002 \pm 0.0028$$

$$A_{SL}^d = (-0.05 \pm 0.56)\%$$

In agreement with SM

- Hadron Colliders experiments measure a combination of B^0_d & B^0_s CP parameters:

$$A_{SL}^b = C_d A_{SL}^d + C_s A_{SL}^s$$

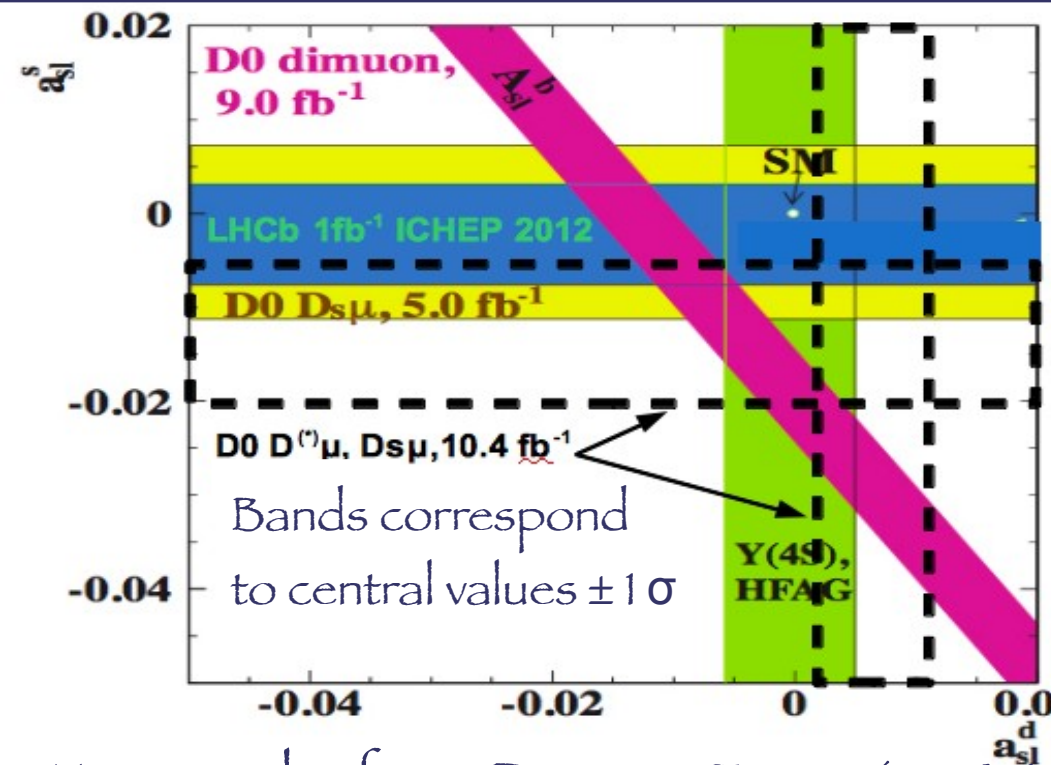
→ $C_{d,s}$ depend on $B^0_{d,s}$ production rates & mixing probability

- SM predicts:

$$A_{SL}^b = (-0.028^{+0.005}_{-0.006})\%$$

- D0 result on charge Asymmetry of like-sign dimuons differs by 3.9σ from SM expectation (Phys. Rev. D 84, 052007 (2011)):

$$A_{SL}^b = (-0.787 \pm 0.172 \pm 0.093)\%$$



- New results from Beauty-Factories & LHCb will help to understand the tension

Analysis Method

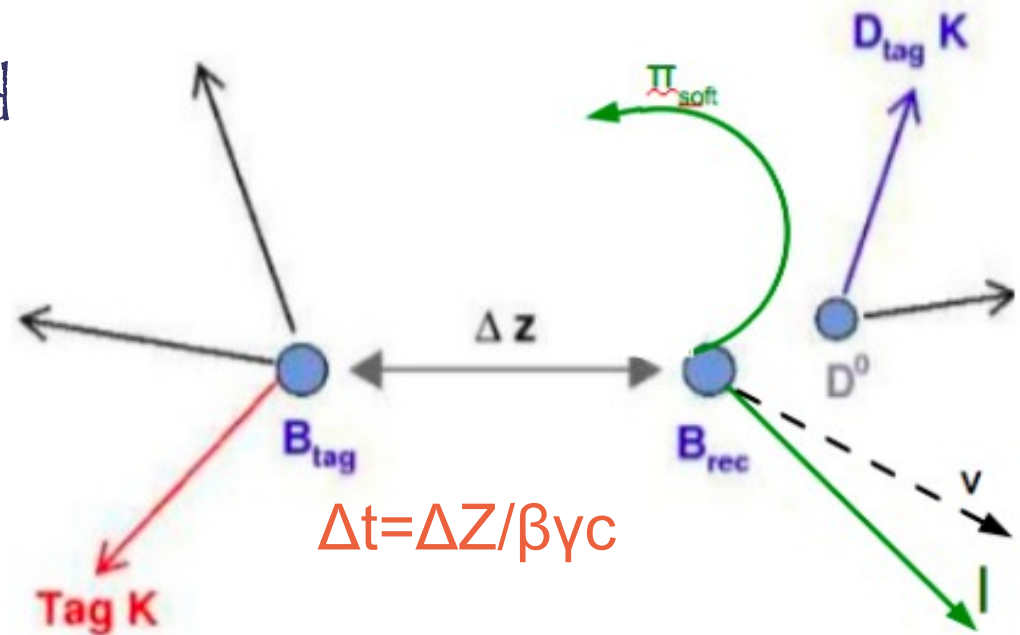
Analysis Method

- Semileptonic Asymmetry measured from Partially Reconstructed $B^0 \rightarrow D^* l \nu$ and K Tag

- P.R. B^0 flavor from lepton charge

- Tag B^0 flavor from K charge

- Tag B vertex from K track extrapolation to the e^+e^- Interaction Region



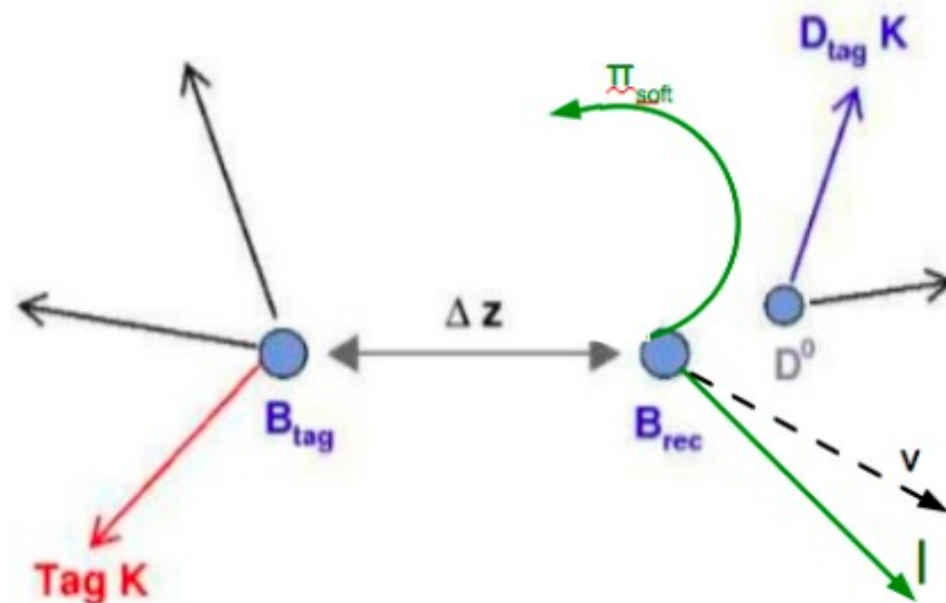
$$A_{SL} \approx \frac{N(l^+ K_T^+) - N(l^- K_T^-)}{N(l^+ K_T^+) + N(l^- K_T^-)}$$

- $|q/p|$ obtained using an Extended Maximum Likelihood Binned fit to the Δt & $\cos(\theta_{K-\text{Lepton}})$ distributions of the 4 subsamples:

Unmixed ($l^- K^+$, $l^+ K^-$); Mixed ($l^+ K^+$, $l^- K^-$) using a BLIND Approach

Partial Reconstruction

- P. R. of $B^0 \rightarrow D^* l \nu$ already exploited in several measurements (τ_{B^0} , Δm , ...)
- **Reconstruct only lepton & π_{soft} with opposite charge**
- Signal selection using missing squared neutrino mass with the approximation of B at rest in the $Y(4s)$ frame
- D^* 4-momentum estimated from π_{soft} kinematics
- Sample composition from a fit to M^2_{ν} by floating D^* , D^{**} and Combinatorial using MC shapes and Continuum shape from Off-Peak events
- Residual Peaking ($D^* \tau \nu$, $D^* D_s X$, $D^* h$) fixed to simulation

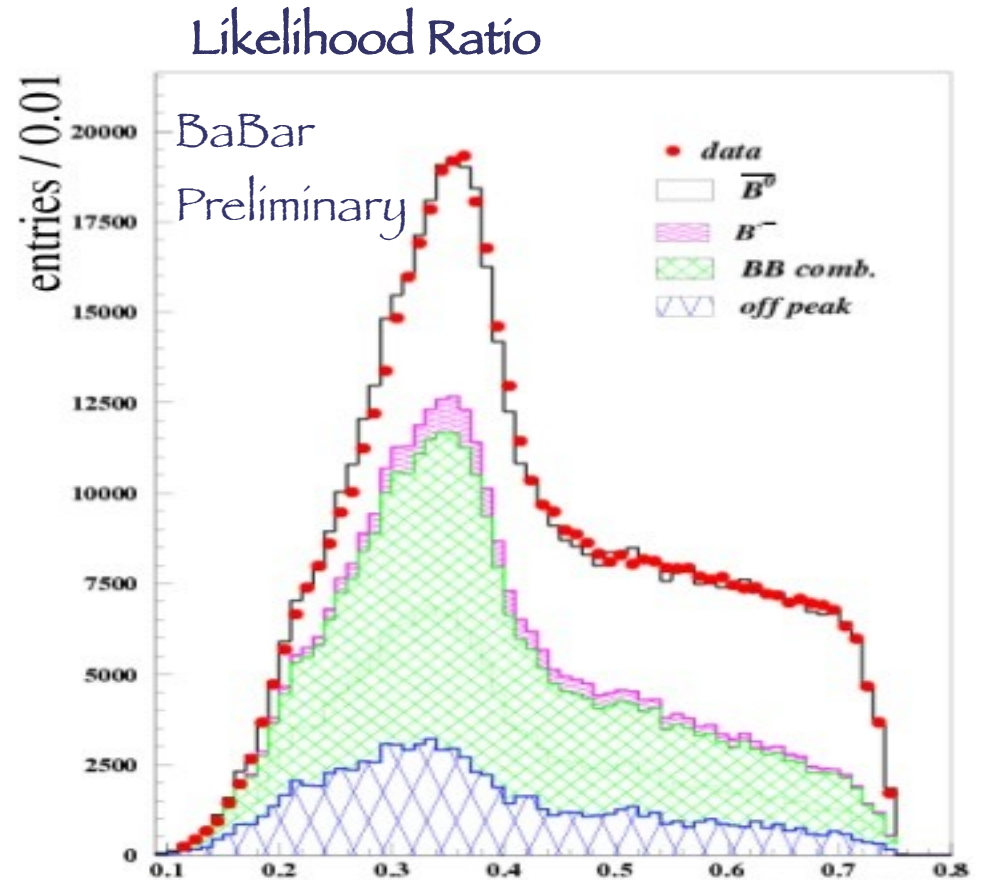


$$\mathcal{M}_\nu^2 \equiv (E_{\text{beam}} - E_{D^*} - E_\ell)^2 - (\vec{p}_{D^*} + \vec{p}_\ell)^2$$

Selection and Tagging

- Full BaBar statistics of 425.7 fb^{-1} analyzed
- $0.06 \text{ GeV}/c < P_{\pi_{\text{soft}}} < 0.19 \text{ GeV}/c$; $1.40 \text{ GeV}/c < P_{e/\mu} < 2.30 \text{ GeV}/c$

• Best lepton π_{soft} pair per event chosen exploiting Likelihood Ratio η ($P_l, P_{\pi_{\text{soft}}}$, Vertex Probability)



η

9

Selection and Tagging

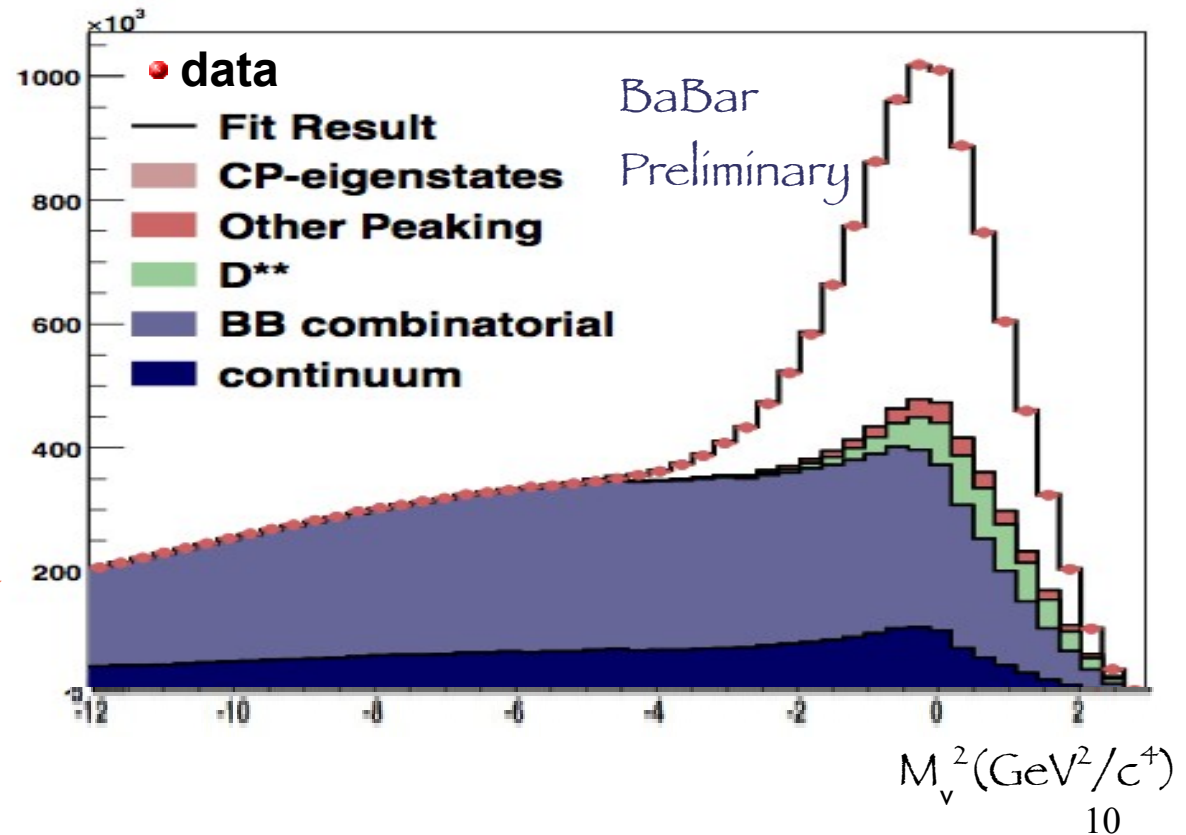
- K selection by means of energy loss & Cherenkov detector information;

$$P_K > 0.2 \text{ GeV}/c$$

- Continuum and Combinatorial BKG suppressed by means of Event Shape variables & Vertex Probability

→ 14×10^6 events selected with
Signal Purity $\sim 30\%$ in the
range:

$$-10 \text{ GeV}^2/c^4 < M_v^2 < 2.5 \text{ GeV}^2/c^4$$



K-Tagging Categories

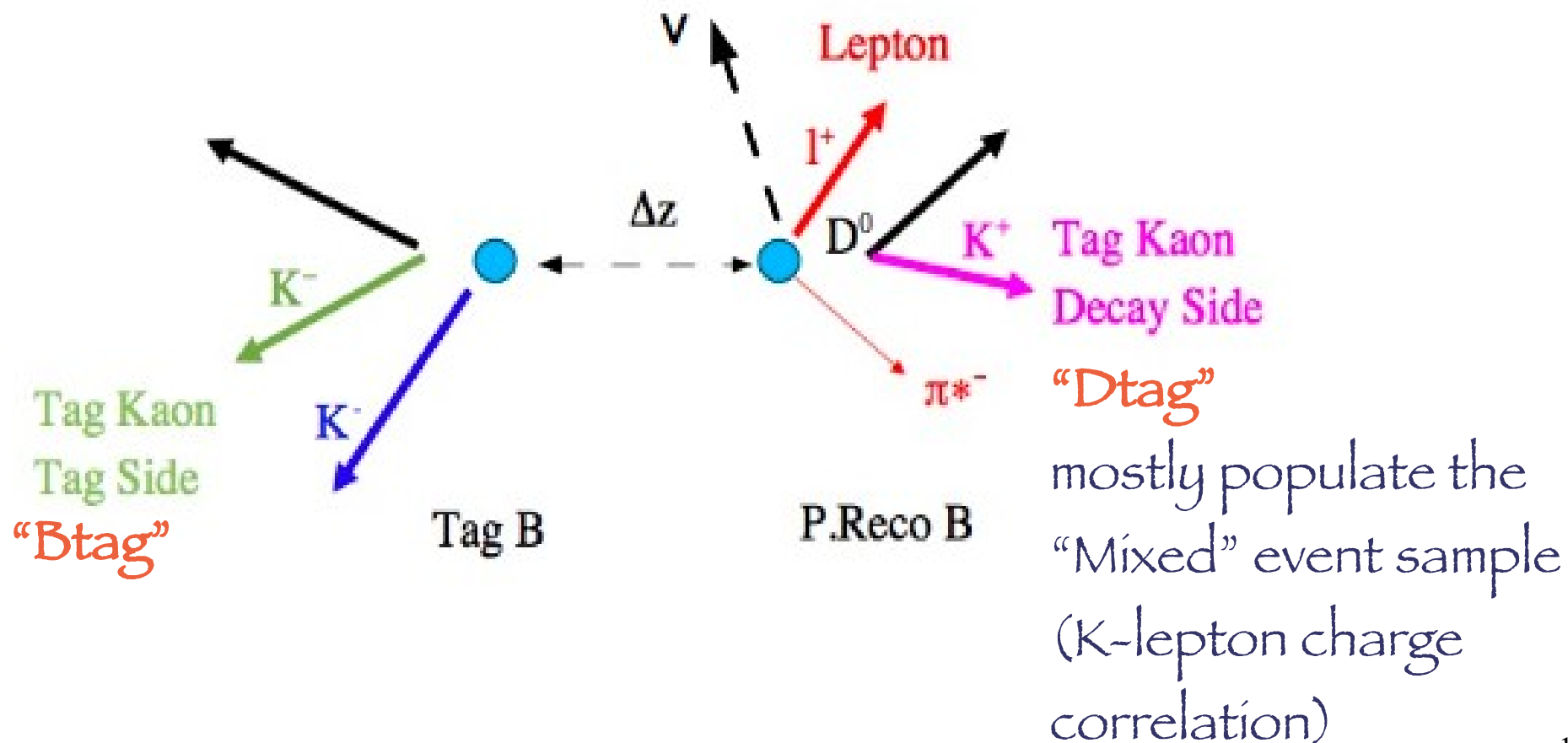
Tagging Kaon Sample: $\left\{ \begin{array}{l} b \rightarrow K + b \rightarrow c \rightarrow K \\ D^0 \rightarrow K \end{array} \right.$

From tag B

“Btag”

From decay B

“Dtag”



PDF Description: Btag

- Signal B^0 Btag PDF for Positive Mixed (l^+K^+) sample, (similar expressions apply for the other ones):

$$\mathcal{F}_{\text{signal}}(\Delta t, s_t, s_m) = \frac{\Gamma}{2(1+r'^2)} e^{-\Gamma|\Delta t|} \left| \frac{p}{q} \right|^2 \left[\left(1 + \left| \frac{q}{p} \right|^2 r'^2 \right) \cosh(\Delta\Gamma\Delta t/2) - \left(1 - \left| \frac{q}{p} \right|^2 r'^2 \right) \cos(\Delta m_d \Delta t) + \left| \frac{q}{p} \right| (b+c) \sin(\Delta m_d \Delta t) \right]$$

- r' , b , c : parameters resulting from interference between Cabibbo-Favoured and Doubly Cabibbo-Suppressed decays on the tag side

Assumptions:

- $\Delta\Gamma=0$
- b , c are treated as effective parameters due to strong correlation with resolution function
 - Only $|q/p|$ is measured

$$\begin{aligned} r' &= \left| \bar{\mathcal{A}}_{DCS} / \mathcal{A}_{CF} \right| \\ b &= 2r' \sin(2\beta + \gamma) \cos \delta' \\ c &= -2r' \cos(2\beta + \gamma) \sin \delta' \\ \delta' &= \text{Strong Phase} \end{aligned}$$

PDF Description: Btag

• In Real Life Physics & Detector effects have to be taken into account:

• Physics

→ Mistag, depending on P_K :

$$\omega^+ = \text{Prob}(B^0 \rightarrow K^-), \omega^- = \text{Prob}(\bar{B}^0 \rightarrow K^+), \Delta\omega = \omega^+ - \omega^-, \omega = (\omega^+ + \omega^-)/2$$

• Detector

→ Reconstruction Asymmetry:

$$\rho = \epsilon(l^+, \pi^-), \bar{\rho} = \epsilon(l^-, \pi^+)$$

$$A_{rec} = (\rho - \bar{\rho}) / (\rho + \bar{\rho})$$

→ Tagging Asymmetry, depending on P_K :

$$\tau = \epsilon(K^+), \bar{\tau} = \epsilon(K^-)$$

$$A_{tag} = (\tau - \bar{\tau}) / (\tau + \bar{\tau})$$

→ Δt Resolution

PDF Description: B_{tag}

- Modified PDF for Positive Mixed (l^+K^+) sample including Mistag & Detector Asymmetries, (similar expressions apply for the other ones):

$$\begin{aligned} \mathcal{F}_\chi^{meas}(\Delta t, s_t = 1, s_m = -1) &= \rho\tau \left[(1 - \omega_\chi^+) \mathcal{F}_\chi(\Delta t, 1, -1) + \omega_\chi^- \mathcal{F}_\chi(\Delta t, -1, 1) \right] = \\ &= RT(1 + A_{rec})(1 + A_{tag}) \left[(1 - \omega_\chi^+) \mathcal{F}_\chi(\Delta t, 1, -1) + \omega_\chi^- \mathcal{F}_\chi(\Delta t, -1, 1) \right] \end{aligned}$$

$$R = (\rho + \bar{\rho})/2$$

$$T = (\tau + \bar{\tau})/2$$

B_{rec} is a	B_{tag} is a	s_t	s_m
B^0	B^0	1	-1
\bar{B}^0	B^0	1	1
B^0	\bar{B}^0	-1	1
\bar{B}^0	\bar{B}^0	-1	-1

- Observed PDFs are obtained from the convolution of the modified PDFs with a resolution function (sum of Gaussians convolved with exponentials)

PDF Description: Dtag

- Dominant BKG in Mixed events: *shows single-tag semileptonic asymmetry*

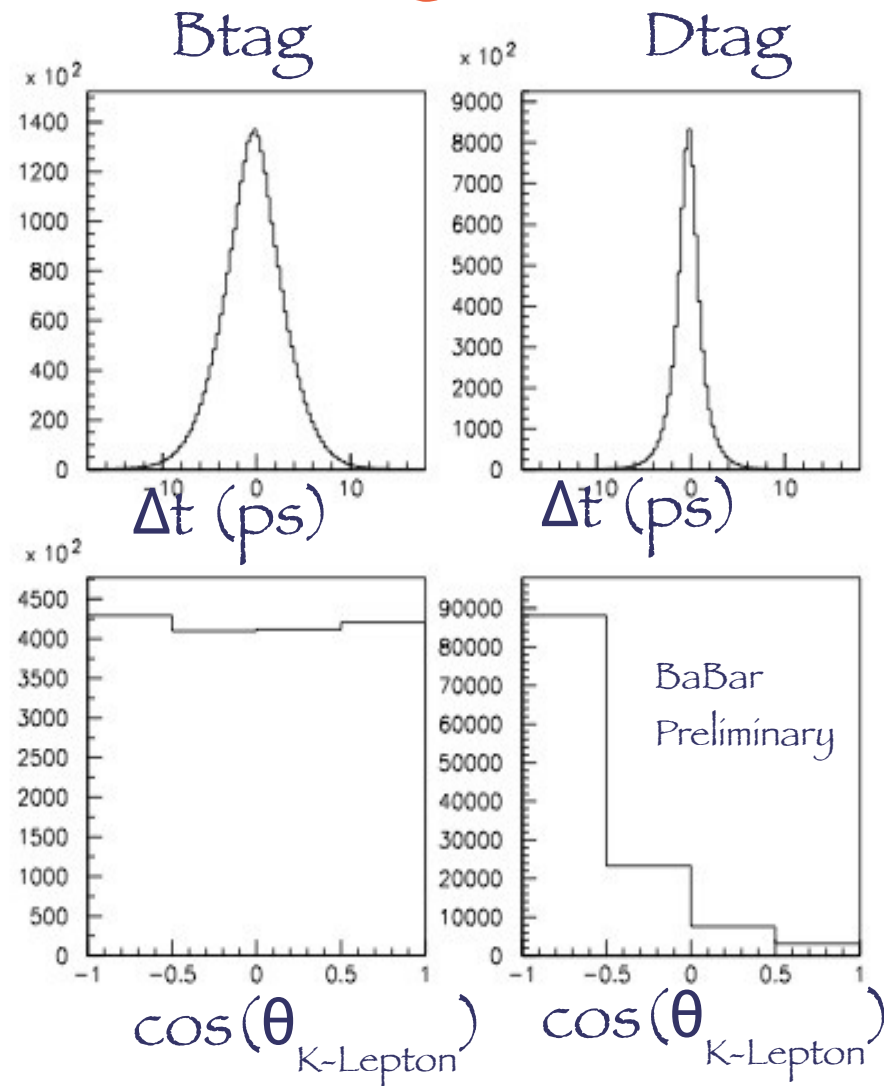
- F_{Dtag} floated by exploiting the different Δt & θ (K-Lepton) distributions wrt Btag events in different P_K bins

- Dtag fraction in B^+ events constrained to B^0 using simulation informations:

$$F_{Dtag}^{B^+} = R_{MC}(P_K) * F_{Dtag}^{B^0}$$

- $\cos(\theta_{K-Lepton})$ PDF from MC

- Δt PDF from a High Purity selection on Real Data (Dtag Purity $\sim 95\%$)



PDF Description: Dtag

Dtag Δt shape from a High Purity selection, two alternative strategies:

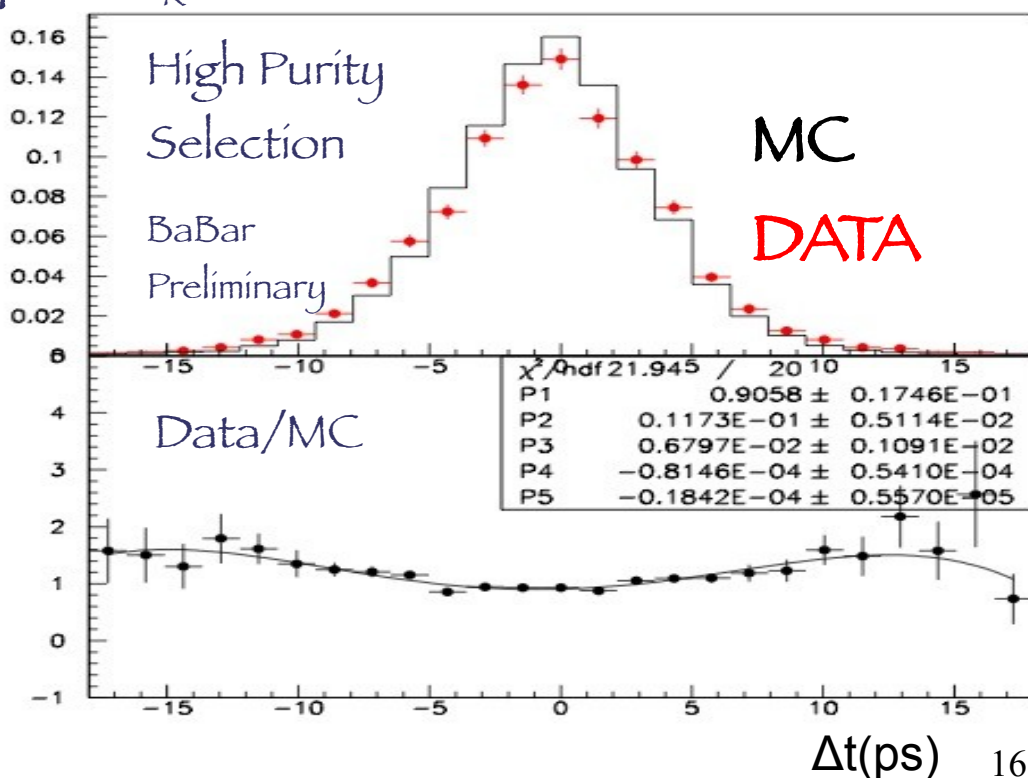
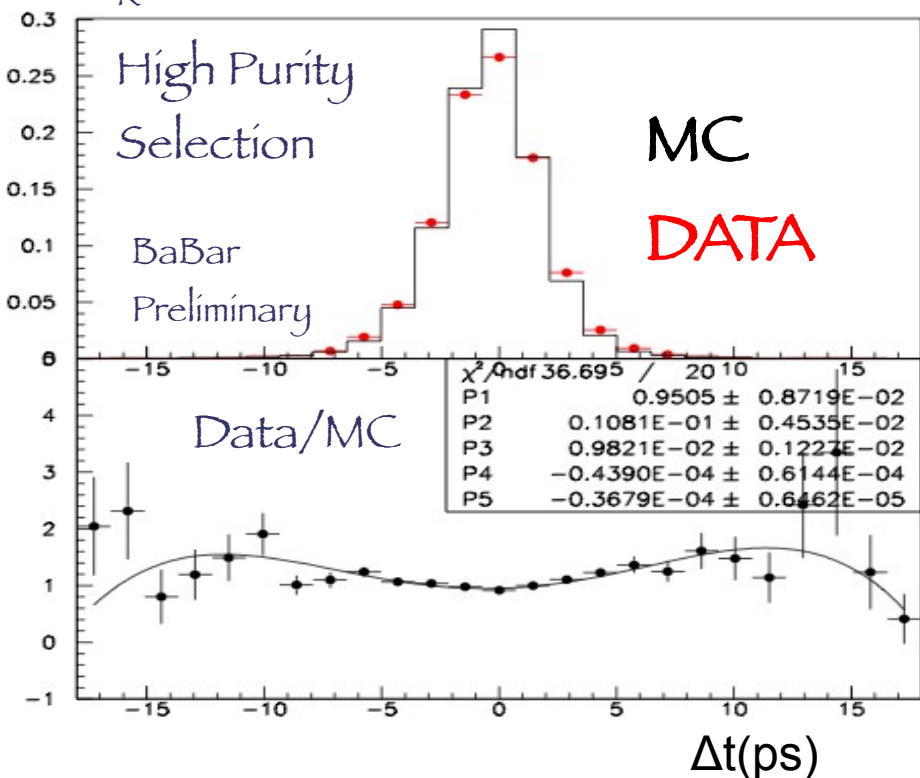
1) $PDF^{DATA} = PDF^{DATA}$
High Purity Selection

2) $PDF^{DATA} = PDF^{MC} \times (PDF^{DATA} / PDF^{MC})$
High Purity Selection

• Data/MC Corrections computed in bin of $(P_K, \sigma\Delta t)$

$P_K = [0.2, 0.52] \text{ GeV}/c, \sigma\Delta t = [1.2, 1.8] \text{ ps}$

$P_K = [0.2, 0.52] \text{ GeV}/c, \sigma\Delta t = [2.4, 3.0] \text{ ps}$



PDF Description: BKG Samples

- B^0 Combinatorial PDF similar to Signal one with effective τ_{B^0} , Δm , same A_{sl} and A_{tag} , different A_{rec} , m_{stag} and resolution parameters.
- B^+ decays parameterized by exponential functions and same resolution model as for B^0 decays.
- Continuum modeled with an exponential with effective lifetime obtained by a simultaneous fit to Off-peak data.
- About 1% of selected events originate from B^0 decays to CP-eigenstates (mostly $D^*D^{(*)}$)

→ Described by:

$$\mathcal{F}_{CP-eigen} = \frac{\Gamma}{4} e^{-\Gamma|\Delta t|} [1 \pm S_{eff} \sin(\Delta m_d \Delta t) \pm C_{eff} \cos(\Delta m_d \Delta t)]$$

→ S_{eff} & C_{eff} obtained from the simulation

+ : P.R. B^0
- : P.R. \bar{B}^0

Detector Asymmetry determination

- Crucial Issue: discriminate between Physical & Detector charge asymmetry **without relying on control samples**
- Different sub-samples (B^0 , B^+) \times (Peaking, BKG) \times (Btag, Dtag) share Physical and/or Detector Asymmetries in different combinations.
- **Strategy: disentangle the Physical and Detector Asymmetries by exploiting all the available information from different sub-samples.**

Detector Asymmetry determination

- Observed Asymmetry in the different subsamples:

	B^0	B^+
P.R. evts (Tag+Untag)	$A_{rec} + A_{sl} * x_d$	A_{rec}
Btag	$A_{rec} + A_{tag}(P_K) + A_{sl}$	$A_{rec} + A_{tag}(P_K)$
Dtag	$A_{rec} + A_{tag}(P_K) + A_{sl} * x_d$	$A_{rec} + A_{tag}(P_K)$

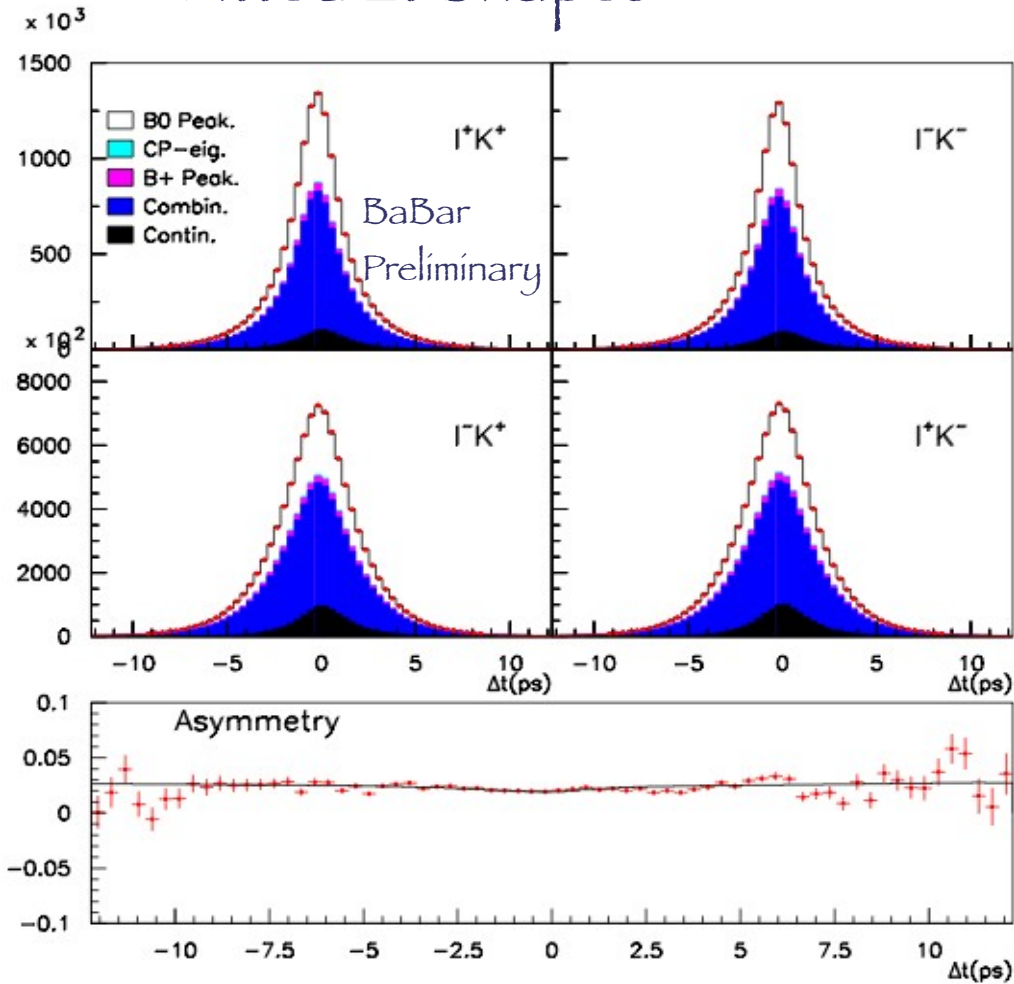
B^+ e Dtag BKG samples are useful in the $|q/p|$ measurement!

MC Validation

Monte Carlo Results

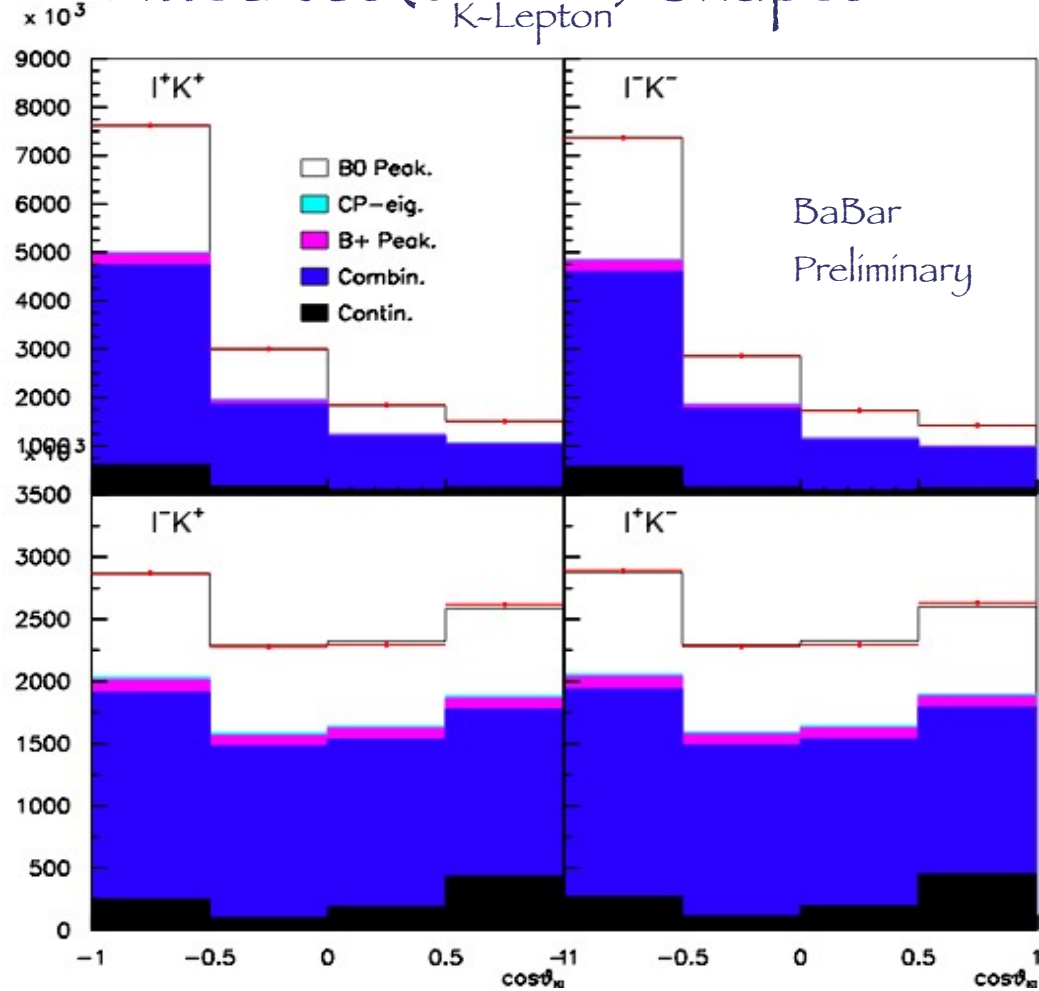
B^0+B^+ Continuum MC Fit

Fitted Δt Shapes



Raw $N(I^+K^+)/N(I^-K^-)$ Asymmetry

Fitted $\cos(\theta_{K\text{-Lepton}})$ Shapes



Monte Carlo Results

- Continuum generated with a Parameterized MC using as input the Off-Peak data sample relevant distributions and normalized to the MC statistics.
- Resolution parameters obtained using an iterative procedure and fixed in the final step.
- Total of 171 Fitted Parameters.

B^0+B +Continuum MC Fit Result:

$$|q/p|-1 = (-0.35 \pm 0.46) \times 10^{-3}$$

No Bias found on MC with $|q/p|=1$

Results on Modified MC with $|q/p| \neq 1$

- $|q/p|$ related to Semileptonic

Asymmetry:

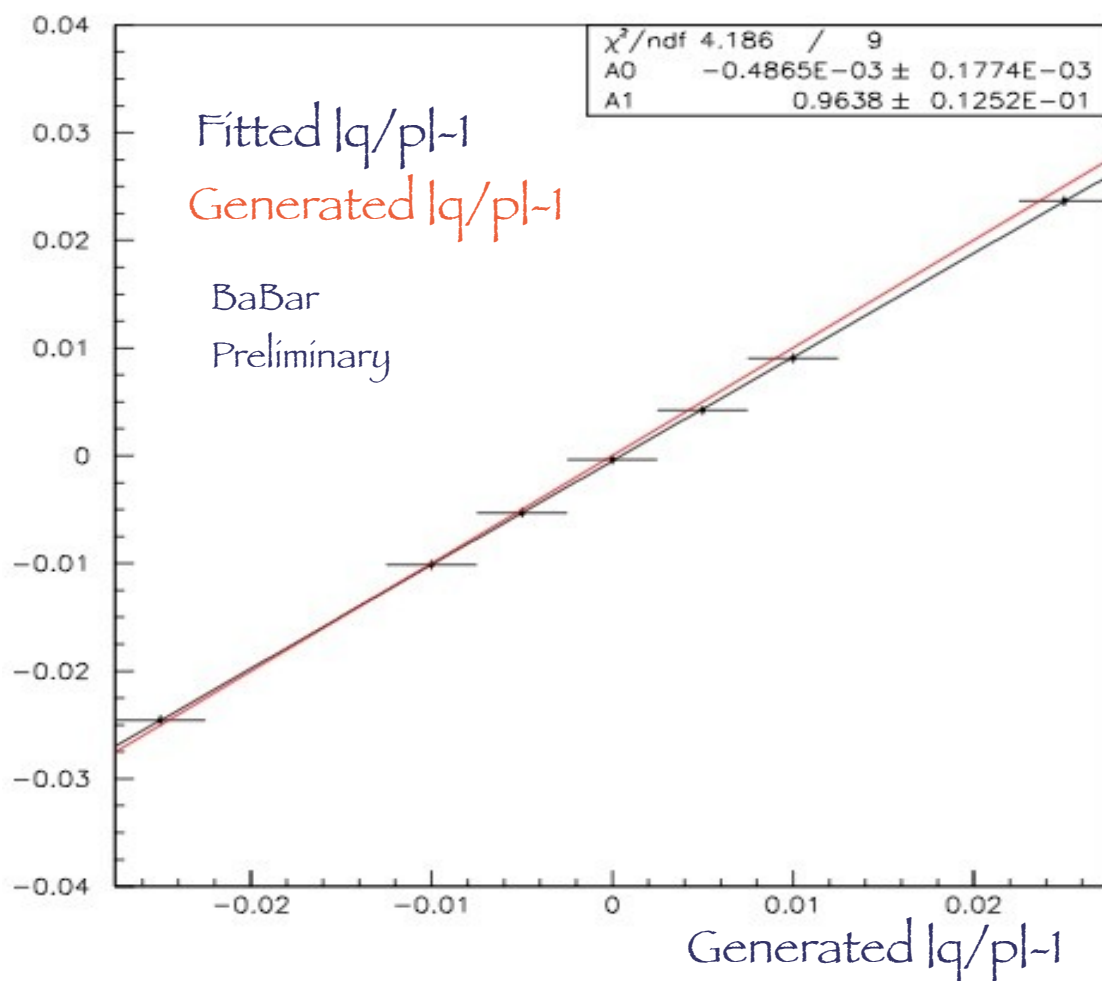
$$A_{SL} = \frac{N(B^0 B^0) - N(\bar{B}^0 \bar{B}^0)}{N(B^0 B^0) + N(\bar{B}^0 \bar{B}^0)}$$

$$A_{SL} = \frac{1 - |q/p|^4}{1 + |q/p|^4} \simeq 2 \left(1 - \left| \frac{q}{p} \right| \right)$$

- MC with $K = |q/p| - 1 \neq 0$ obtained by random rejecting a fraction $F = 4K / (2K + 1)$ of mixed $B^0 \bar{B}^0$ ($K < 0$) or $\bar{B}^0 B^0$ ($K > 0$) events
- Fraction $F/2$ of Unmixed events ($B^0 B^0$) rejected to preserve the correct value of x_d
- Rejection performed by exploiting the MC truth on B^0 flavor
- Checks: correctness of algorithm, mistag, detector asymmetries and D_{tag} fraction determination

Fitted vs Generated $|q/p|-1$

Result obtained on B^0+B +Continuum
Full MC Fit

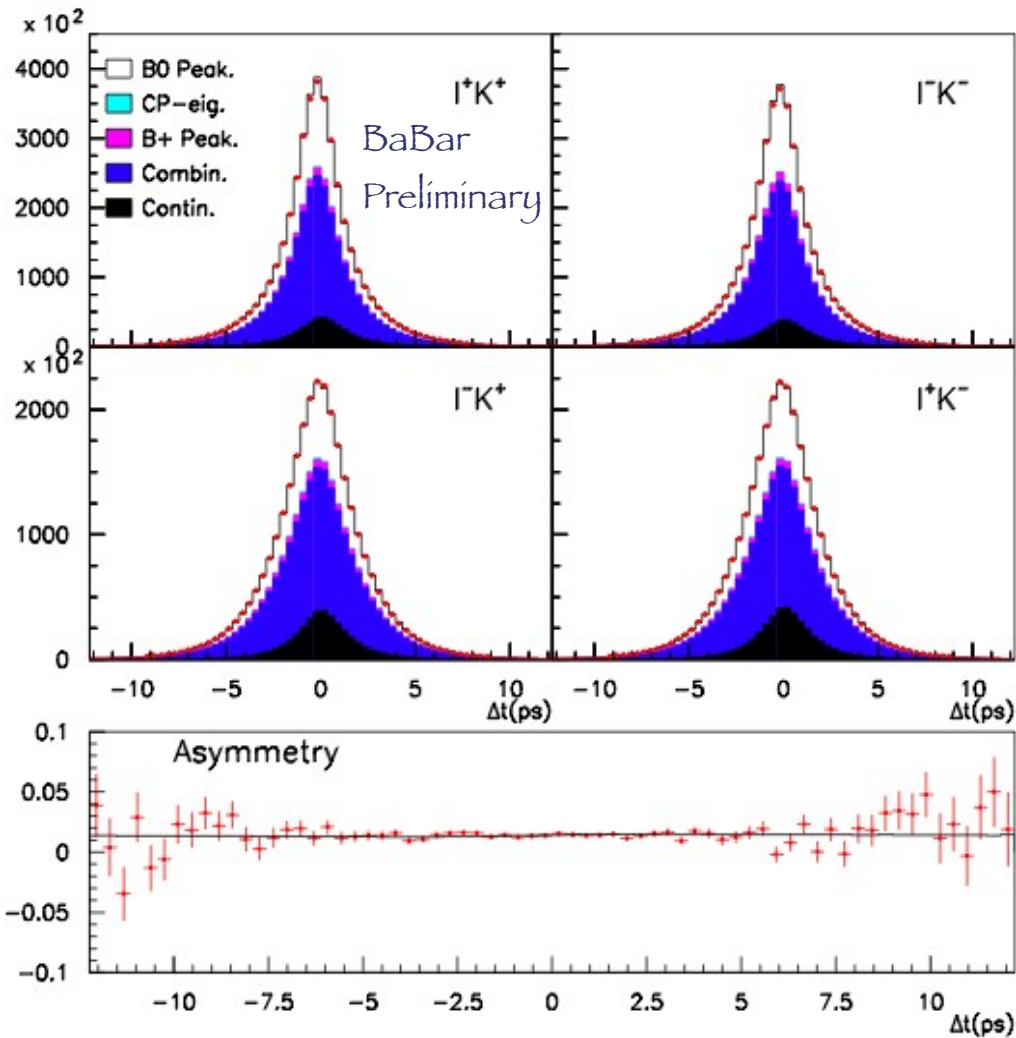


- Slope=0.96: ~4% relative bias on $|q/p|-1$ found
- Effect lower than Data statistical error in a very wide $|q/p|$ range.
- Correction applied to the $|q/p|$ unblinded result.

Real Data Results

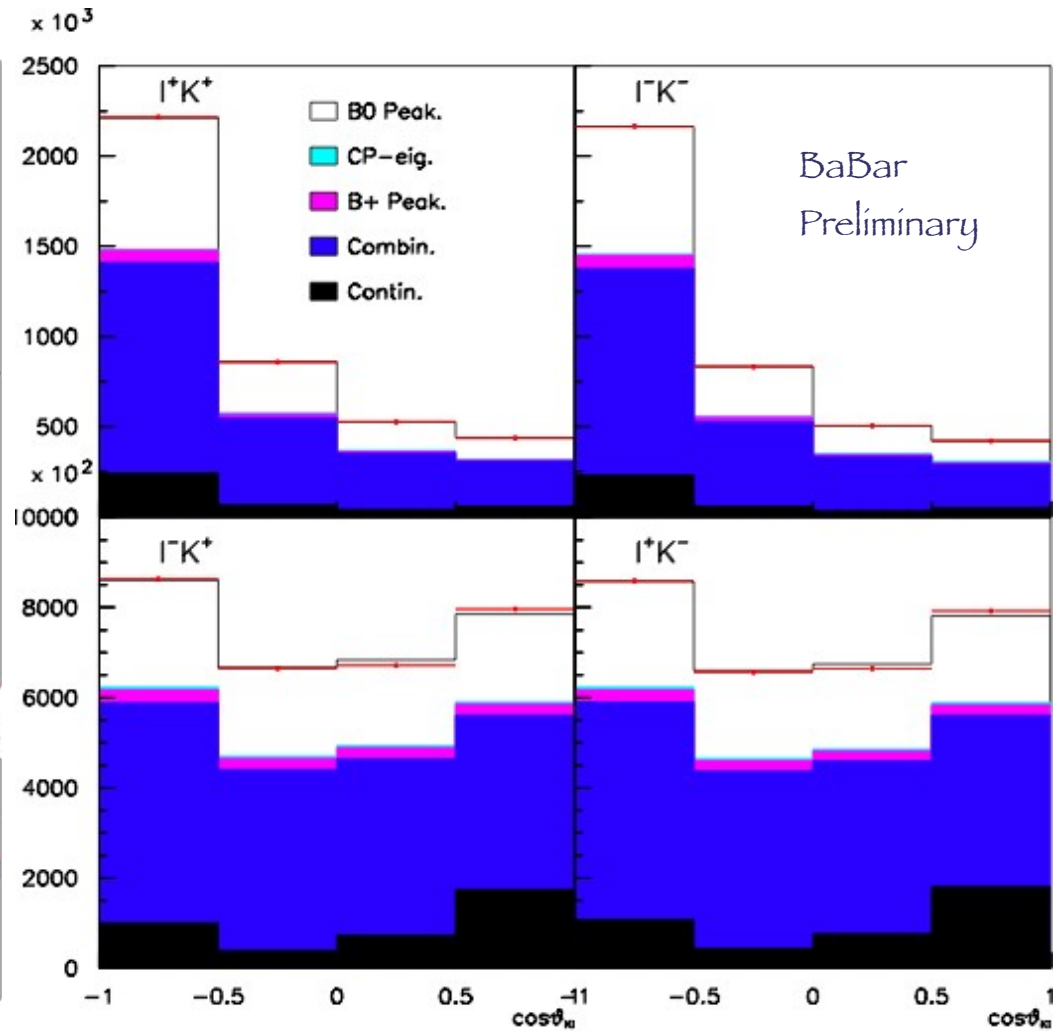
Real Data Results

Fitted Δt Shapes



Raw $N(I^+K^+)/N(I^-K^-)$ Asymmetry

Fitted $\cos(\theta_{K\text{-Lepton}})$ Shapes



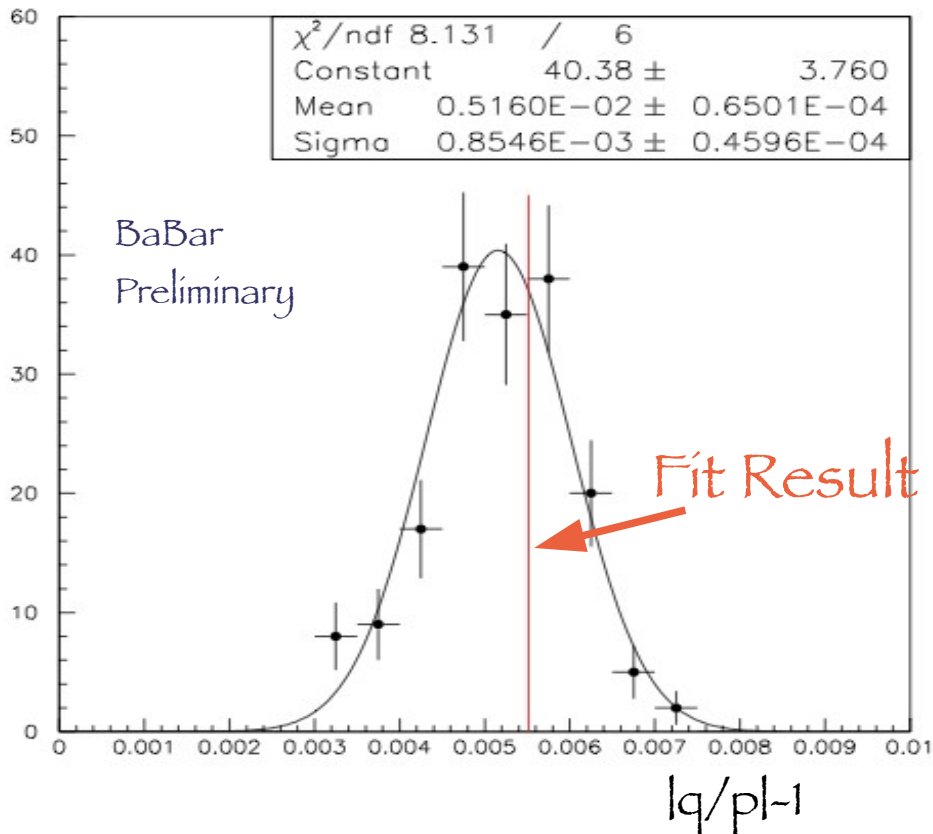
Real Data Results

Blind Result

$$|q/p|-1 = (5.56 \pm 0.84) \times 10^{-3}$$

- Result checked using a parameterized simulation by generating several pseudo-experiments (Toy MC)

Pseudo Experiments results



- Toy MC Spread in very good agreement with statistical error of the result
- Bias of $-3.6 \times 10^{-4} < 0.5 \sigma$ wrt Nominal Fit quoted as systematic error related to analysis bias

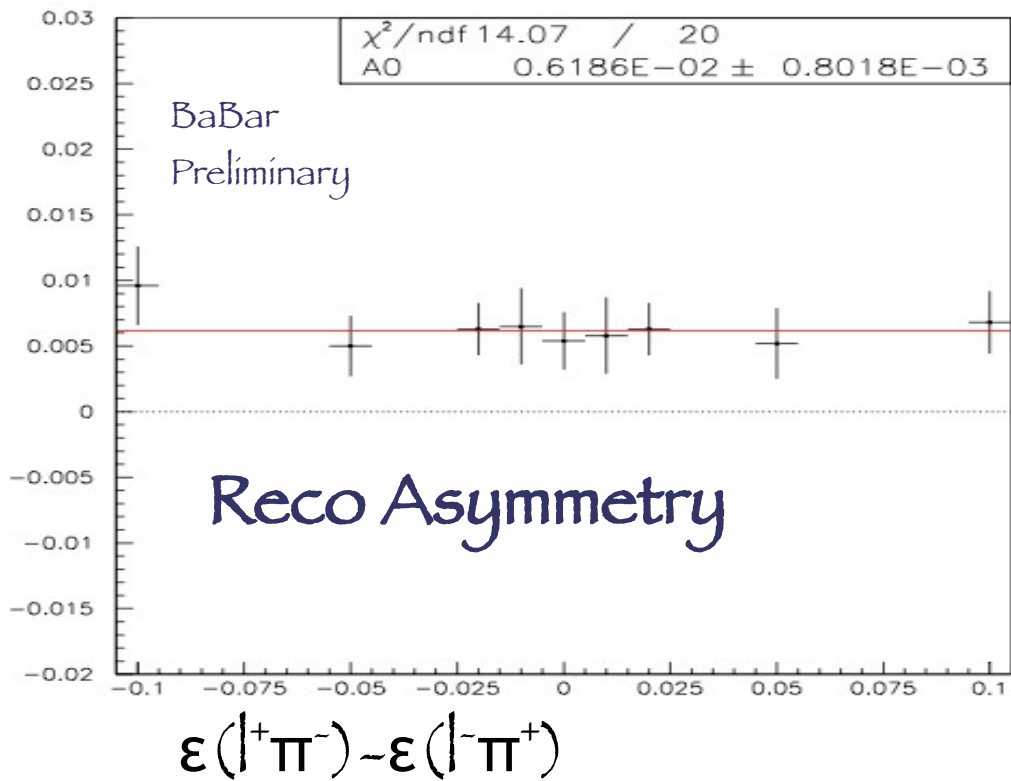
Checks & Systematic Uncertainties

$|q/p|$ vs Detector Asymmetries

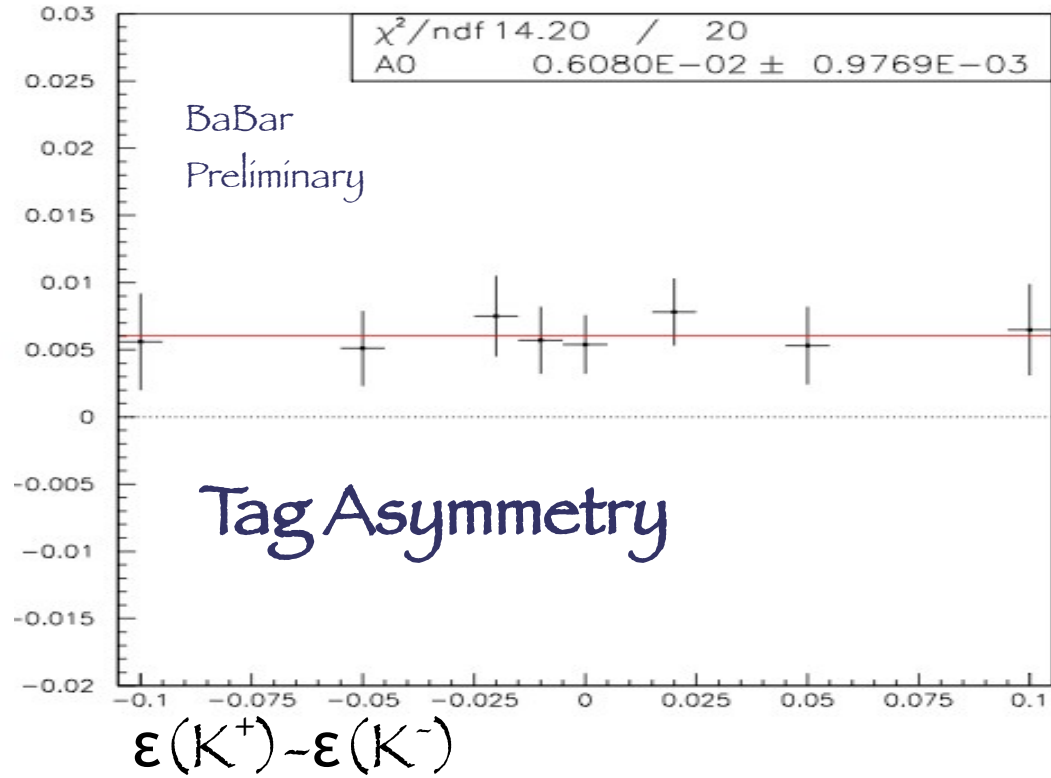
- Physical and Detector Asymmetries are strongly correlated
- Test performed to look for possible bias on the $|q/p|$ determination produced by a not correct description of the interconnection between Physical & Detector Asymmetries in the Fit:
 - Modify the data in order to produce an artificial efficiency asymmetry by random rejecting positive or negative leptons/kaons from the selected sample
 - Artificial $|\Delta\epsilon| = |\epsilon(l^+\pi^-) - \epsilon(l^-\pi^+)|$ & $|\epsilon(K^+) - \epsilon(K^-)| = 1\%, 2\%, 5\%, 10\%$ produced
 - $|\Delta\epsilon|$ range of variation very large as compared to PID studies

$|q/p|-1$ vs $\Delta\epsilon$

Fitted $|q/p|-1$ BLIND



Fitted $|q/p|-1$ BLIND



- Real Data Uncorrelated Subsamples
- Stable $|q/p|$ behaviour observed in all the $\Delta\epsilon$ range

→ The Fit correctly disentangles Physical vs Detector Asymmetries

Systematic Uncertainties

- **Sample Composition** determined by an external Fit on M^2v by floating D^* , D^{**} and Combinatorial using shapes from MC and Off-peak events

- Statistical error of M^2v fit, Uncertainty on Fraction of other Peaking events, CP-eigenstates and B^+ events in the Combinatorial sample

$$\rightarrow \Delta|q/p| = \begin{matrix} +1.23 \\ -1.55 \end{matrix} \times 10^{-3}$$

Dominant Uncertainty

- **Δt Resolution Model:**

- Fit repeated by leaving free all the Resolution Parameters

$$\rightarrow \Delta|q/p| = +0.6 \times 10^{-3}$$

- **Analysis Bias:**

- MC Statistical error plus bias from Toy MC study

$$\rightarrow \Delta|q/p| = \begin{matrix} +0.46 \\ -0.58 \end{matrix} \times 10^{-3}$$

Systematic Uncertainties

- Dtag Δt shape:
 - Semi-difference of the two different strategies (High Purity Sel.)
 - $\Delta|q/p| = \pm 0.65 \times 10^{-3}$
- Dtag Fraction in the B^+ sample:
 - $F_{Dtag}^{B^+} = R_{MC} * F_{Dtag}^{B^0}$; $R_{MC} = BR(D^{*0} \rightarrow K^- X) / BR(D^{*+} \rightarrow K^- X)$, $\Delta R_{MC} = 6.8\%$
 - $\Delta|q/p| = \pm 0.11 \times 10^{-3}$
- Physical Parameters floated or fixed to the world averages
 - $\Delta\Gamma = 0 / 0.02 \text{ ps}^{-1}$; $\Delta m = 0.508 \text{ (Fit)} / 0.507 \text{ (PDG)}$
 - $\tau_{B^0} = 1.553 \text{ (Fit)} / 1.519 \text{ (PDG)}$; $\tau_{B^+} = 1.76 \text{ (Fit)} / 1.4 \text{ (PDG)}$
 - $\Delta|q/p| = +0.28 \times 10^{-3}$

→ Total Systematics: $\Delta|q/p| = \begin{matrix} +1.61 \\ -1.78 \end{matrix} \times 10^{-3}$

Conclusions

Unblinded Preliminary Result

Preliminary Systematic Uncertainties

Source	$\Delta q/p $
Peaking Sample Composition	$+1.17$ -1.50×10^{-3}
Combinatoric Sample Composition	$\pm 0.39 \times 10^{-3}$
ΔT Resolution Model	$+0.60 \times 10^{-3}$
Dtag fraction	$\pm 0.11 \times 10^{-3}$
Dtag ΔT distribution	$\pm 0.65 \times 10^{-3}$
Fit Bias	$+0.46$ -0.58×10^{-3}
CP-eigenstate description	—
Physical Parameters	$+0.28 \times 10^{-3}$
Total	$+1.61$ -1.78×10^{-3}

After Unblinding:

$$|q/p|-1 = \left(-0.76 \pm 0.84 \begin{matrix} +1.61 \\ -1.78 \end{matrix} \right) \times 10^{-3}$$

After Bias Correction:

$$|q/p|-1 = \left(-0.29 \pm 0.84 \begin{matrix} +1.61 \\ -1.78 \end{matrix} \right) \times 10^{-3}$$

In agreement
with SM

Conclusions

- We present a new precise measurement of the parameter governing CP violation in B^0 mixing based on the full BaBar statistics and using a technique exploiting a Partial Reconstruction of $B^0 \rightarrow D^* l \nu$ decays and K Tag.

We obtain the preliminary result:

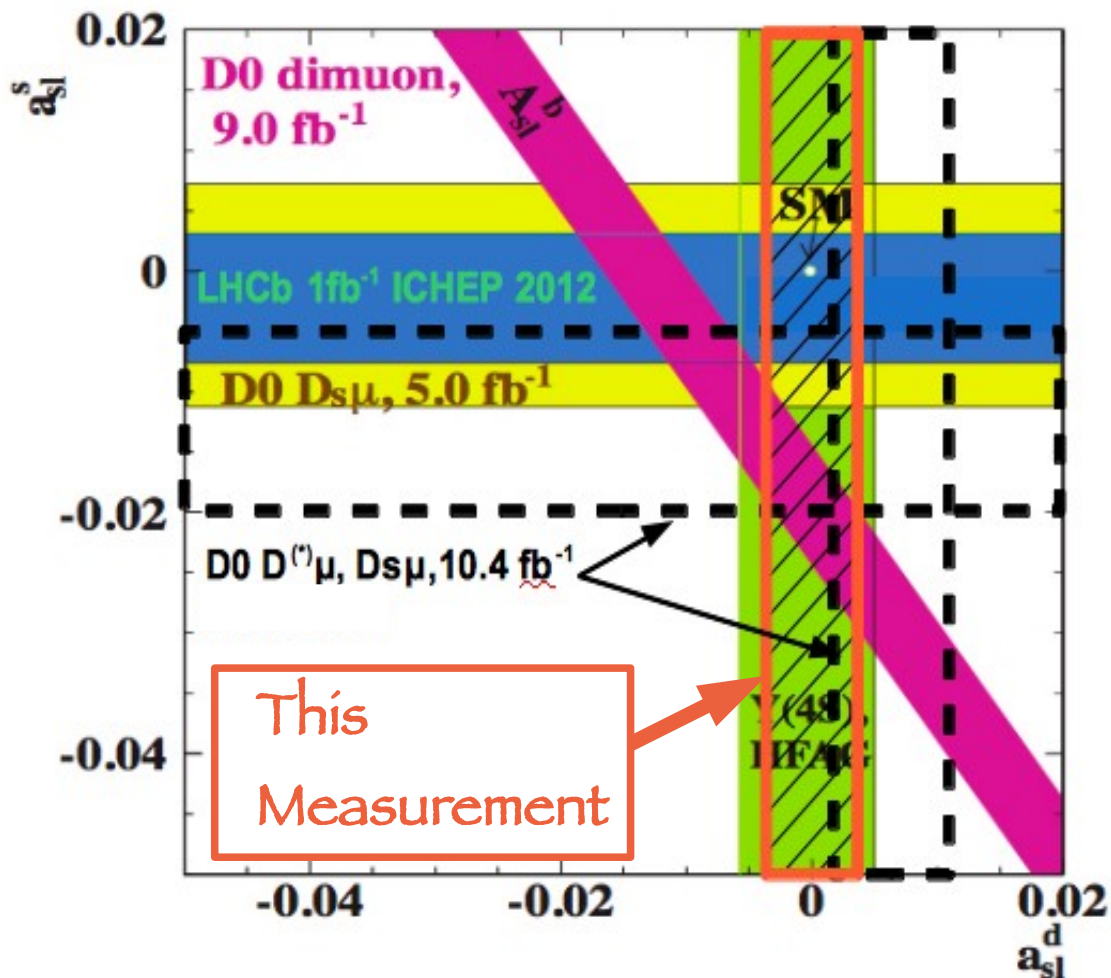
$$|q/p|-1 = \left(-0.29^{+1.82}_{-1.97} \right) \times 10^{-3}$$

$$A_{sl} = \left(0.06^{+0.39}_{-0.36} \right) \%$$

To be compared with the current average from B-factories:

$$|q/p|-1 = (0.2 \pm 2.8) \times 10^{-3}$$

$$A_{sl} = (-0.05 \pm 0.56) \%$$



Backup

Analysis Strategy

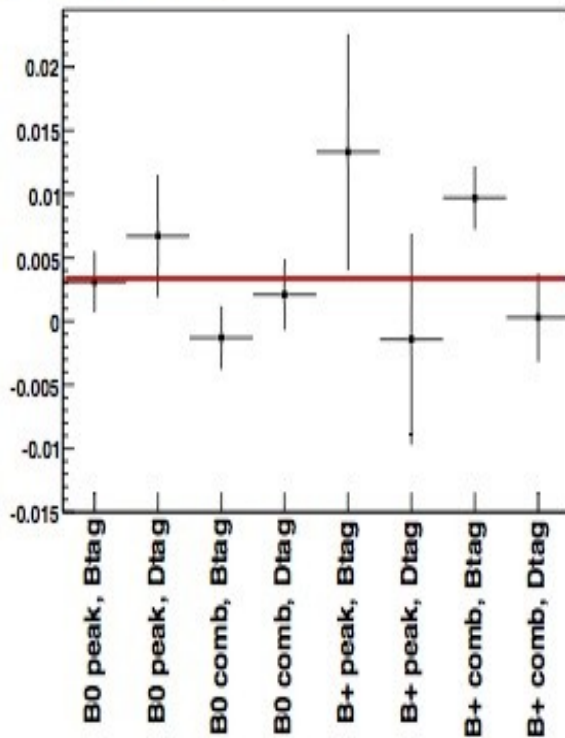
- Hypothesis: same Detector Asymmetries shared by different samples

- Verified on simulation:

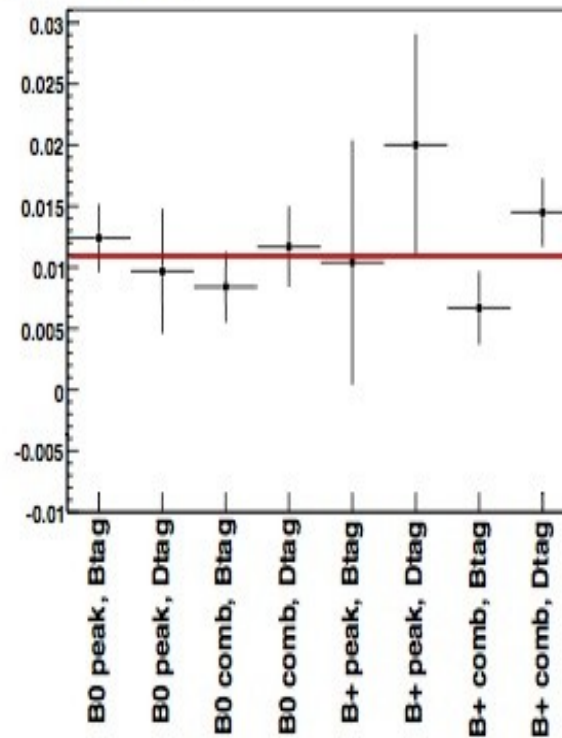
$$A_{\ell K} = \frac{N(\ell^+ K^+) - N(\ell^- K^-)}{N(\ell^+ K^+) + N(\ell^- K^-)}$$

	Electrons	Muons
$A_{\ell K}(B_{tag})$	0.0149 ± 0.0013	0.0196 ± 0.0016
$A_{\ell K}(D_{tag})$	0.0152 ± 0.0009	0.0205 ± 0.0010
$A_{\ell K}(B_{tag}) - A_{\ell K}(D_{tag})$	-0.0003 ± 0.0016	-0.0009 ± 0.0019

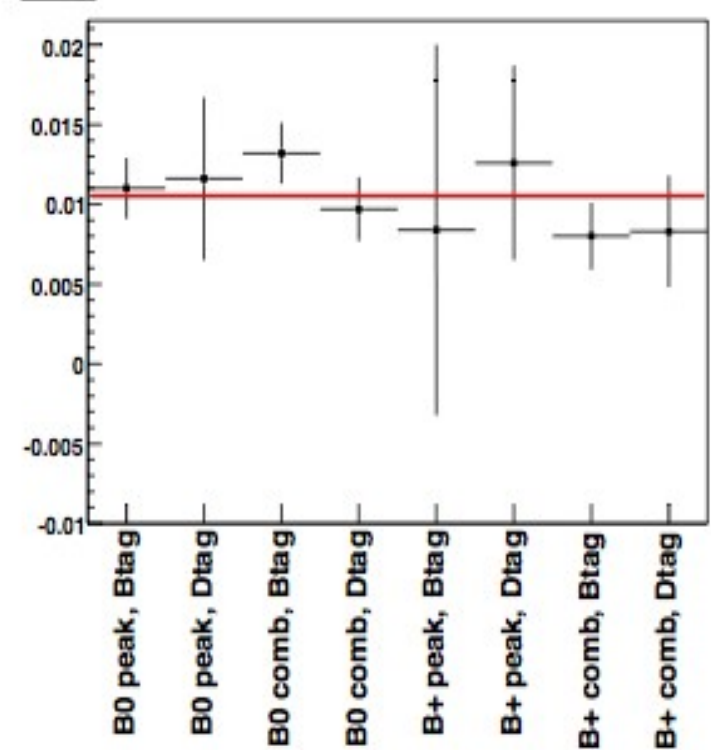
A_{rec} - electrons



A_{rec} - muons



A_{tag}



Likelihood Constraints

- Best statistical accuracy on Physical/Detector Asymmetries and mistag obtained by applying to the Likelihood some multiplicative Binomial Constraints

- For every P_K bin of Signal B^0 Btag events, (similar expressions apply for the other samples):

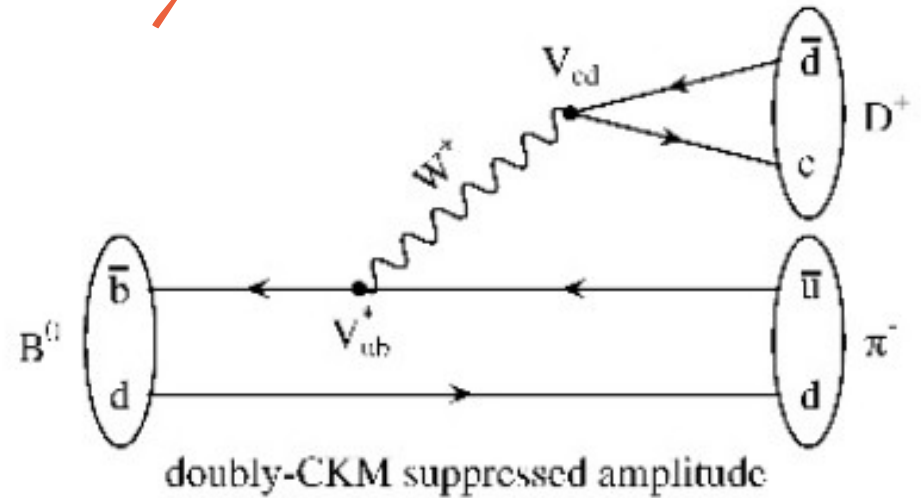
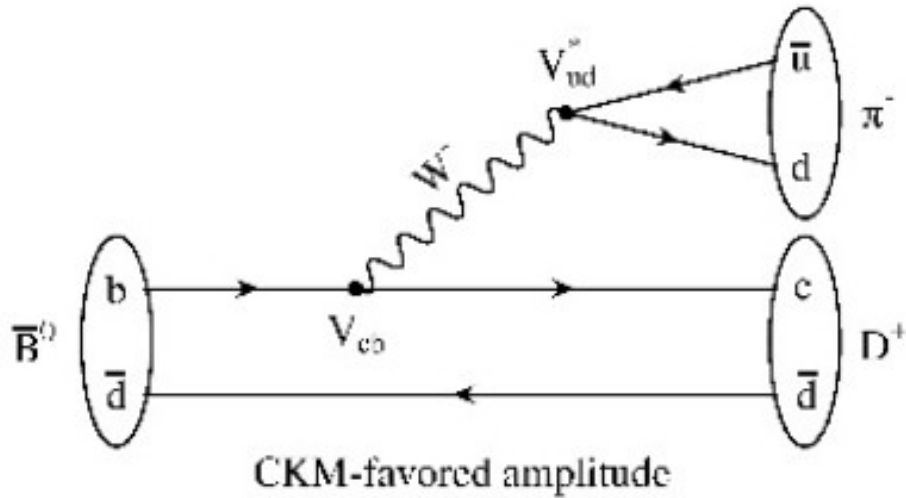
$$C(\omega, A_{rec}, A_{tag}, |q/p|) = \binom{N}{N_M} p_M^{N_M} (1 - p_M)^{N_U} \times \\ \binom{N_M}{N_{MK^+}} p_{MK^+, M}^{N_{MK^+}} (1 - p_{MK^+, M})^{N_{MK^-}} \binom{N_U}{N_{UK^+}} p_{UK^+, U}^{N_{UK^+}} (1 - p_{UK^+, U})^{N_{UK^-}}$$

- $N = N_{Mixed} + N_{Unmixed}$; $N_{Mixed} = N_{Mixed K^+} + N_{Mixed K^-}$; $N_{Unmixed} = N_{Unmixed K^+} + N_{Unmixed K^-}$

- Probabilities p_{xy} obtained from integrals of the relevant observed PDF(Δt) in terms of mistag, Physical and Detector Asymmetries

- 8 Detector-Asymmetry parameters floated in the fit

DCS Decays



$$\bar{\mathcal{A}}_{CF}$$

$$\mathcal{A}_{DCS}$$

$$r' = |\bar{\mathcal{A}}_{DCS}/\mathcal{A}_{CF}|$$

$$\mathcal{A}_{CF} = \bar{\mathcal{A}}_{CF} = |\mathcal{A}_{CF}| e^{i\delta_c}$$

$$\bar{\mathcal{A}}_{DCS} = r' |\mathcal{A}_{CF}| e^{i\delta_u} e^{i\gamma}$$

$$\mathcal{A}_{DCS} = r' |\mathcal{A}_{CF}| e^{i\delta_u} e^{-i\gamma}$$

δ_c, δ_u : strong phases of CF, DCS

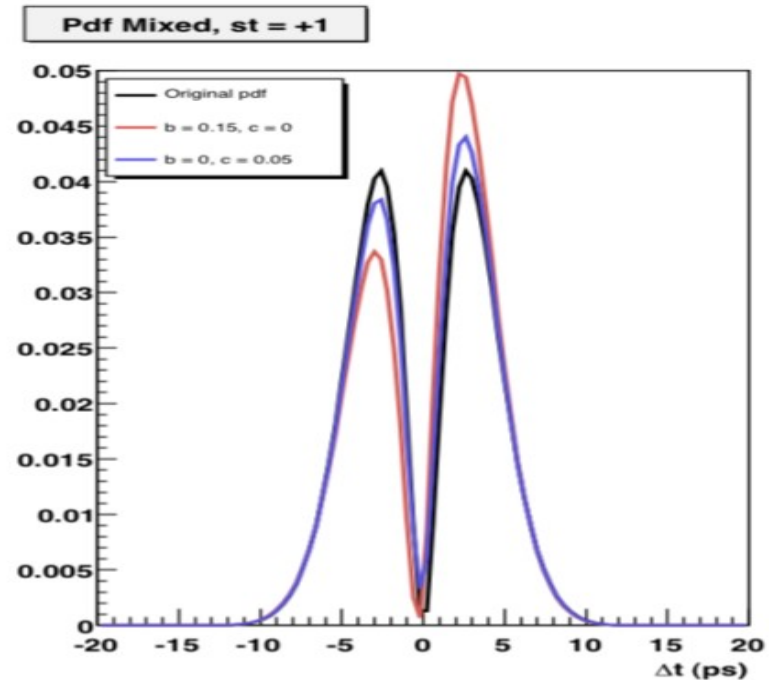
γ : relative weak phase between the two decays

$$\frac{q}{p} = \left| \frac{q}{p} \right| e^{-2i\beta}$$

$$b = 2r' \sin(2\beta + \gamma) \cos \delta'$$

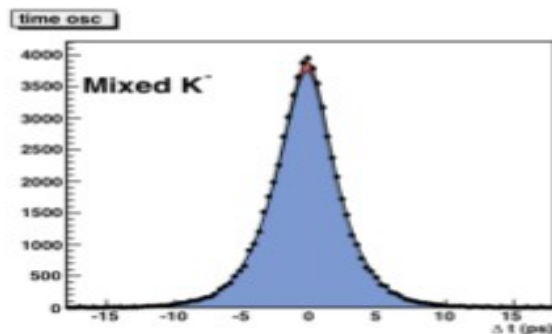
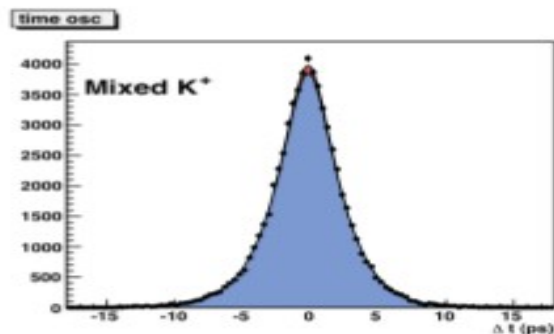
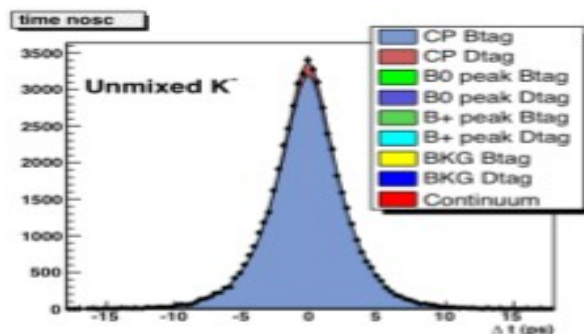
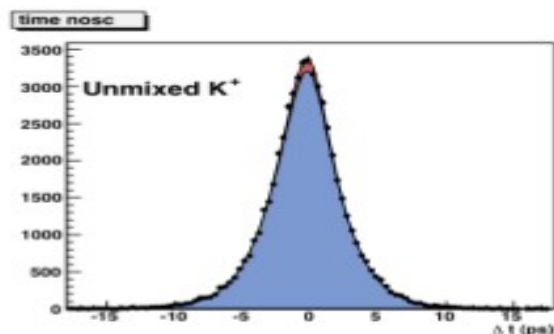
$$c = -2r' \cos(2\beta + \gamma) \sin \delta'$$

$$\delta' = \delta_u - \delta_c$$

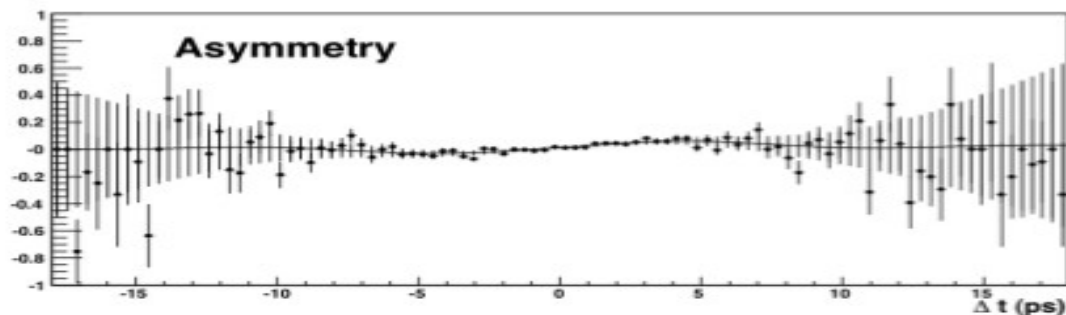


CP-eigenstates

$$F_{CP\text{-eigen}} = \frac{\Gamma}{4} e^{-\Gamma|\Delta t|} [1 \pm S_{eff} \sin(\Delta m_d \Delta t) \pm C_{eff} \cos(\Delta m_d \Delta t)]$$



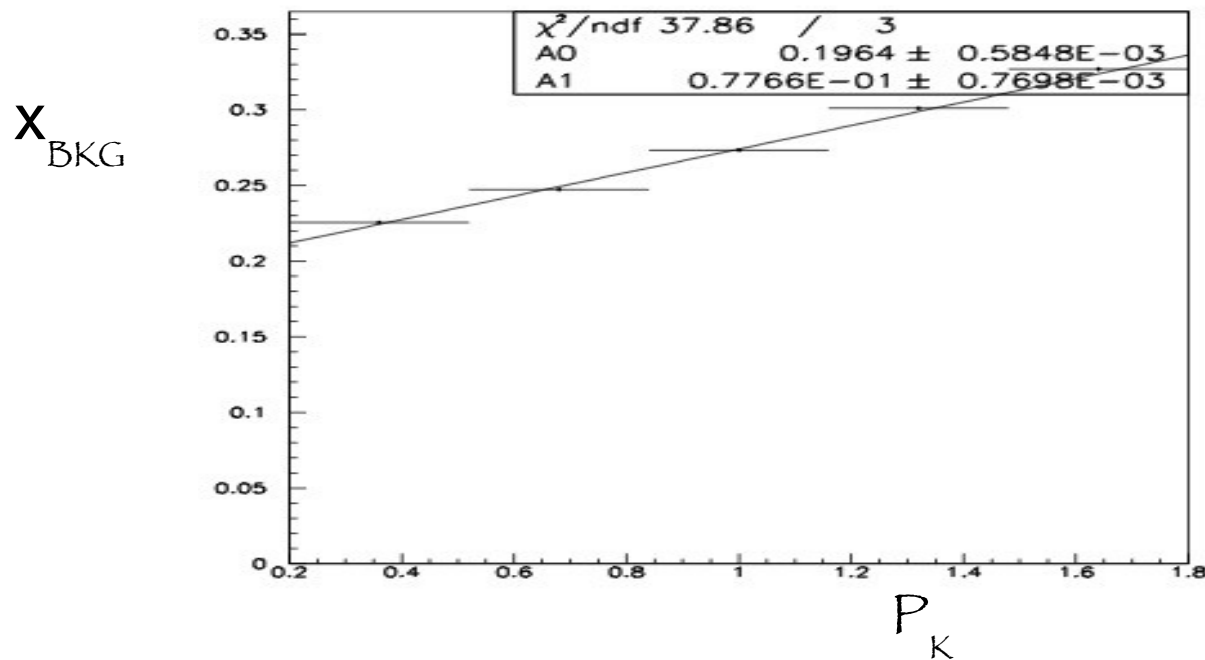
Parameter	Fit result
C_{eff}	-0.0110 ± 0.0066
S_{eff}	-0.0886 ± 0.0056



B^0 Combinatorial: Effective d

- Due to charge correlation between Lepton & π_{soft} , B^0 Combinatorial Sample shows a higher fraction of mixed events wrt Signal
- In BKG events it's possible to pick up Lepton & π_{soft} from the two different B^0 decays (more probable in "Mixed" events).

→ $\langle x_d(\text{BKG}) \rangle \sim 1.4 x_d(\text{SIG})$ depending on P_K



• B^0 BKG Observed PDF modified to include this effect

• 27 mistag & effective mixing parameters floated

B^0 Combinatorial: Mistag vs Effective χ_d

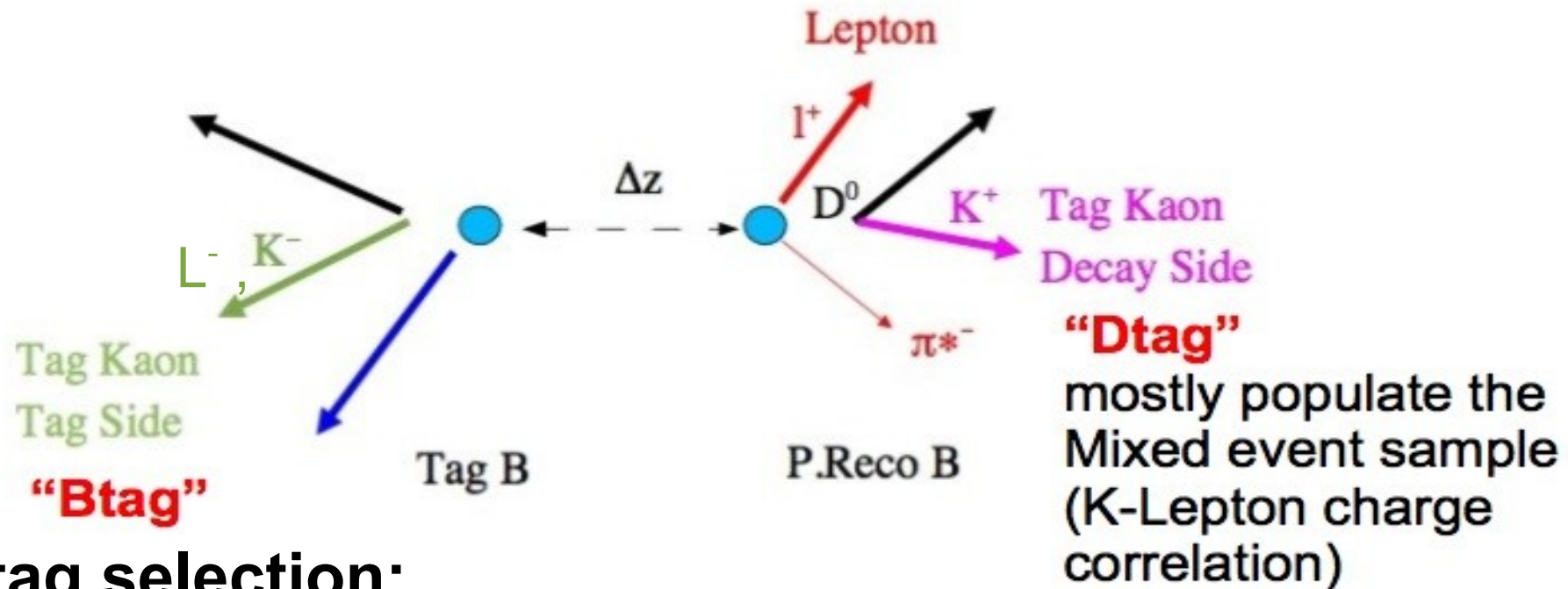
- Combinatorial BKG B^0 Btag PDF for Positive Mixed (l^+K^+) sample, (similar expressions apply for the other ones):

$$\begin{aligned} \mathcal{F}_\chi^{meas}(\Delta t, s_t = 1, s_m = -1) &= \rho\tau \left[(1 - \omega_\chi^+) \frac{\chi_d^{Bkg}}{\chi_0^{Bkg}} \mathcal{F}_\chi(\Delta t, 1, -1) + \omega_\chi^- \frac{1 - \chi_d^{Bkg}}{1 - \chi_0^{Bkg}} \mathcal{F}_\chi(\Delta t, -1, 1) \right] = \\ &= RT(1 + A_{rec})(1 + A_{tag}) \left[(1 - \omega_\chi^+) \frac{\chi_d^{Bkg}}{\chi_0^{Bkg}} \mathcal{F}_\chi(\Delta t, 1, -1) + \omega_\chi^- \frac{1 - \chi_d^{Bkg}}{1 - \chi_0^{Bkg}} \mathcal{F}_\chi(\Delta t, -1, 1) \right] \end{aligned}$$

$$\chi_d^{Bkg}(P_K) = \chi_0^{Bkg} \times (a + bP_K)$$

$$\chi_0^{Bkg} = \frac{x_{Bkg}^2}{2(1+x_{Bkg}^2)}, \text{ where } x_{Bkg} = \tau_{B^0}^{Bkg} \Delta m_d^{Bkg}$$

High Purity Dtag Selection



Dtag selection:

- Look for same charge (L^+_{Reco}, K^+) pairs
- Opposite charge Tag Lepton L^- required to suppress Btag Mixed events $B \rightarrow K^+$
- ($L^+_{\text{Reco}}, L^-_{\text{Tag}}, K^+$) sample has Dtag-Purity=87%
- 13% Residual Btag contamination from Tag Side $B \rightarrow D \rightarrow K^+$, Tag Side $B \rightarrow D \rightarrow L^-$, Reco Side $B \rightarrow D \rightarrow L^-$
- Purity can be increased from 87% to **94% ($\epsilon \sim 5\%$)** by requiring K tracks to be assigned to Reco Side according to some angular variables included in a likelihood ratio

Δt Dtag PDF Determination on Real Data

Strategy:

- **High-Purity Dtag selection optimized with Purity =94%, $\epsilon \sim 5\%$**
- Perform the same Dtag selection on MC & Real Data (OnPeak & OffPeak)
- Subtract residual Continuum BKG from OnPeak using Luminosity-rescaled selected OffPeak events
- Subtract residual Btag events ($\sim 6\%$) using MC predictions
- **Compute Real Data PDFs for the four different Dtag classes (B^0 , B^+)X(Peaking, BKG):**

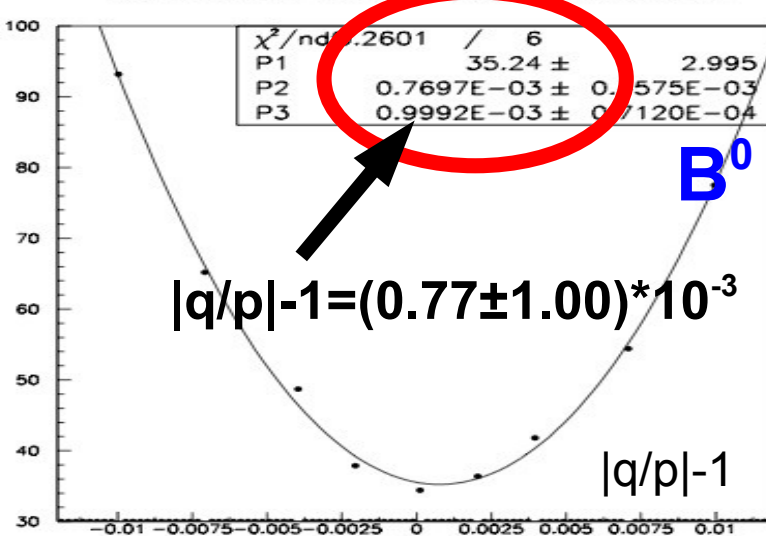
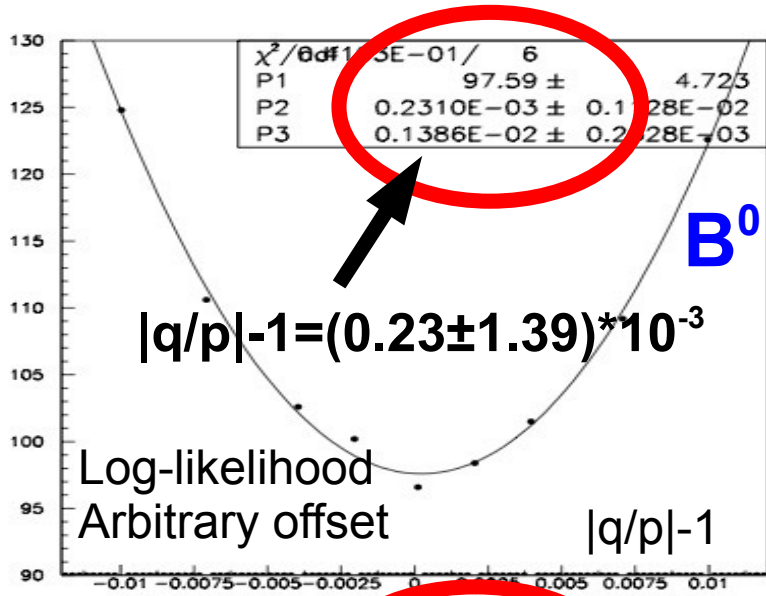
$$\text{PDF}_{\text{Class } i}^{\text{DATA}} = \text{PDF}_{\text{Class } i}^{\text{MC}} * (\text{PDF}_{\text{High Purity Selection}}^{\text{DATA}} / \text{PDF}_{\text{High Purity Selection}}^{\text{MC}})$$

- Method checked on MC using Standard vs High Purity Selection PDFs

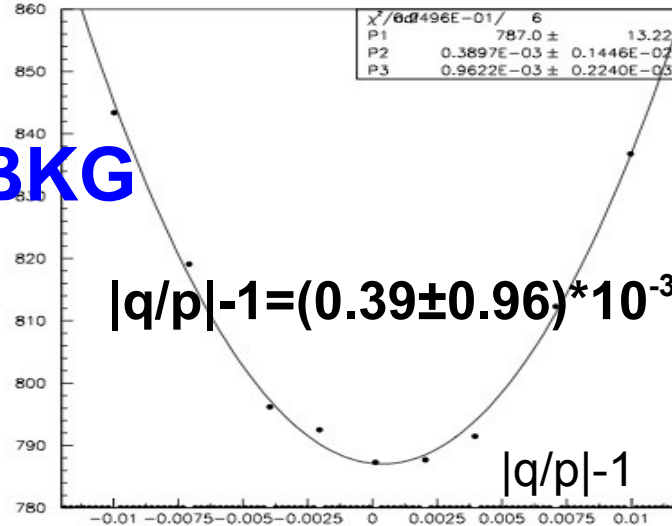
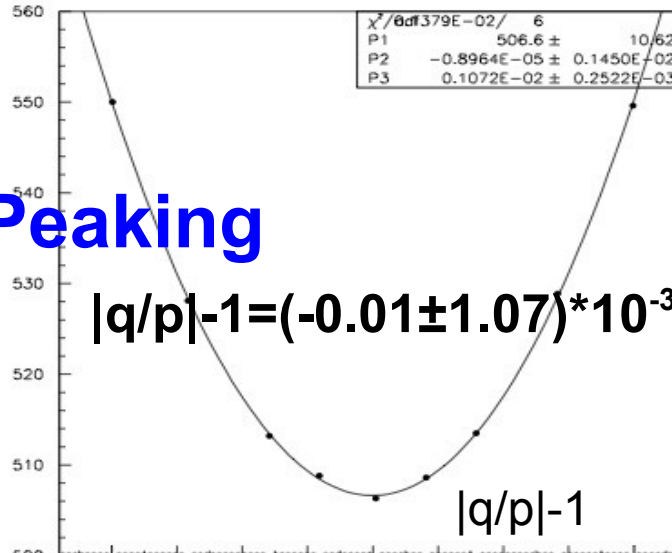
MC Dtag Δt PDF: Standard vs High Purity Selection

- Comparison of MC Fit results using the Standard or High Purity PDFs:

Standard PDF



High Purity Selection



$\delta|q/p|$

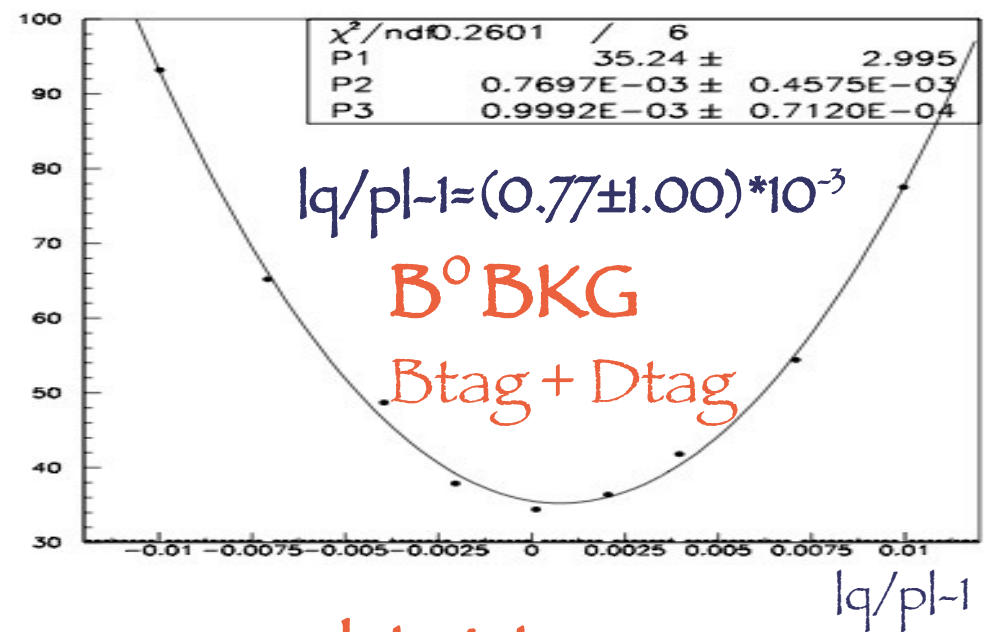
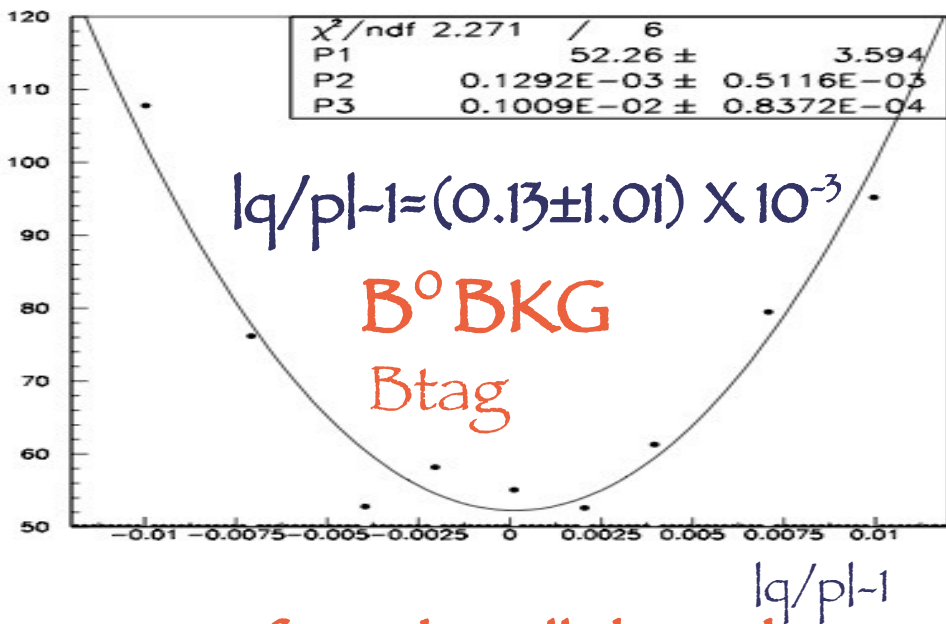
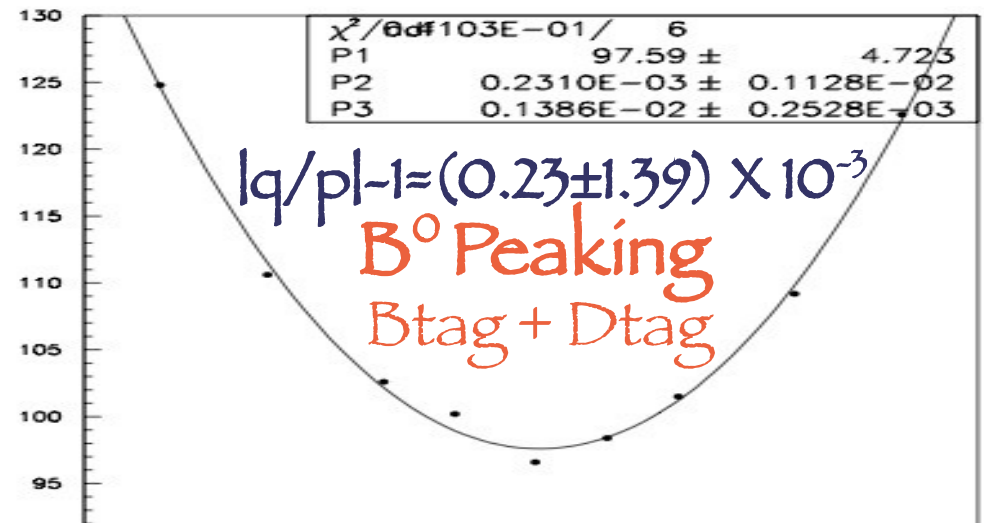
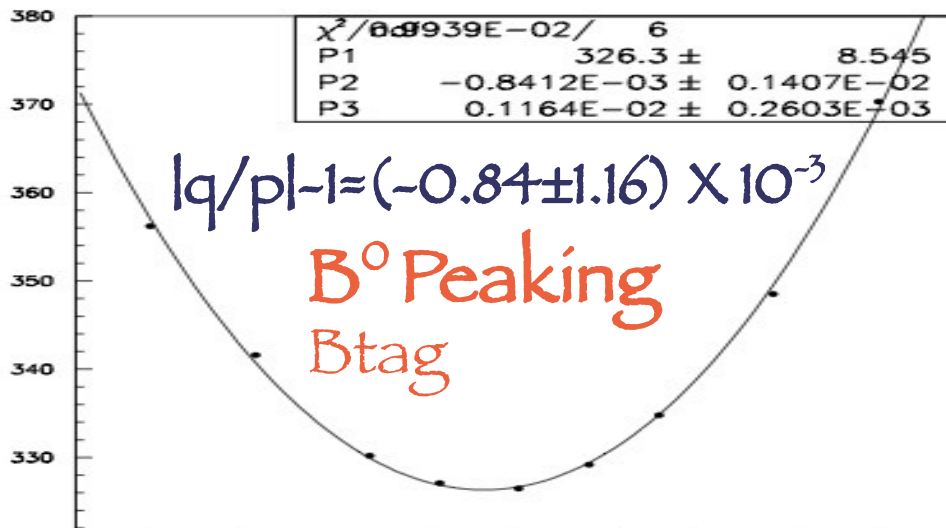
$-0.24 \cdot 10^{-3}$

$-0.38 \cdot 10^{-3}$

Effect ~1/3 of MC Statistical σ

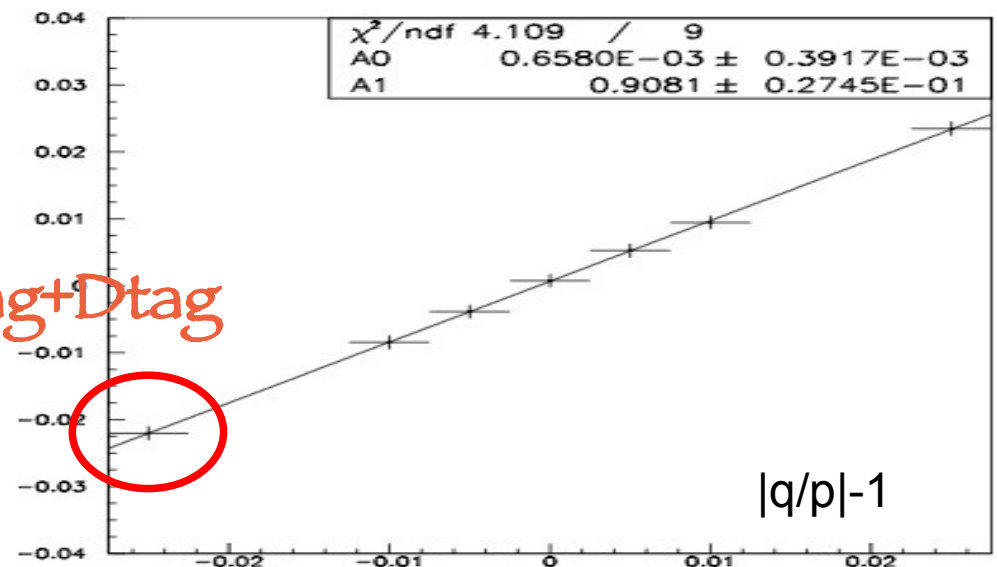
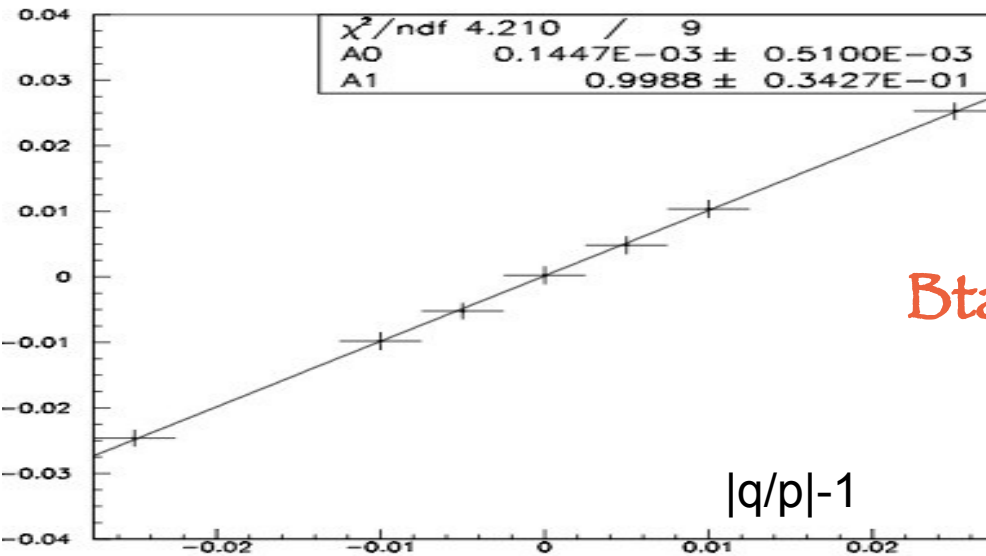
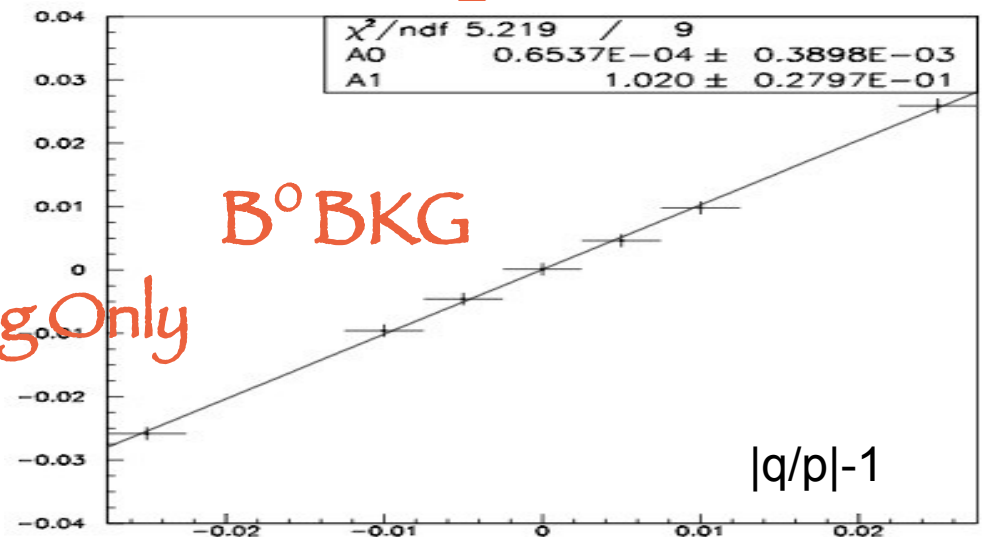
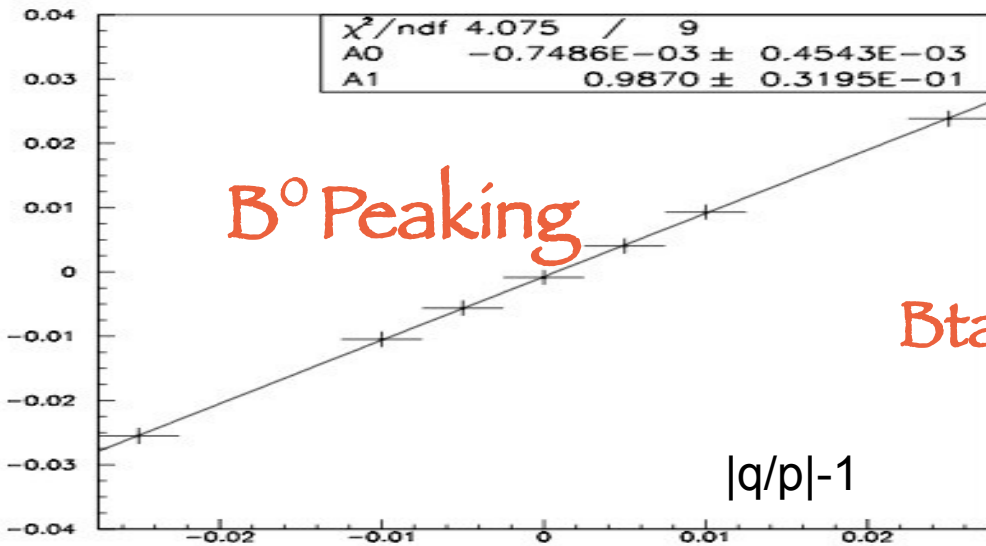
MC Results on different B^0 subsamples

Likelihood Profiles with Arbitrary Offsets



- No Bias found in all the subsamples on MC with $|q/p|=1$
- B^0 combinatorial BKG helps in $|q/p|$ measurement

Fitted vs Generated $|q/p|-1$



- B^0 Peaking: no bias found
- B^0 BKG only (Btag+Dtag):
10% bias (2.7σ) on $|q/p|-1$ for $|q/p|-1 = -0.025$

Sample Composition

Sample Composition determined by an external Fit on M^2 by floating D^* , D^{**} and Combinatorial using shapes from MC

- Dominant systematic uncertainty

- Peaking Sample Uncertainty

- Statistical error of external fit $\pm 1.09 \cdot 10^{-3}$

- Isospin symmetry breaking: B^0/B^+ in the $D^{**} = (50 \pm 25)\% \pm 0.20 \cdot 10^{-3}$

- CP-eigenstates yield varied by $\pm 50\% \pm 0.31 \cdot 10^{-3}$

- Remnant Peaking yield (D^* , D^*D_sX , D^*h) varied by $\pm 20\%$
 $+0.22/-0.96 \cdot 10^{-3}$

$$\Delta|q/p| = \begin{matrix} +1.17 \\ -1.50 \end{matrix} \times 10^{-3}$$

Sample Composition

- Combinatorial Sample Uncertainty
- Fraction of B^+ and B^0 in the Combinatorial fixed to MC expectations
 - Difference between B^0 and B^+ is expected when mixing takes place and the lepton is coupled with a slow pion from the tag side:
 $B^0 \rightarrow D^* X, D^* \rightarrow \pi^+ D^0$
 - B^0 BKG has 40% more mixed events than B^0 Peaking
 - Other BKG events have same probability between B^0 and B^+
 - Fraction of B^+ conservatively varied by $\pm 4.5\%$ which corresponds to the error on inclusive $BR(B^0 \rightarrow D^{*+} X)$ (from PDG)

$$\Delta|q/p| = \pm 0.39 \times 10^{-3}$$