

News on CPV in mixing using P.R. D^*lv and K-tag

•Alessandro Gaz PHD thesis results:

Martino, 5/28/2008

$$|q/p|-1 = xxx \pm 0.0025(\text{stat}) \pm 0.0018(\text{syst}) \pm 0.0023(\text{bias})$$

(2nd best meas. @ B factories)

A good result but:

- $|q/p|$ bias ~ 0.004 from MC, bigger than statistical error;
- Bias reflects in the largest systematic error...

Large bias on τ_{B_0} , Δm_d :

PDG:

$$\bullet \tau_{B_0} = 1.490 \pm 0.004 \text{ ps}$$

$$1.530 \pm 0.009 \text{ ps}$$

$$\bullet \Delta m_d = 0.5699 \pm 0.0022 \text{ ps}^{-1}$$

$$0.507 \pm 0.005 \text{ ps}^{-1}$$



Bias to be understood before publication!

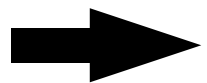
Problems of the Unbinned Fit

A) Slowness:

- Fit of the full Run1-Run5 data statistics too long (~ 100 free parameters);
- Split of data set (takes ~ 24 h to fit 5% of the real data statistics);
- Result from the average of the different subsample;

B) Convergence difficulty:

- $\log(\text{Likelihood})$ shows a structure with secondary minima;
- **Measured Bias is actually a true effect or is it a feature of the fit instability?**
- Same question about the evaluation of systematic uncertainties;



A) and B) effects interfere:

Slowness precludes studies on convergence & stability of the fit.

Solution: Binned Fit

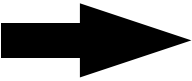
- Binning extended to all the relevant variables:

Δt , $\sigma(\Delta t)$, P_K , $m^2 v$, $\Theta(1-K) = 50K$ bins

8 event categories: (e/μ) X (Mixed/Unmixed) X (K^+/K^-)

→ Convergence takes ~ 15 h on the full R1-R5 data statistics by floating all the parameters!

→ Result on data compatible with the “Old-Unbinned” fit!

- 
- Go back to the MC in order to:
 - Define a strategy to reach the fit convergence;
 - Understand at which level of fit complexity the bias does appear (perfect/measured resolution and tagging; only signal/full sample composition);
 - Re-blind the fit on real data;

Study of Fit Convergence

- **Study the $\Delta\log(L)$ profile around the minimum** by performing a set of several fits with a fixed value of a relevant variable x (i.e. $|q/p|-1$, Δm_d , ...) and floating all the other parameters;

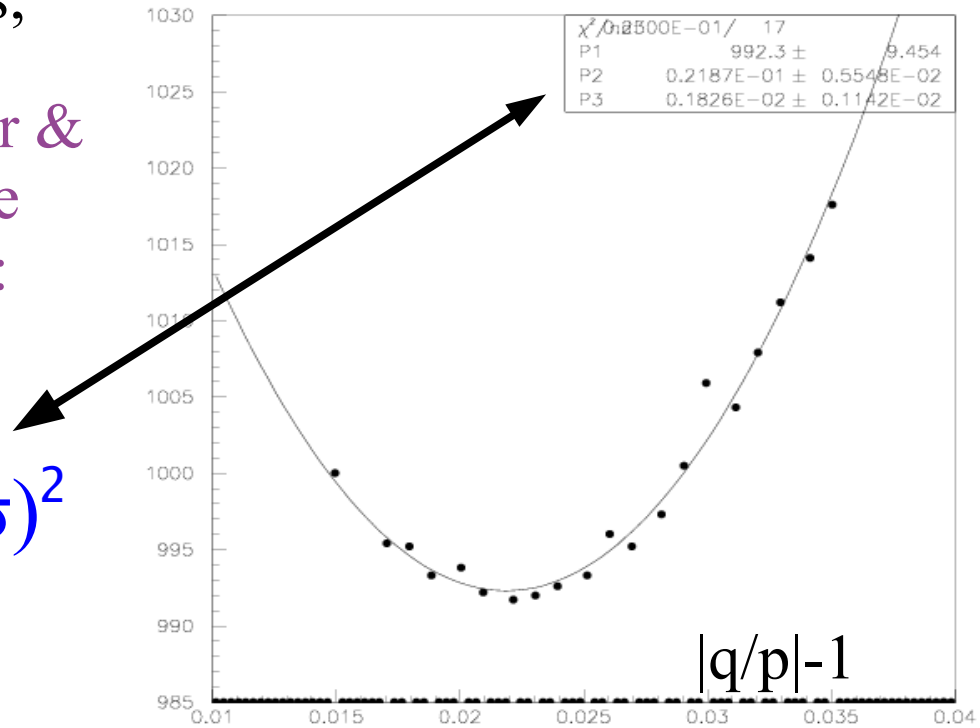
- **Determination of the parameter & statistical error directly from the plot by means of a parabolic fit:**

$$\log(L) = \log(L_{\min}) + \frac{1}{2} \left(\frac{x - x_{\min}}{\sigma} \right)^2$$

x_{\min} = Best Value

σ = Statistical Error

To be compared with the nominal fit results



Blind fit on data:

$$|q/p|-1 = 0.022 \pm 0.002$$

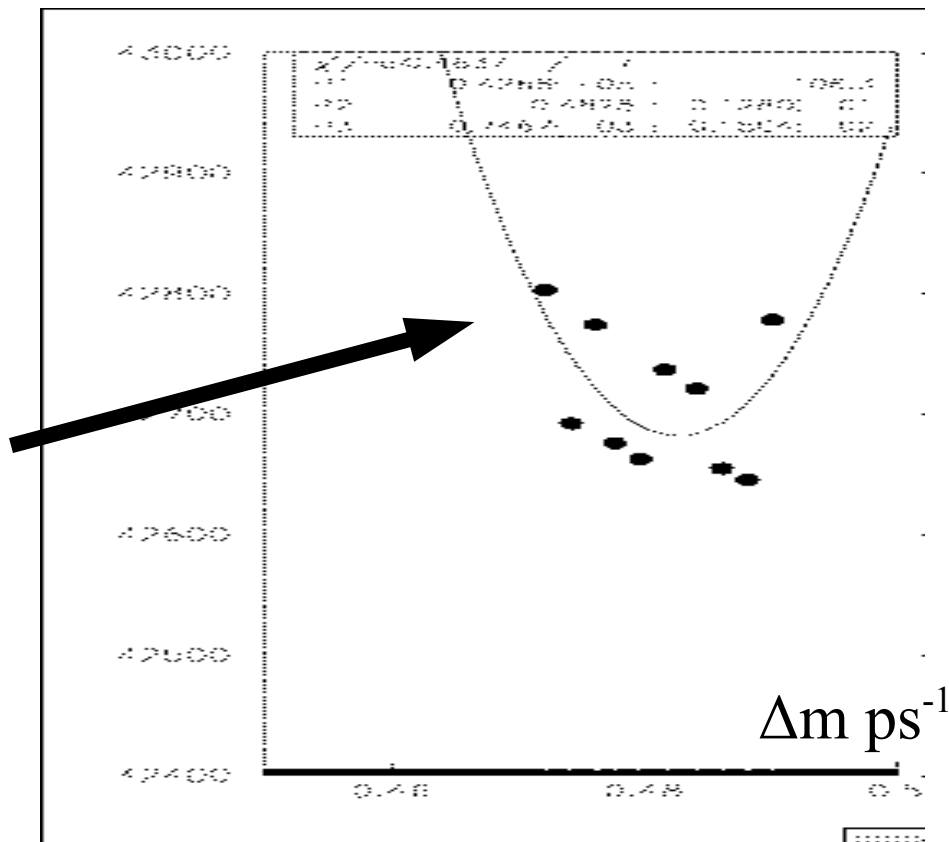
in agreement with Alessandro thesis result

Study of Fit Convergence

- $\log(L)$ shows multiple minima: often the fit does not converge to the absolute minimum (minuit status= FAILED, usually Covariance Matrix not positive defined);
- **$\log(L)$ scan is the solution!**

Scan vs Δm of B^0 MC Signal with measured Δt & tag

In case of problem in the fit convergence, the parabolic fit to the $\log(L)$ profile is BAD.



Definition of Fit Strategy

Recipe to reach the convergence:

- 1) Perform the nominal fit;
in case of convergence problems (often using experimental resolution or Signal+BKG sample):
- 2) **Launch a scan on Gridka** (~10 fits need a few hours \rightarrow a couple of days depending on sample statistics & fit complexity)
- 3) Check if the parabolic fit is good & it gives x_{\min} and σ in good agreement with the nominal fit;
- 4) Otherwise: Launch another scan starting from the parameters corresponding to the lowest minimum of the $\log(L)$ in the previous one;
- 5) **Iteratively reach a good $\log(L)$ profile;**
- 6) Perform the nominal fit starting from the parameters of the best fit of the set;

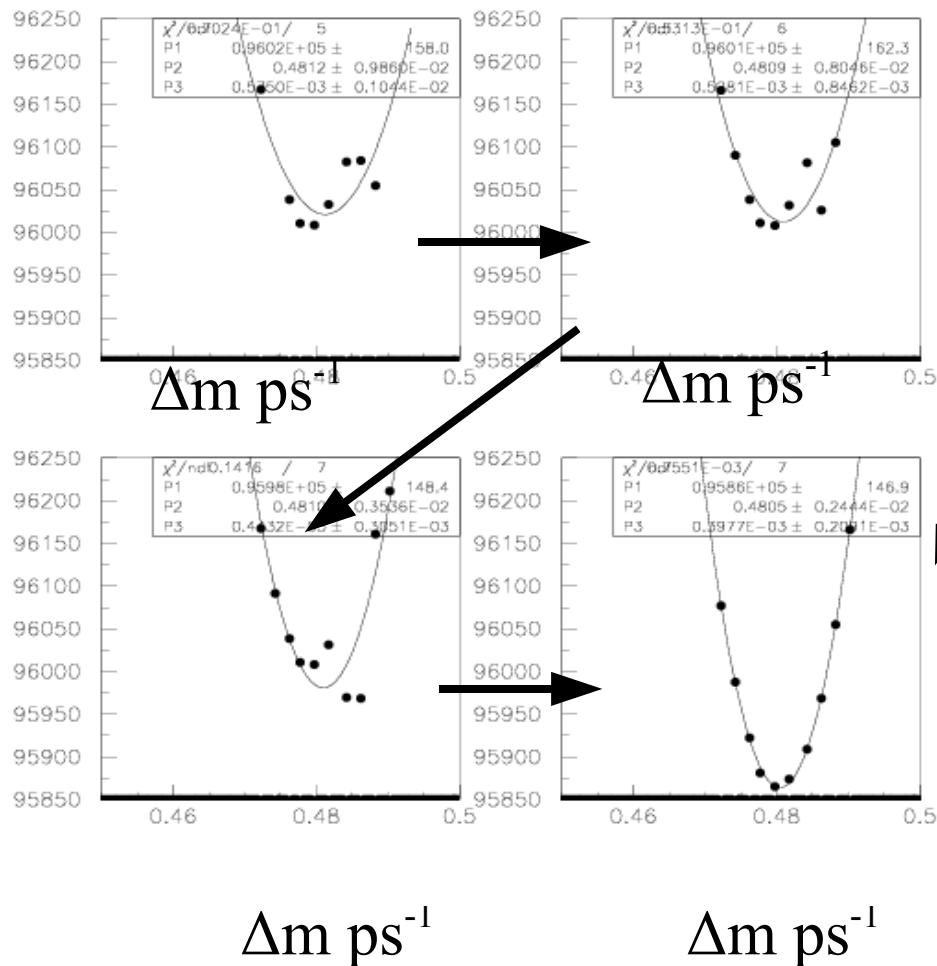


The nominal fit converges!

Fit Strategy

- Example on MC: $\Delta\log(L)$ vs Δm_d :

Signal B^0 B-tag, Exper. Δt + perfect tag:



$$\Delta m = 0.4805 \pm 0.0004 \text{ ps}^{-1}$$

To be compared with the nominal fit result, obtained according to the recipe:

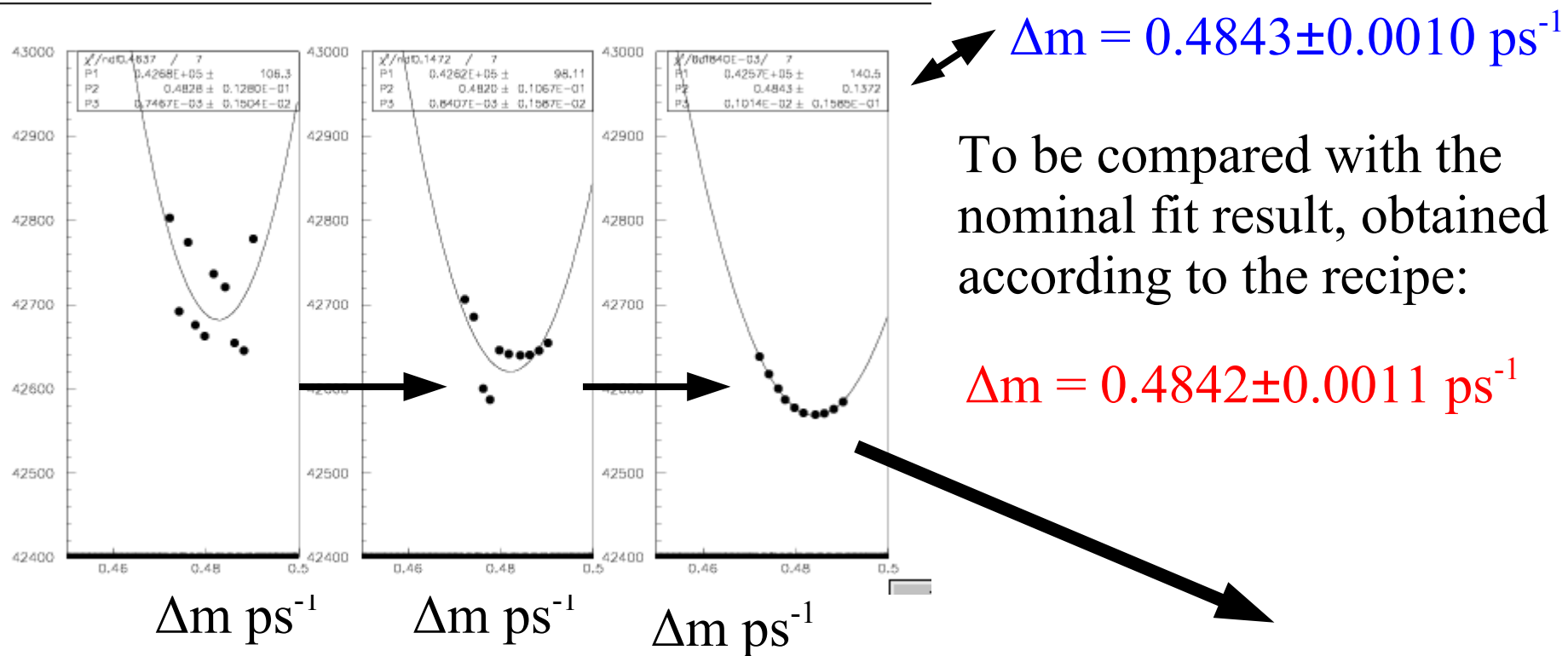
$$\Delta m = 0.4803 \pm 0.0003 \text{ ps}^{-1}$$

Very Good agreement found!

Fit Strategy

- Example on MC: $\Delta\log(L)$ vs Δm_d

Signal B^0 B-tag+D-tag, Exper. Δt and tag:



To be compared with the nominal fit result, obtained according to the recipe:

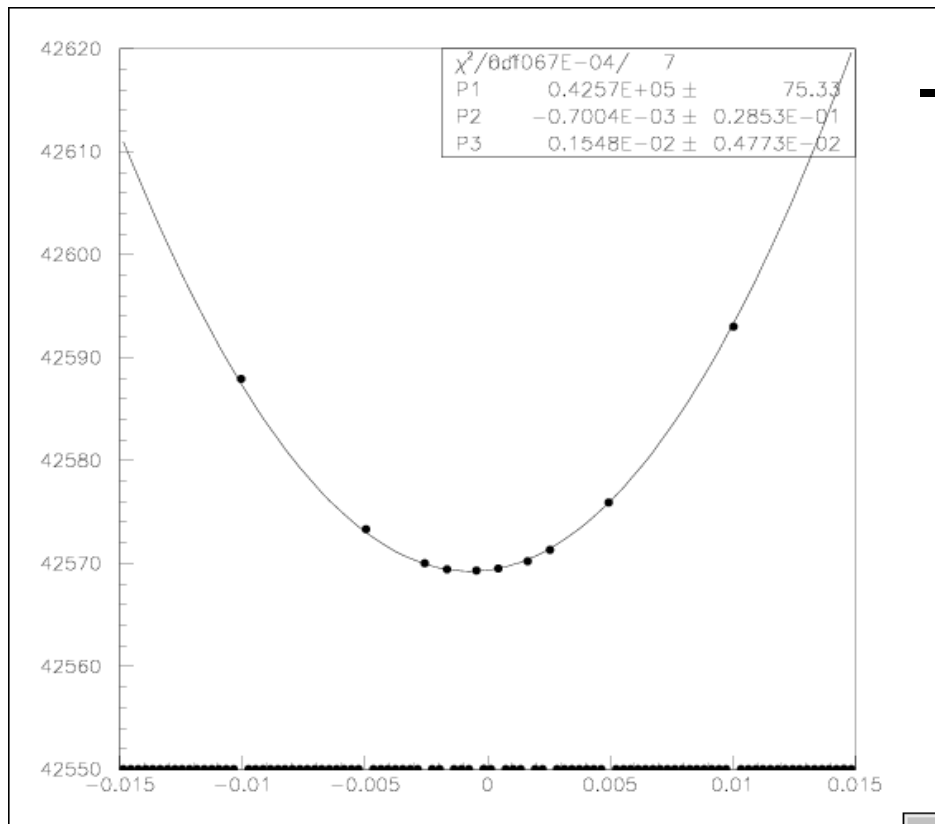
$\Delta m = 0.4842 \pm 0.0011 \text{ ps}^{-1}$

Starting from the minimum of this last scan vs Δm

Fit Strategy

Signal B^0 B-tag+D-tag, Exper. Δt and tag:

.... We got this very nice profile vs $|q/p|-1$



$$|q/p|-1 = -0.0007 \pm 0.0015$$

To be compared with the nominal fit result, obtained according to the recipe:

$$|q/p|-1 = -0.0006 \pm 0.0015$$

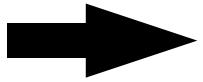
$|q/p|-1$

Fit Strategy

- To reach the absolute minimum usually is very useful to perform likelihood scans over different relevant variables (Δm , q/p , τ , Detector Asymmetries, dilutions)

The Log(L) scan strategy allow us to:

- 1) Reach the convergence at the “true” Log(L) minimum;
- 2) Check the statistical error of the nominal fit.



MC Validation: Fit Bias

- Study the bias on τ , Δm , $|q/p|$ step by step, from MC truth to experimental Δt and tagging. Add one component at a time from pure B^0 signal to full sample composition to see at which level of fit complexity the bias becomes dangerous (if it is the case...).
- Use only CONVERGED fits, obtained by means of the “log(L) Scan” recipe to avoid fit instability effects;

MC-Reference parameters:

$$\tau_{B^0} = 1.540 \text{ ps}$$

$$\chi_d = 0.1809$$

$$\Delta m = 0.489 \text{ ps}^{-1}$$

$$|q/p| - 1 = 0$$

$$b = 0$$

$$c = 0$$

Doubly Cabibbo Suppressed

Bias w.r.t. MC truth

B^0 Btag Signal Fit with Perfect Resolution & tagging:

Δt Bins	:	20	50	100
τ_{B^0}		0.0183 ± 0.0007	-0.0062 ± 0.0006	-0.0095 ± 0.0006
Δm		-0.0159 ± 0.0002	-0.0049 ± 0.0002	-0.0033 ± 0.0002
b		0.0019 ± 0.0004	0.0021 ± 0.0005	0.0021 ± 0.0005
c		0.0000 ± 0.0005	-0.0003 ± 0.0004	-0.0002 ± 0.0004

➔ Use at least 50 Δt bins; 100 Δt bins in the following

$$\text{Fitted } \chi_d = 0.176 \pm 0.0001 \quad 0.1778 \pm 0.0001 \quad 0.1780 \pm 0.0001$$

(in good agreement with $F(\text{mixed}) = 0.1786 \pm 0.0002$)

➔ -0.2% selection bias on $F(\text{mixed})$ (MC truth: $\chi_s = 0.1809$)
Bias of several Statistical Sigmas on τ_{B^0} & Δm , but $< 1\%$.

Bias w.r.t. MC truth

B^0 Btag Signal Fit with Perfect Resolution & exp. tagging:

τ_{B^0}	-0.0098 ± 0.0006	
Δm	-0.0065 ± 0.0005	\longrightarrow Bias $\sim 1.3\%$
b	0.0033 ± 0.0007	
c	0.0007 ± 0.0013	
χ_d	-0.0045 ± 0.0002	

Mistag effect (comparison with previous page result):

τ_{B^0}	-0.0004	
Δm	-0.0032	
b	0.0012	\longrightarrow Experimental (mis)tag is not a problem, biggest effect on Δm
c	0.0009	
χ_d	-0.0016	

Bias w.r.t. MC truth

B^0 Btag Signal Fit with Measured Δt & perfect tagging:

τ_{B0}	-0.0019 ± 0.0011	
Δm	-0.0087 ± 0.0003	→ Bias $\sim 1.8\%$
b	-0.0002 ± 0.0008	
c	0.0044 ± 0.0009	
χ_δ	-0.0044 ± 0.0001	

Resolution effect (comparison w.r.t. Perfect Δt & tagging fit):

τ_{B0}	0.0080	
Δm	-0.0022	
b	-0.0035	→ Experimental Δt resolution is not a problem, biggest effect on τ_{B0}
c	0.0037	
χ_δ	0.0001	

Bias w.r.t. MC truth

B^0 Btag+Dtag Signal Fit with Measured Δt & tagging:

τ_{B^0}	-0.0169 ± 0.0018	\longrightarrow	Bias $\sim 1.1\%$
Δm	-0.0048 ± 0.0011		
b	-0.0004 ± 0.0013	\swarrow	• As already known, due to the Dtag resolution model, we will not be able to measure DCS parameters b, c.
c	-0.0844 ± 0.0019		
χ_d	-0.0049 ± 0.0005		

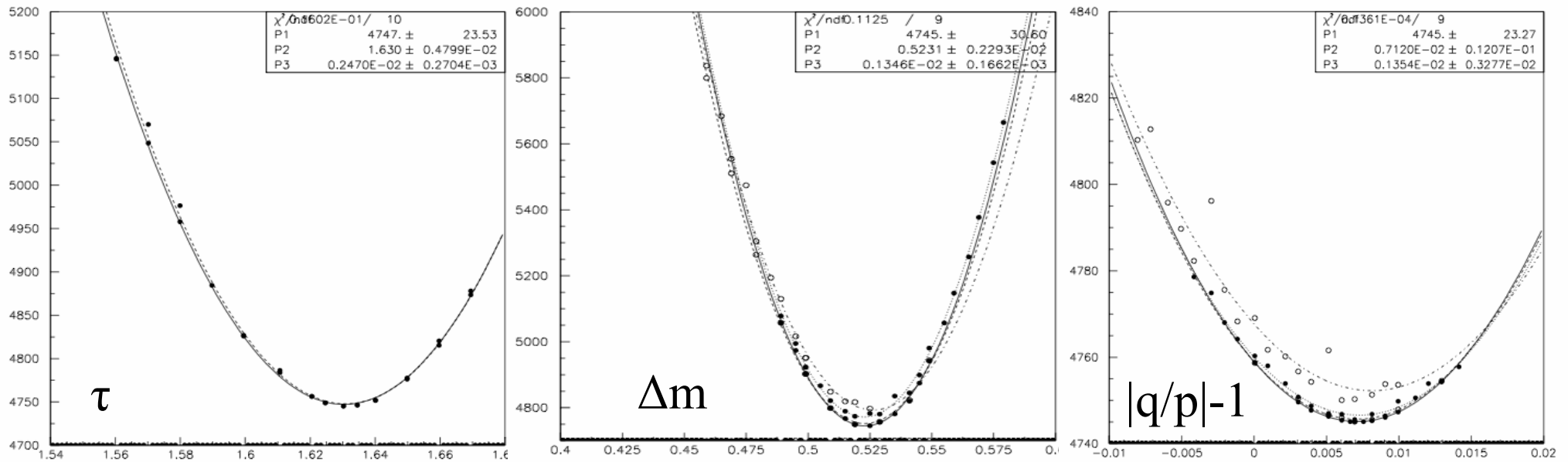
$|q/p|-1$ -0.0006 ± 0.0015

Results on Pure-Signal Monte Carlo:

- τ_{B^0} , Δm show a 1% bias ;
- **NO BIAS on $|q/p|$** (with the “old unbinned” procedure we had already a 0.004 bias on q/p at this level)

B⁰ Combinatorial BKG Study

B-tag+D-tag, measured Δt and tag



$$\tau = 1.630 \pm 0.0025 \text{ ps}; \Delta m = 0.5231 \pm 0.0013 \text{ ps}^{-1}; |q/p|-1 = 0.0071 \pm 0.0014$$

• $\chi_d(\text{BKG}) > \chi_d(\text{SIG})$ (if two B⁰ → D*⁺lv decays in the event, it's possible to pick up lepton & π* from the two different sides with the right charge correlation):

➔ $\tau_{\text{BKG}}, \Delta m_{\text{BKG}}$ just effective parameters;

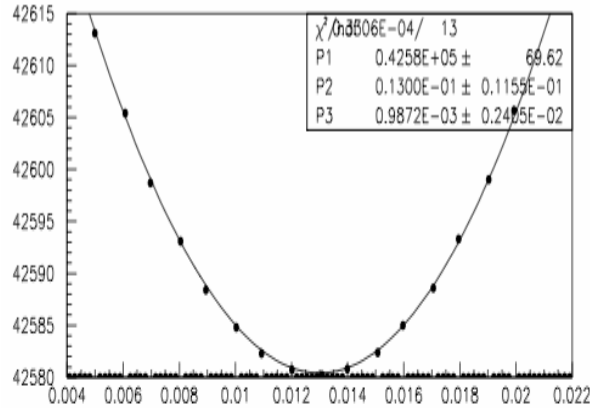
• $|q/p|-1$ shows a strong bias... **PROBLEM?**

• Look at the detector asymmetries to compare SIGNAL vs BKG... 16

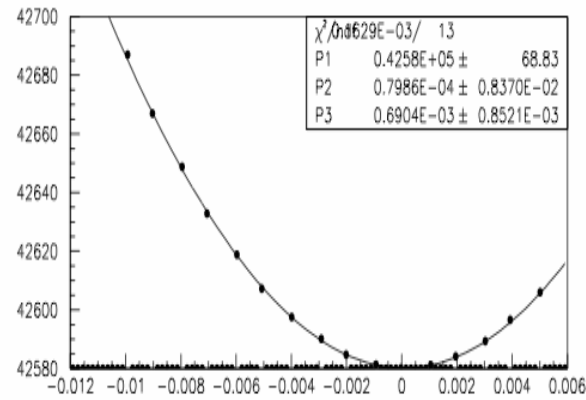
Detector Asymmetries SIG vs BKG

S
I
G
N
A
L

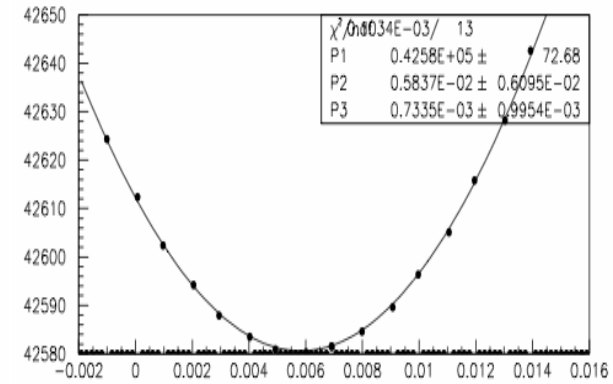
ATAG



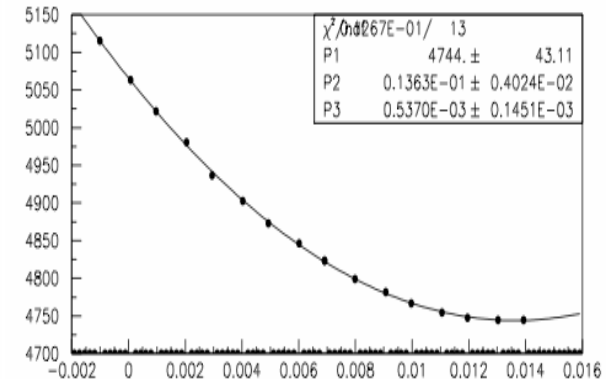
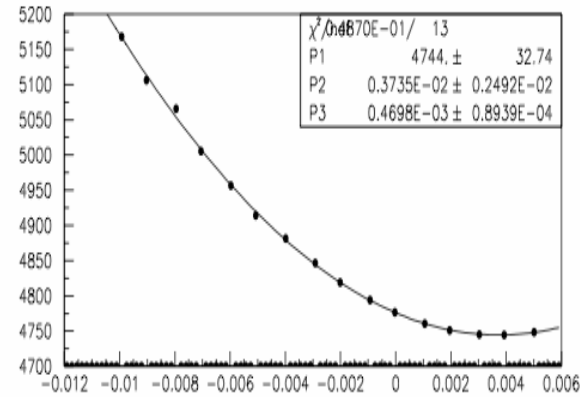
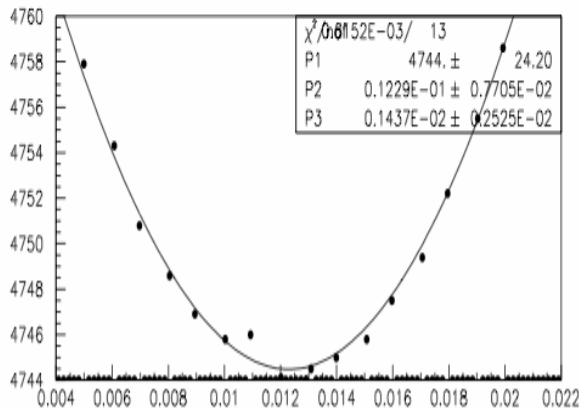
AREC(e)



AREC(μ)



B
K
G



- Atag in good agreement between SIG & BKG;
- Arec(BKG) higher than Arec(SIG)... contradiction w.r.t. our “old fit” results?
- Arec & |q/p| are strongly correlated: maybe the |q/p| bias would be reabsorbed by using common detector asymmetries?

Arec BKG vs SIGNAL from MC counting

SIGNAL

BKG

Electron Sample

A Unm -0.0833229+-0.0384739(%)

A Mix 0.0453182+-0.0820595(%)

A all -0.0601405+-0.0348352(%)

Chi_d 0.1804+-0.000189488

B^0

0.18002+-0.000189219

\bar{B}^0

A Unm -0.113381+-0.0410147(%)

A Mix -0.0121102+-0.0743625(%)

A all -0.0897592+-0.0359142(%)

Chi_d 0.233433+-0.000214947

B^0

0.233071+-0.000214639

\bar{B}^0

Muon Sample

A Unm 0.749731+-0.0463026(%)

A Mix 0.678318+-0.0990136(%)

A all 0.736917+-0.041943(%)

Chi_d 0.179339+-0.000226725

B^0

0.17955+-0.000228507

\bar{B}^0

A Unm 0.768166+-0.0481464(%)

A Mix 0.991979+-0.0882264(%)

A all 0.819524+-0.0422629(%)

Chi_d 0.229861+-0.000250449

B^0

0.229069+-0.000252204

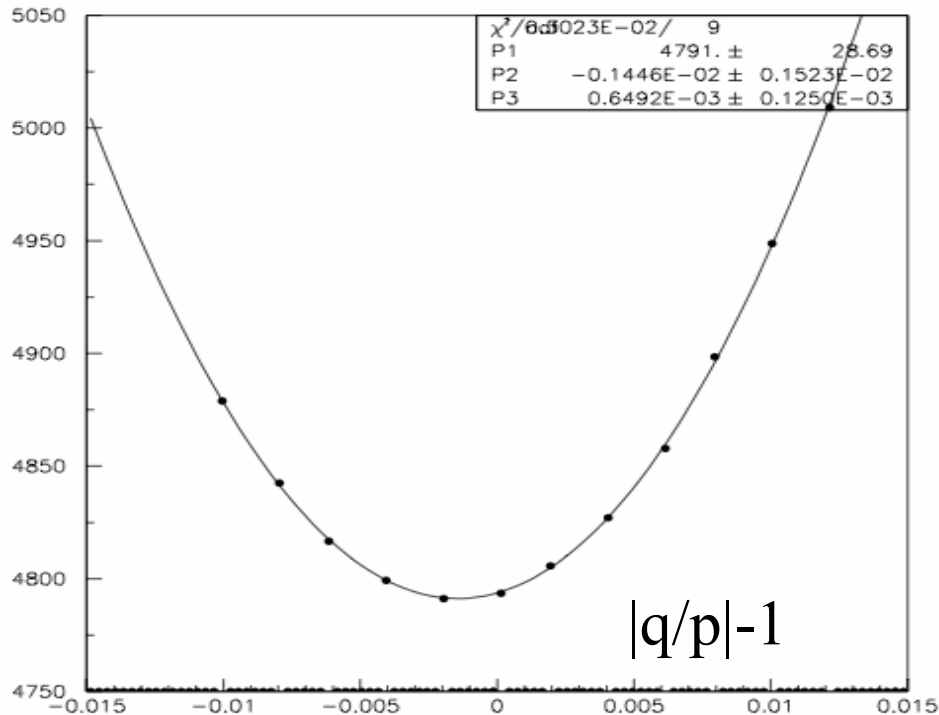
\bar{B}^0

- Good agreement found between SIGNAL and BKG!
- Results in agreement with previous page plots for the SIGNAL FIT!

B⁰ Combinatorial BKG Study

→ CHECK:

Perform a scan on $q/p(\text{BKG})$ by fixing A_{tag} , A_{rec} to the SIGNAL ones:

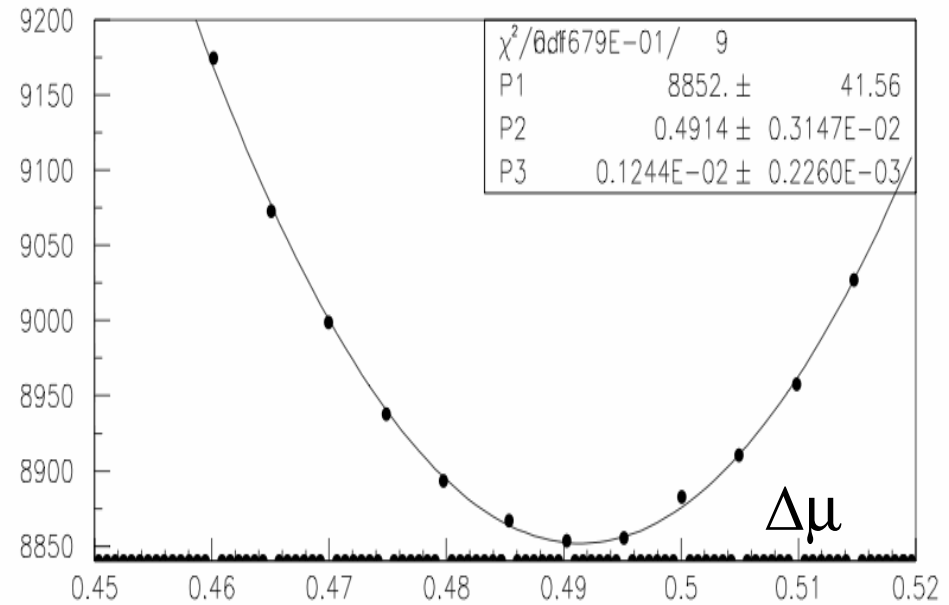
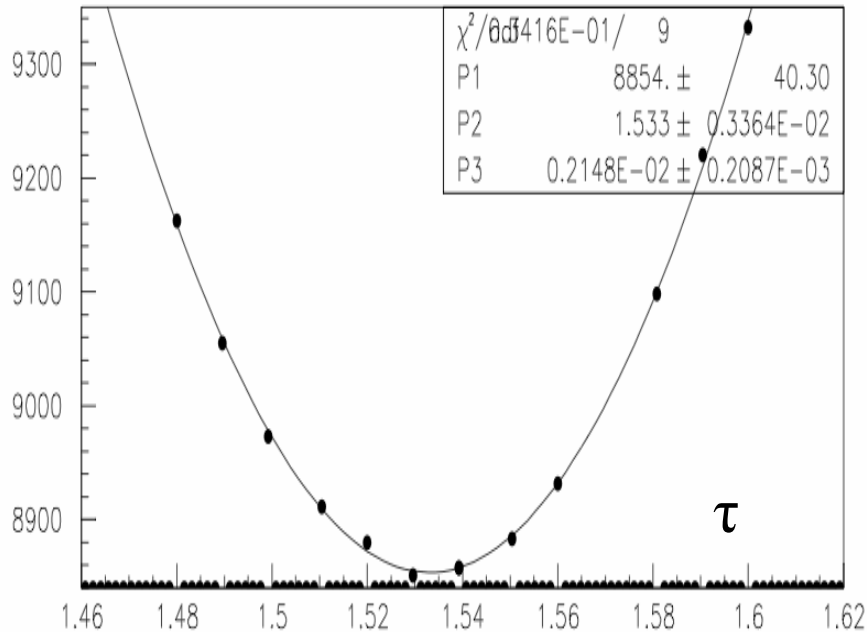


$|q/p|-1 = -0.0014 \pm 0.0006$
bias strongly reduced!

- Compensation between the A_{rec} & $|q/p|-1$ differences in SIGNAL vs BKG !
- Result compatible with sharing common A_{tag} , A_{rec} between SIGNAL & BKG and negligible $|q/p|$ bias...

B⁰ SIGNAL+BKG Results

- Scan performed by using common Atag & Arec for SIGNAL & BKG



Results on B⁰ Monte Carlo:

$$\tau_{B^0} = 1.5330 \pm 0.0021$$

$$\Delta m = 0.4914 \pm 0.0012$$

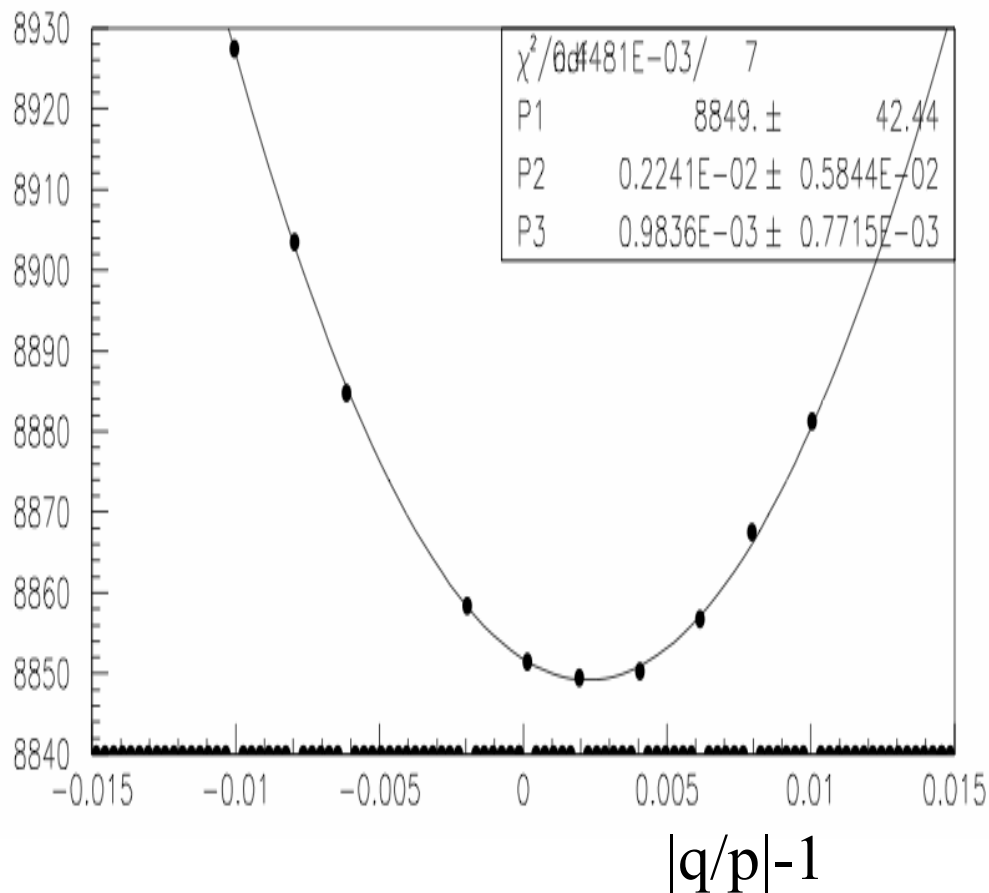
$$\delta\tau = -0.0070 \pm 0.0021$$

$$\delta\Delta m = 0.0024 \pm 0.0012$$

**0.5% bias
on both!**

Let's wait for the Full MC sample result to decide if we want to measure them

B^0 SIGNAL+BKG Results



$\rightarrow |q/p|-1 = 0.0022 \pm 0.0010$

$|q/p|$ bias still at the level of one statistical sigma of real data RUN1-RUN5 result.

Conclusion & Next Steps

- Strategy to reach the fit convergence & evaluate the analysis bias finalized;
- Scan on the Full MC statistics with all the BKG included already started;
- BLIND Scan on the RUN1-RUN5 real data statistics under way;
- Enrico Feltresi is working on the development of a Toy MC for the result validation;
- We still hope to be in time for Summer Conferences: Franco is going to begin to write the Conference Paper;