

**B^0 Lifetime and Mixing with
partially reconstructed D^*lv and**

Lepton Tag

IHBD Meeting

May 9, 2003

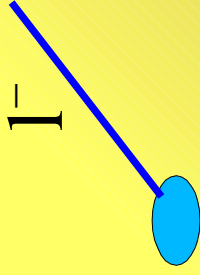
M.Margoni, F.Simonetto

Analysis Strategy

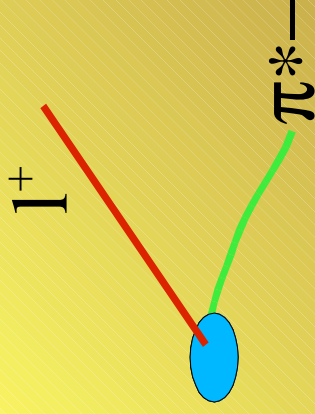
Signal Vertex: $l\pi^*$ + beam spot (x,y)

Tag Vertex: l (Elbatag) + beam spot (x,y)

Tag Side



Signal Side



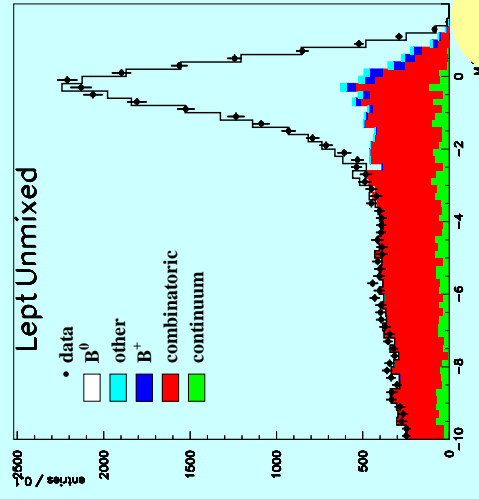
* Fit to Δz distribution to determine simultaneously Δm , τ and dilution constrained to the inclusive fraction of mixed events χ_d

Lepton Tag Sample

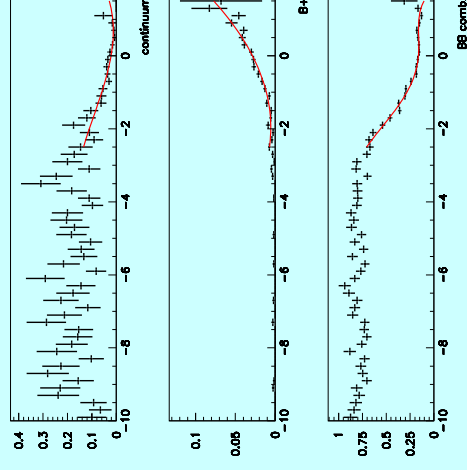
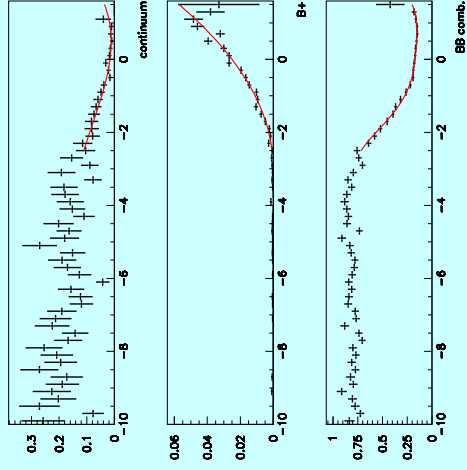
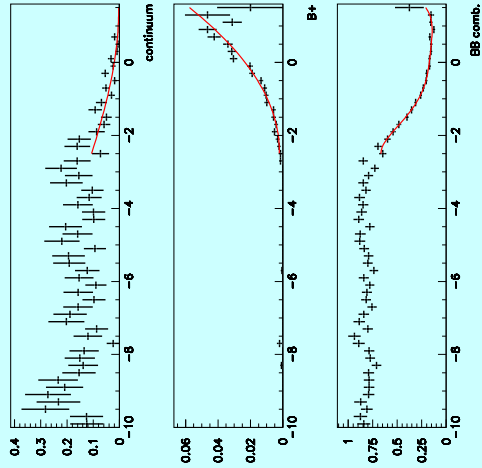
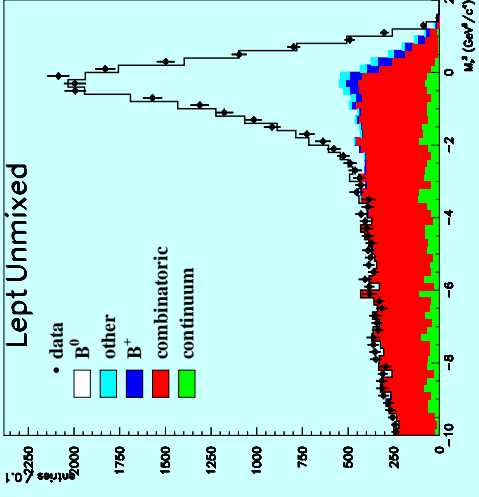
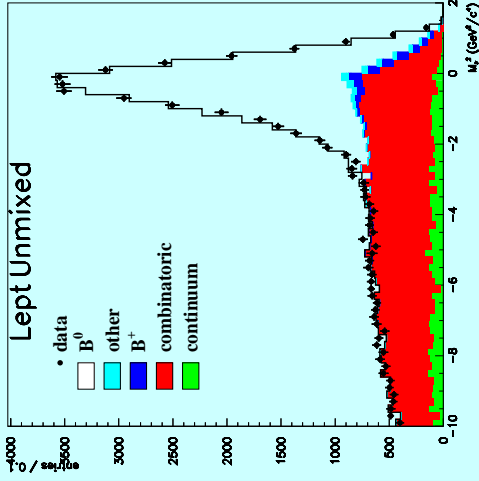
2000

2001

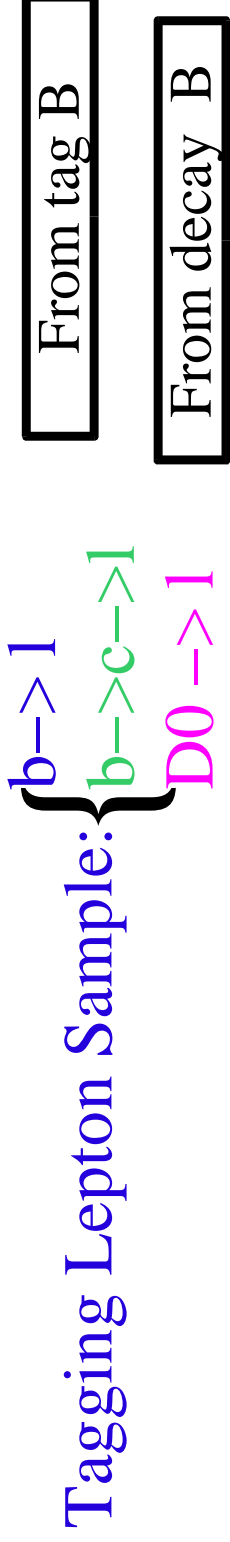
2002



m_ν^2



The Signal PDF



Resulting PDF:

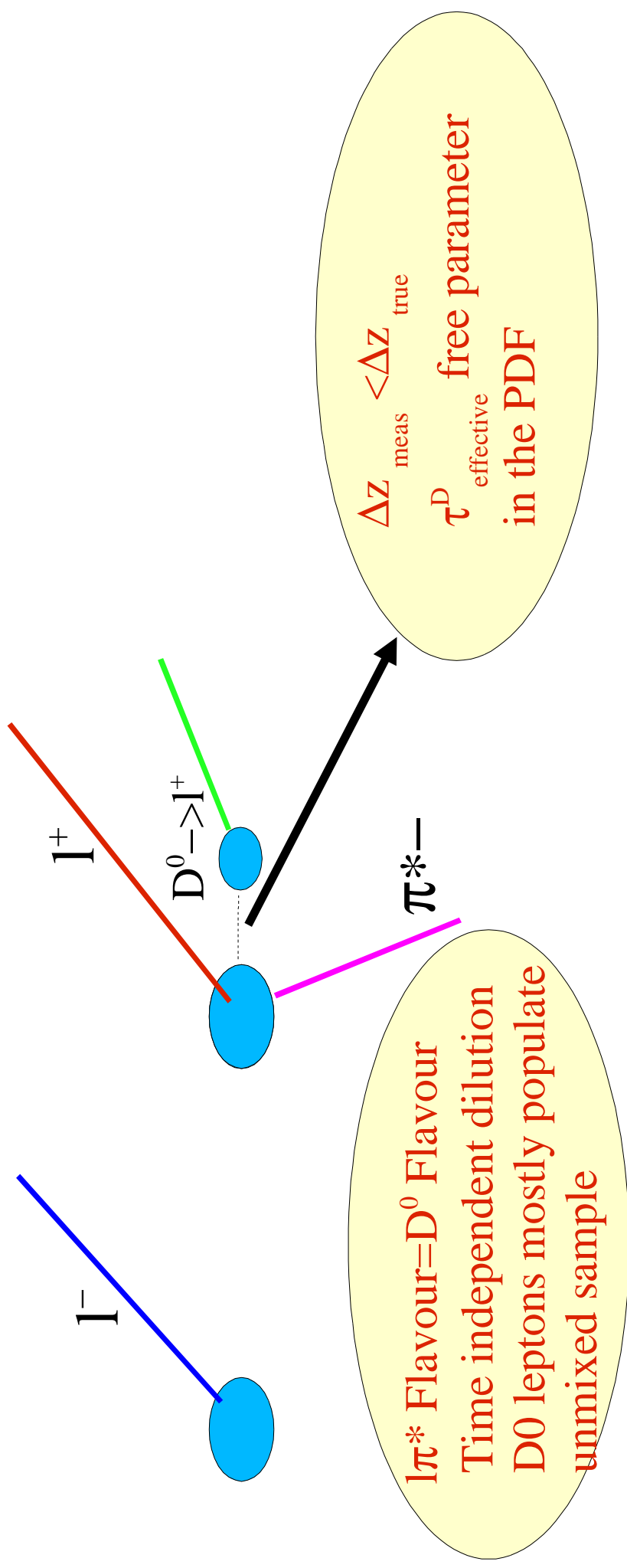
$$\begin{aligned}
 f^{\pm}(\Delta t; \tau_B; \Delta m; \dots) = & \\
 & \Gamma_B / 2 \exp(-\Gamma_B |\Delta t|) * (1 - \alpha) / 2 * [F_{b \rightarrow l} (1 \pm D_{b \rightarrow l} \cos(\Delta m \Delta t)) + \\
 & + F_{b \rightarrow c \rightarrow l} (1 \pm D_{b \rightarrow c \rightarrow l} \cos(\Delta m \Delta t))] \\
 & + \Gamma_D / 2 \exp(-\Gamma_D |\Delta t|) * \begin{cases} \alpha(1 - \rho) \\ \alpha \rho \end{cases}
 \end{aligned}$$

Tag Side Composition 1

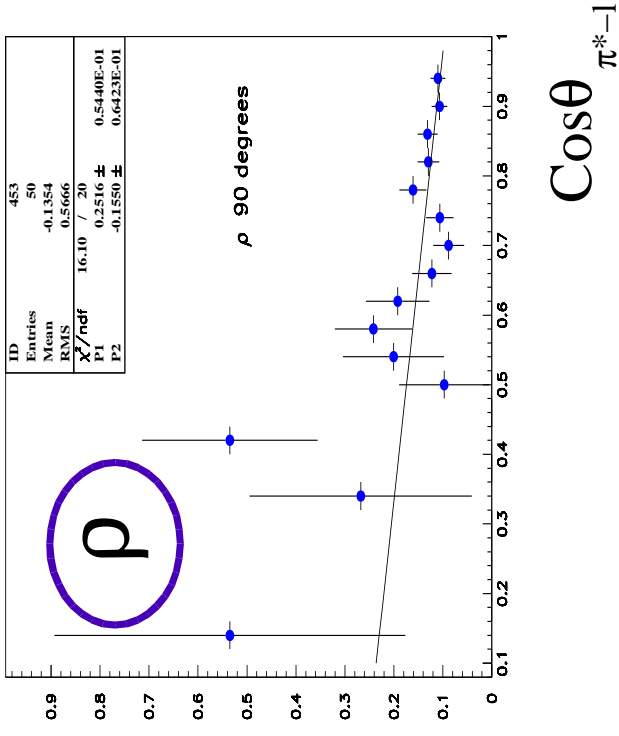
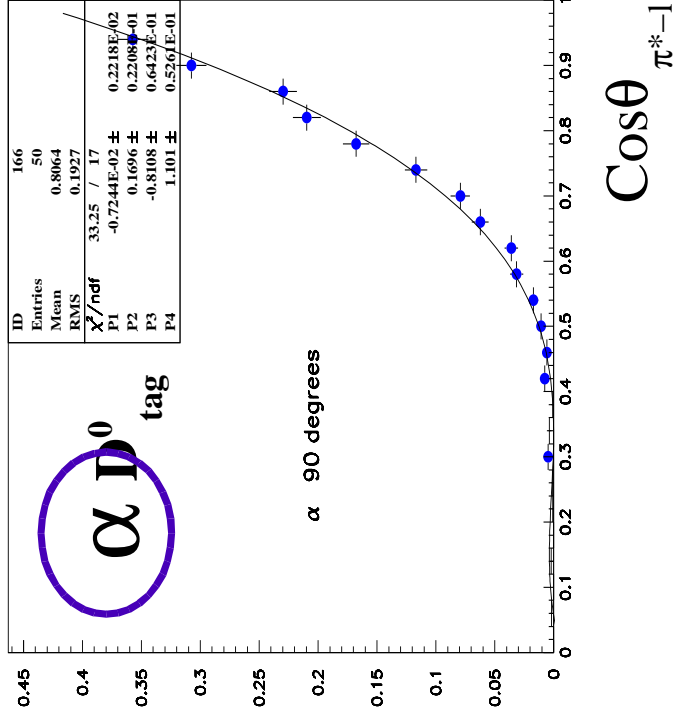
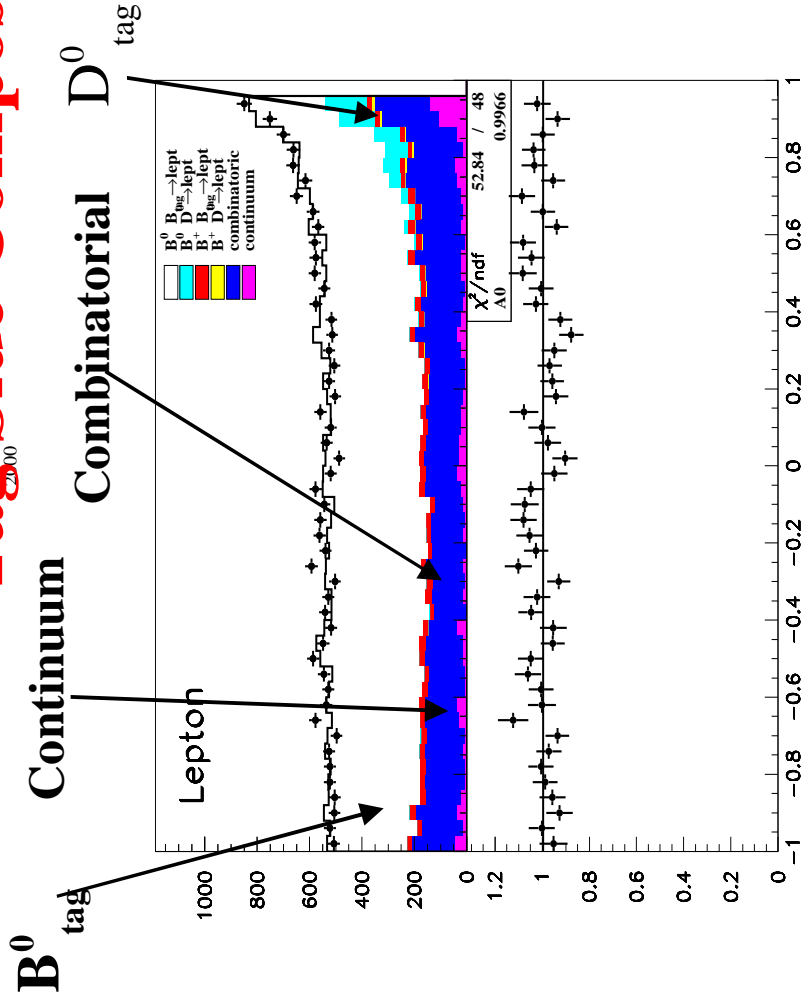
Lepton from D^0 (Signal Vertex) affects the Tag-Side

Signal Side

Tag Side



Tag Side Composition 2



$$\alpha(\text{Cos}\theta_{\pi^{*-1}}) = ND_{\text{tag}}/N_{\text{tag}}$$

$$\rho(\text{Cos}\theta_{\pi^{*-1}}) = (NM_{\text{mixed}}/N_{\text{tot}})_{D_{\text{tag}}}$$

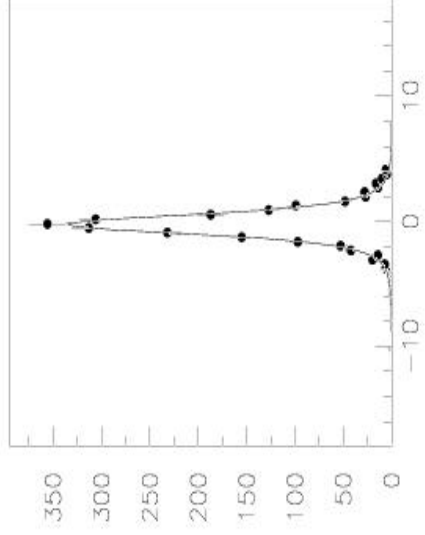
Expressed in terms of $\text{Cos}\theta_{\pi^{*-1}}$ to disentangle

B_{tag} from D_{tag} components

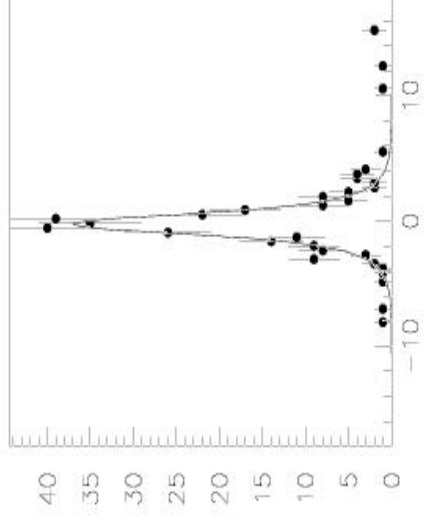
Signal Vertex: $D^0 \rightarrow l$ Description

- Dtag PDF: $\tau \otimes 2G$
- Free parameters: effective τ_{D^0} , bias

Unmixed

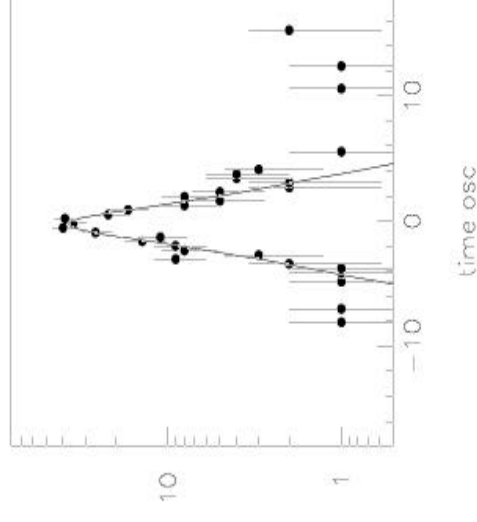
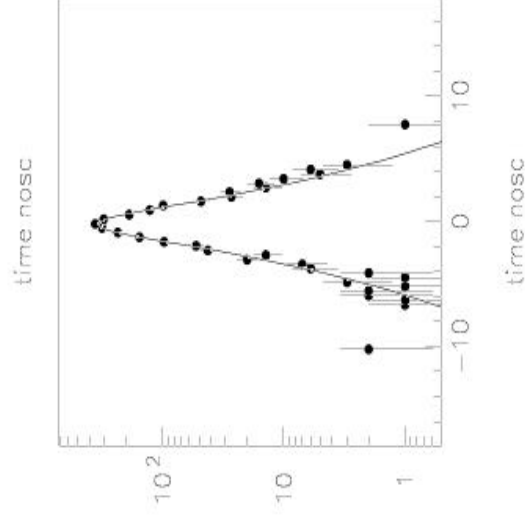


Mixed



MC 2000

$\tau_{D^0} = 0.316 \pm 0.022$ ps
bias = -0.233 ± 0.019 ps



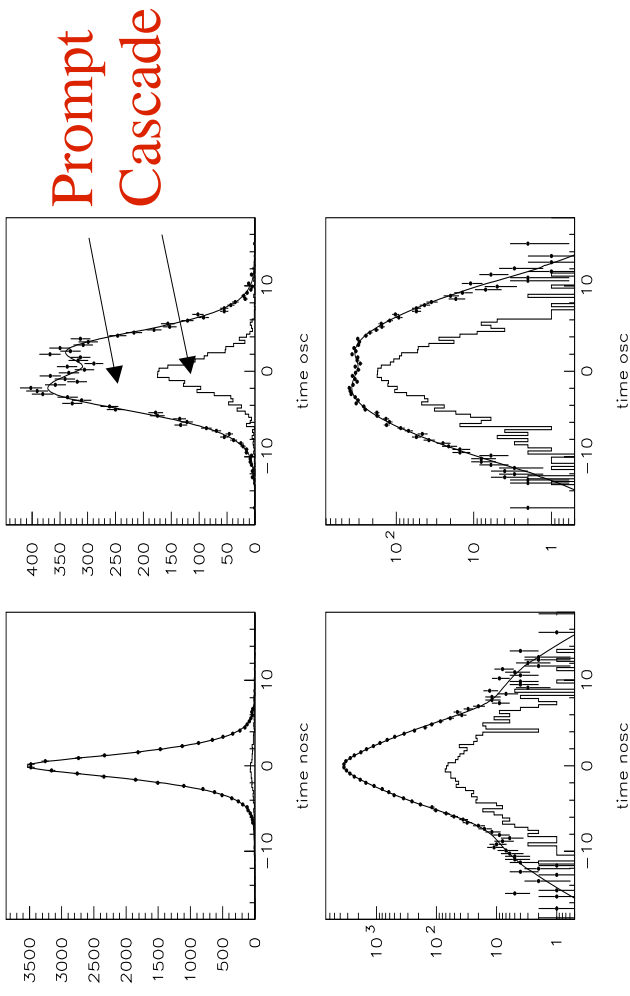
Tag Vertex: $b \rightarrow l / b \rightarrow c \rightarrow l$ Description

Unmixed

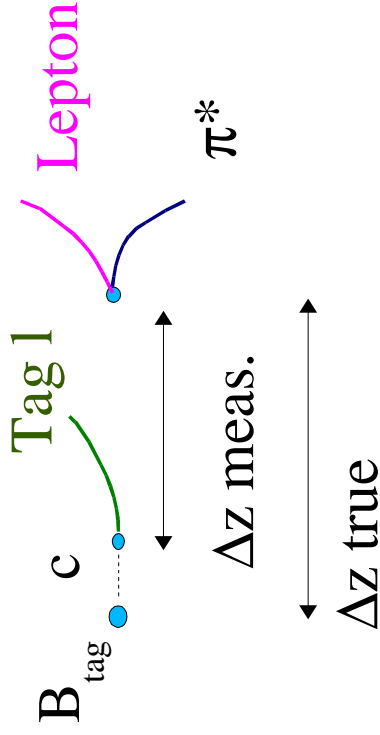
Mixed

MC 2000

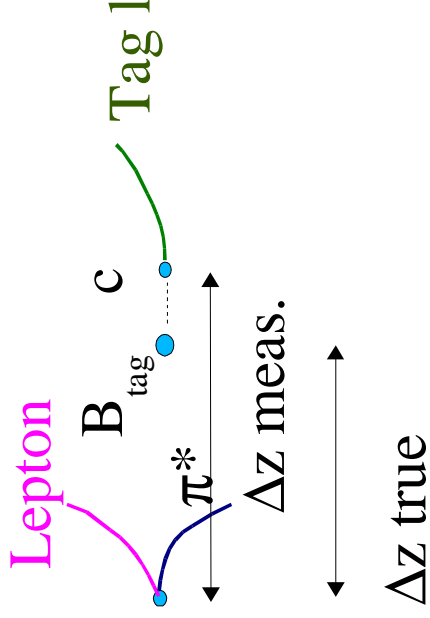
- Separate treatment of the prompt and cascade lepton samples: same pulls, different biases (~ 0 for $b \rightarrow l$) and dilutions.
- Cascade fraction ($\sim 7\%$) from external fit to Lepton Momentum (up to now fixed from MC)



$$\Delta Z = Z_{\text{reco}} - Z_{\text{tag}}$$



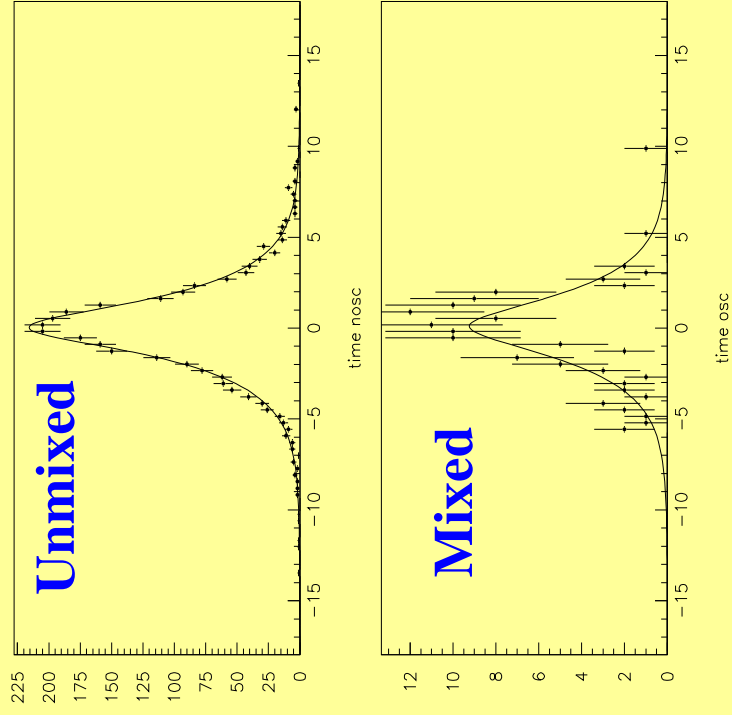
If $\Delta Z > 0$: $\Delta Z_{\text{meas}} < \Delta Z_{\text{true}}$



If $\Delta Z < 0$: $|\Delta Z_{\text{meas}}| > |\Delta Z_{\text{true}}|$

Fit to resonant B^+

2000 MC



PDF

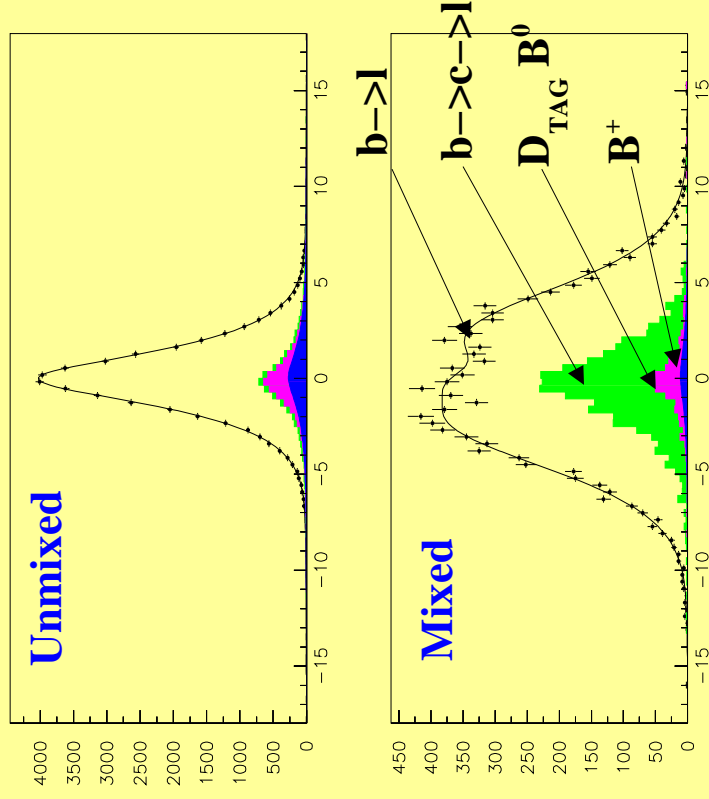
pure lifetime term \otimes resolution
resolution: same as for signal B^0 ,
with separate biases for
narrow and wide gaussians

Free parameters:
– two biases

α^+, ρ^+ vs $\cos\theta$
taken from MC

Fit to signal B^0 + resonant B^+

2000 MC



- B^+ lifetime fixed to 1.65ps
 - B^+ fraction constrained ($\sigma=50\%$) to MC estimation
 - α^+ , ρ^+ vs $\cos\theta$ calculated from MC
- Free parameters:
- signal B^0 resolution function params
 - two biases in B^+ resolution function, same pulls as for B^0 resolution

2000 MC

Results

$\tau_B = 1.5379 \pm 0.0069$ ps

$\Delta m_d = 0.4683 \pm 0.0050$ ps $^{-1}$

$D_{b \rightarrow l} = 0.9823 \pm 0.0032$

$D_{b \rightarrow c \rightarrow l} = -0.663 \pm 0.087$

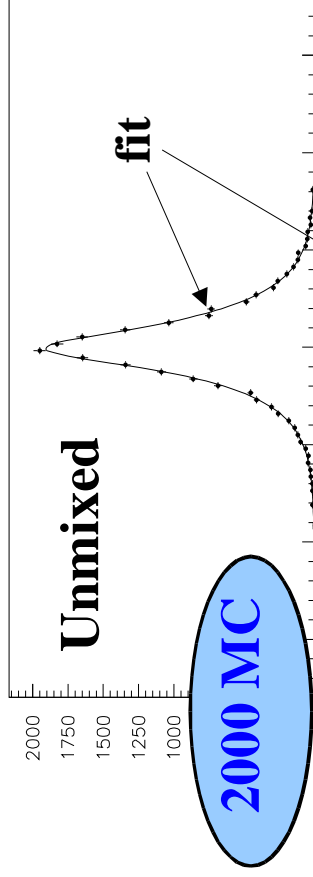
$\tau_D = 0.423 \pm 0.061$ ps

$f_{B^+} = 0.74 \pm 0.32$

$\chi_d = 0.171 \pm 0.003$

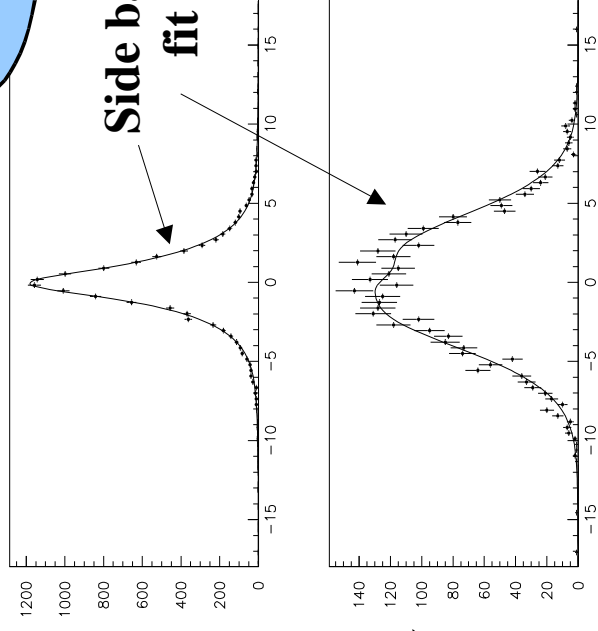
Combinatorial background

$B^0 + B^+$ combinatorial (MC)
side band, right charge



$B^0 + B^+$ combinatorial (MC)
mass band, right charge

2000 MC



Compatible shapes

Combinatorial PDF

Empirical parametrization:

- combinatorial B^0
- combinatorial B^+
- B^0 and B^+ fractions are free parameters in the fit

$\mathbf{f}_{\text{BKG}}^B$: (oscill + lifetime) \otimes 3G

$\mathbf{f}_{\text{BKG}}^D$: lifetime \otimes 2G (same bias)

2 lifetimes ($\tau_{\text{unmix}}, \tau_{\text{mix}}$)

$\mathbf{f}_{\text{BKG}}^+$: lifetime \otimes 3G (same resolution params as in $\mathbf{f}_{\text{BKG}}^B$)

\mathbf{f}_D^+ : lifetime \otimes 2G (same resolution params as in $\mathbf{f}_{\text{BKG}}^D$)

1 lifetime only

Unmixed:

Free parameters

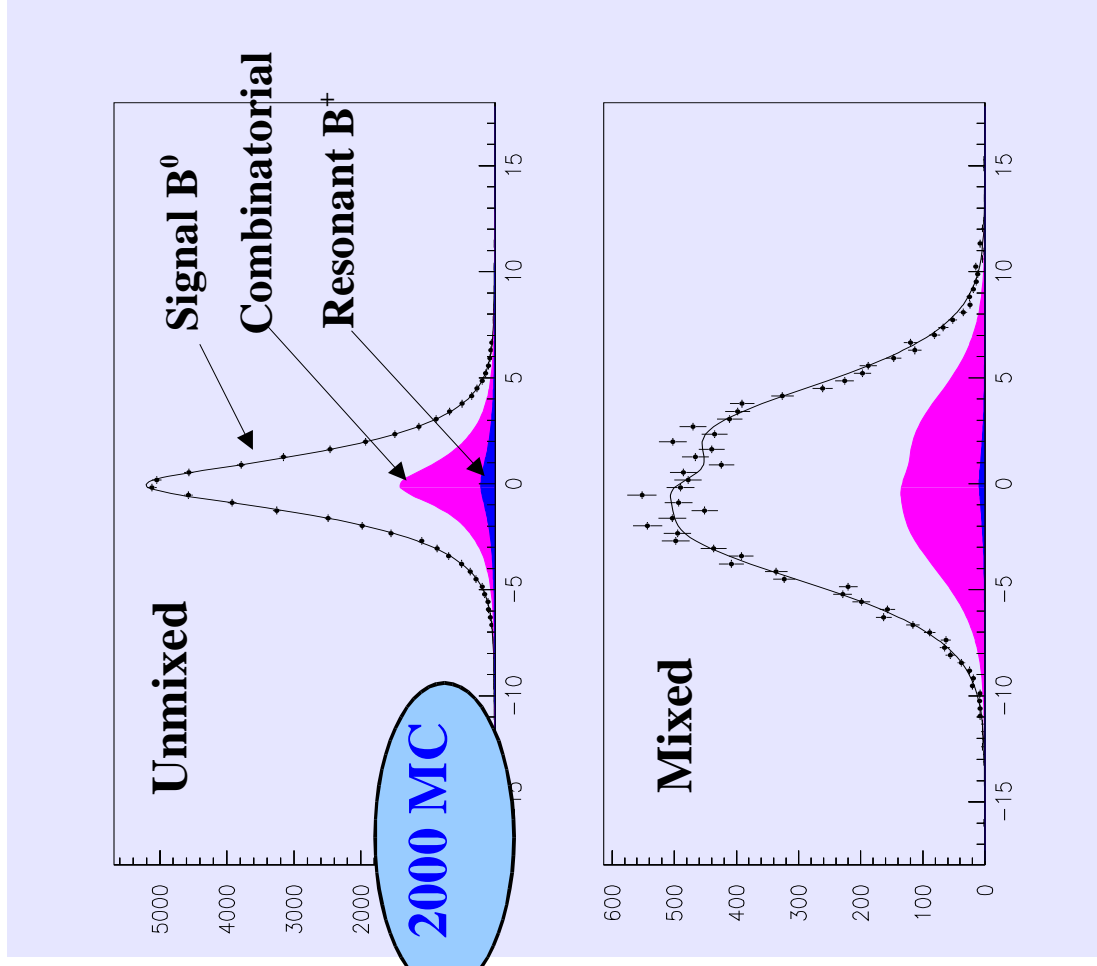
$$\mathbf{f}_{\text{BKG}} = \mathbf{f}_{\text{BKG}}^{B^0} (1 - \alpha_{\text{BKG}}^{B^+}) + \mathbf{f}_{\text{BKG}}^{B^+} \alpha_{\text{BKG}}^{B^+} \quad \mathbf{f}_{\text{BKG}}^{B^+} (1 - \rho_{\text{BKG}}^{B^+})$$

$$B^0: \quad \mathbf{f}_{\text{BKG}}^{B^0} = \mathbf{f}_{\text{BKG}}^B (1 - \alpha_{\text{BKG}}^B) + \alpha_{\text{BKG}}^B \mathbf{f}_{\text{BKG}}^D \quad \mathbf{f}_{\text{BKG}}^D (1 - \rho_{\text{BKG}}^D)$$

$$B^+: \quad \mathbf{f}_{\text{BKG}}^{B^+} = \mathbf{f}_{\text{BKG}}^+ (1 - \alpha_{\text{BKG}}^+) + \alpha_{\text{BKG}}^+ \mathbf{f}_D^+ \quad \mathbf{f}_D^+ (1 - \rho_{\text{BKG}}^+)$$

Signal + background MC fit

Combinatorial parameters fixed
from side-band fit



$$\tau_B = 1.5447 \pm 0.0086 \text{ ps}$$

$$\Delta m_d = 0.4661 \pm 0.0063 \text{ ps}^{-1}$$

to be compared with the
pure-signal fit result:

$$\tau_B = 1.5379 \pm 0.0069 \text{ ps}$$

$$\Delta m_d = 0.4683 \pm 0.0050 \text{ ps}^{-1}$$

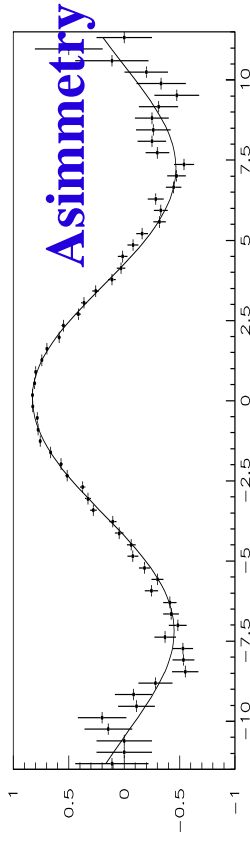
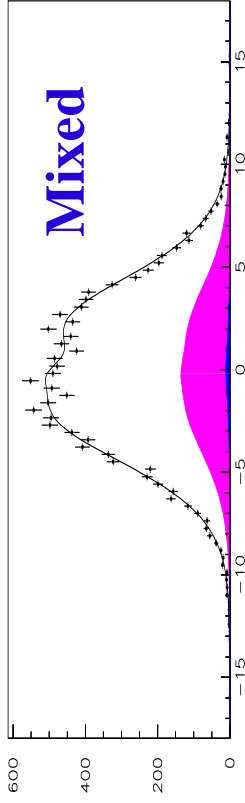
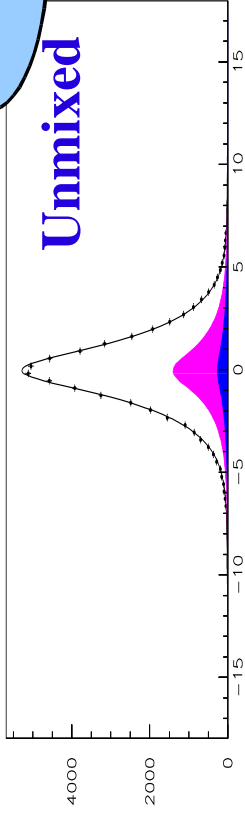


$$\Delta(\tau_B) = 0.0068 \pm 0.0051 \text{ ps}$$

$$\Delta(\Delta m_d) = -0.0022 \pm 0.0038 \text{ ps}^{-1}$$

New approach: Systematics from combinatorial BKG absorbed in the statistical error by means of a simultaneous side-band fit

2000 MC



Preliminary

$$\begin{aligned}\tau_B &= 1.5426 \pm 0.0058 \text{ ps} \\ \Delta m_d &= 0.4657 \pm 0.0042 \text{ ps}^{-1} \\ \chi_d &= 0.170 \pm 0.002\end{aligned}$$

to be compared with the old-approach result:

$$\begin{aligned}\tau_B &= 1.5447 \pm 0.0086 \text{ ps} \\ \Delta m_d &= 0.4661 \pm 0.0063 \text{ ps}^{-1} \\ \chi_d &= 0.171 \pm 0.004\end{aligned}$$

$$(P_{ij}) = \begin{matrix} \Delta m_{\text{sig}} & \tau_{\text{sig}} \\ \Delta m_{\text{BKG}} & -0.23 \\ \tau_{\text{BKG}} & -0.55 \end{matrix}$$

Statistical errors significantly lowered due to strong anticorrelations arising between signal/BKG parameters

Conclusions and Next Steps

- * **MC fit finalized:**
 - Separate description of prompt and cascade leptons
 - Dtag fraction from $\cos\theta_{\pi^*l}$ fit
 - Dtag PDF described in terms of an effective τ_D
 - B^+ PDF described by a pure lifetime term
 - B^+ fraction constrained to m^2v fit result
 - Combinatorial PDF from simultaneous fit to the side-band right charge sample
 - χ_d constraint from the fraction of mixed events

* **Given the available luminosity (Run1+Run2) we expect:**

$$\sigma_{\text{stat}}(\tau_B) \sim 0.005 \text{ ps}$$

$$\sigma_{\text{stat}}(\Delta m) \sim 0.004 \text{ ps}^{-1}$$

$$\Delta m: -0.005 \text{ ps}^{-1} \text{ (Boost Approximation Bias)}$$

- * **Next Steps:**
 - **Year by year stability**
 - **Real Data Analysis**