Is there evidence for a peak in this data?







"Observation of an Exotic S=+1

Baryon in Exclusive Photoproduction from the Deuteron" S. Stepanyan et al, CLAS Collab, Phys.Rev.Lett. 91 (2003) 252001

"The statistical significance of the peak is 5.2 \pm 0.6 σ "

Is there evidence for a peak in this data?



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"A Bayesian analysis of pentaquark signals from CLAS data"
D. G. Ireland et al, CLAS Collab, Phys. Rev. Lett. 100, 052001 (2008)
"The In(RE) value for g2a (-0.408) indicates weak evidence in favour of the data model without a peak in the spectrum."

Comment on "Bayesian Analysis of Pentaquark Signals from ₃ CLAS Data" Bob Cousins, http://arxiv.org/abs/0807.1330

p-values and Discovery

Louis Lyons IC and Oxford I.lyons@physics.ox.ac.uk

Padova,

May 2010

PARADOX

Histogram with 100 bins Fit 1 parameter S_{min} : χ^2 with NDF = 99 (Expected $\chi^2 = 99 \pm 14$)

For our data, $S_{min}(p_0) = 90$ Is p_1 acceptable if $S(p_1) = 115$?

1) YES. Very acceptable χ^2 probability 2) NO. $\sigma_p \text{ from } S(p_0 + \sigma_p) = S_{\min} + 1 = 91$ But $S(p_1) - S(p_0) = 25$ So p_1 is 5 σ away from best value



Louis LYONS

OUNP-99-12



CONCLUSION FOR THIS RASE COMPARING HI: $\dot{p} = J_1$ d H2: $\dot{p} = \dot{p}_2$ Declair Depends on $\Delta \chi^2$

7



Frenesste works according to HI (+ star flucta)
Try fitting according to HI or to H2
$$\chi_1^2$$
 χ_2^2

Look at dist of
$$\chi_1^2$$
 As expected for NDF=100
 χ_1^2 Bit bigger Many #
"satisfactory"
 $\chi_3^2 - \chi_1^2$ Decision based on AX²
has much better forest
Referet for events generated according to H 2
Look at dist of χ_1^2
 $\chi_2^2 - \chi_1^2$
 $\chi_1^2 - \chi_1^2$
 $\chi_1^2 < 130$

24 6

8





Comparing data with different hypotheses



p-values and Discovery

Louis Lyons IC and Oxford I.lyons@physics.ox.ac.uk

Technion,

Feb 2010



on

Statistical Issues for LHC Physics

CERN Geneva June 27-29, 2007

This Workshop will address statistical topics relevant for LHC Physics adyses. Issues related to discovery, and the associated problems arising from systematic uncertainties, will feature prominently.

> Contacts Louis Lyons Albert De Roeck Albert.de.Roeck@cern.ch

Conference secretary Dorothée Denise Dorothee.Denise@cern.ch

Further information and registration at http://cern.ch/phystat-lhc



Discoveries H0 or H0 v H1 p-values: For Gaussian, Poisson and multi-variate data Goodness of Fit tests Why 5σ ? **Blind analyses** What is p good for? Errors of 1st and 2nd kind What a p-value is not $P(\text{theory}|\text{data}) \neq P(\text{data}|\text{theory})$ Optimising for discovery and exclusion Incorporating nuisance parameters

DISCOVERIES

"Recent" history:					
Charm	SLAC, BNL	1974			
Tau lepton	SLAC	1977			
Bottom	FNAL	1977			
W,Z	CERN	1983			
Тор	FNAL	1995			
{Pentaquarks	~Everywhere	2002 }			
?	FNAL/CERN	2010?			

? = Higgs, SUSY, q and I substructure, extra dimensions, free q/monopoles, technicolour, 4th generation, black holes,.....

QUESTION: How to distinguish discoveries from fluctuations?

Penta-quarks?

Hypothesis testing: New particle or statistical fluctuation?



H0 or H0 versus H1?

H0 = null hypothesis

e.g. Standard Model, with nothing new H1 = specific New Physics e.g. Higgs with $M_H = 120 \text{ GeV}$ H0: "Goodness of Fit" e.g. χ^2 , p-values H0 v H1: "Hypothesis Testing" e.g. \mathcal{L} -ratio Measures how much data favours one hypothesis wrt other

H0 v H1 likely to be more sensitive



Testing H0:

Do we have an alternative in mind?

1) Data is number (of observed events) "H1" usually gives larger number (smaller number of events if looking for oscillations) 2) Data = distribution. Calculate χ^2 . Agreement between data and theory gives $\chi^2 \sim ndf$ Any deviations give large χ^2 So test is independent of alternative? Counter-example: Cheating undergraduate 3) Data = number or distribution Use \mathcal{L} -ratio as test statistic for calculating p-value 4) H0 = Standard Model

p-values

Concept of pdf Example: Gaussian



y

y = probability density for measurement x

y =
$$1/(\sqrt{(2\pi)\sigma}) \exp\{-0.5*(x-\mu)^2/\sigma^2\}$$

p-value: probablity that $x \ge x_0$

Gives probability of "extreme" values of data (in interesting direction)

$(x_0-\mu)/\sigma$	1	2	3	4	5
p	16%	2.3%	0.13%	0.003%	0.3*10-6

i.e. Small p = unexpected

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p-values, contd

Assumes: Gaussian pdf (no long tails) Data is unbiassed σ is correct If so, Gaussian x → uniform p-distribution

(Events at large x give small p)



0 $p \rightarrow 1_{19}$

p-values for non-Gaussian distributions

e.g. Poisson counting experiment, bgd = bP(n) = $e^{-b} * b^{n}/n!$



For n=7, p = Prob(at least 7 events) = $P(7) + P(8) + P(9) + \dots = 0.03$

Poisson p-values

n = integer, so p has discrete values So p distribution cannot be uniform Replace Prob $\{p \le p_0\} = p_0$, for continuous p by Prob $\{p \le p_0\} \le p_0$, for discrete p (equality for possible p_0)

p-values often converted into equivalent Gaussian σ e.g. 3*10⁻⁷ is "5 σ " (one-sided Gaussian tail) Does NOT imply that pdf = Gaussian

Significance

Significance = S/\sqrt{B} ?

Potential Problems:

•Uncertainty in B

•Non-Gaussian behaviour of Poisson, especially in tail

•Number of bins in histogram, no. of other histograms [FDR]

- •Choice of cuts (Blind analyses)
- •Choice of bins (.....)

For future experiments:

• Optimising S/\sqrt{B} could give S =0.1, B = 10⁻⁶

Look Elsewhere Effect

See 'peak' in bin of histogram

- p-value is chance of fluctuation at least as significant as observed under null hypothesis
- 1) at the position observed in the data; or
- 2) anywhere in that histogram; or
- 3) including other relevant histograms for your analysis; or
- 4) including other analyses in Collaboration; or
- 5) anywhere in HEP.

Penta-quarks?

Hypothesis testing: New particle or statistical fluctuation?



Goodness of Fit Tests

Data = individual points, histogram, multi-dimensional, multi-channel

 χ^2 and number of degrees of freedom $\Delta\chi^2$ (or *lnL*-ratio): Looking for a peak Unbinned \mathcal{L}_{max} ? Kolmogorov-Smirnov Zech energy test Combining p-values

Lots of different methods. Software available from: http://www.ge.infn.it/statisticaltoolkit

χ^2 with v degrees of freedom?

1) v = data - free parameters ?
Why asymptotic (apart from Poisson → Gaussian) ?
a) Fit flatish histogram with v = N {1 + 10⁻⁶ exp{-0.5(x-x₀)²} x₀ = free param

b) Neutrino oscillations: almost degenerate parameters

$$y \sim 1 - A \sin^2(1.27 \Delta m^2 L/E)$$
 2 parameters

 $\rightarrow 1 - A (1.27 \Delta m^2 L/E)^2 = 1 \text{ parameter}$

Small Δm^2

χ^2 with v degrees of freedom?

2) Is difference in χ^2 distributed as χ^2 ? H0 is true.

Also fit with H1 with k extra params

e. g. Look for Gaussian peak on top of smooth background

 $y = C(x) + A \exp\{-0.5 ((x-x_0)/\sigma)^2\}$

Is $\chi^2_{H0} - \chi^2_{H1}$ distributed as χ^2 with $\nu = k = 3$?

Relevant for assessing whether enhancement in data is just a statistical fluctuation, or something more interesting

N.B. Under H0 (y = C(x)): A=0 (boundary of physical region) x_0 and σ undefined 27

Is difference in χ^2 distributed as χ^2 ?



Is difference in χ^2 distributed as χ^2 ?, contd.

So need to determine the $\Delta \chi^2$ distribution by Monte Carlo

N.B.

- 1) Determining $\Delta \chi^2$ for hypothesis H1 when data is generated according to H0 is not trivial, because there will be lots of local minima
- If we are interested in 5σ significance level, needs lots of MC simulations (or intelligent MC generation)

Unbinned \mathcal{L}_{max} and Goodness of Fit?

Find params by maximising \mathcal{L} So larger \mathcal{L} better than smaller \mathcal{L} So \mathcal{L}_{max} gives Goodness of Fit ??





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† →



Example 1: Exponential distribution

Fit exponential λ to times t_1, t_2, t_3 [Joel Heinrich, CDF 5639] $\mathcal{L} = \prod \lambda e^{-\lambda} t$ $\ln \mathcal{L}_{max}^{i} = -N(1 + \ln t_{av})$ i.e. $\ln \mathcal{L}_{max}$ depends only on AVERAGE t, but is INDEPENDENT OF DISTRIBUTION OF t (except for.....) (Average t is a sufficient statistic)

Variation of \mathcal{L}_{max} in Monte Carlo is due to variations in samples' average t , but NOT TO BETTER OR WORSE FIT

Same average t \implies same \mathcal{L}_{max}





pdf (and likelihood) depends only on $\cos^2\theta_i$

Insensitive to sign of $\cos\theta_i$

So data can be in very bad agreement with expected distribution

e.g. all data with $\cos\theta < 0$, but \mathcal{L}_{max} does not know about it.

Example of general principle

Example 3

Fit to Gaussian with variable $\mu,$ fixed σ

$$p = \frac{1}{\sigma\sqrt{2\pi}} e_{p} - \frac{1}{2} \left(\frac{x - \mu}{\sigma} \right)^{2} \right)$$

$$ln \mathcal{L}_{max} = N(-0.5 \ln 2\pi - \ln \sigma) - 0.5 \Sigma (x_{i} - x_{av})^{2} / \sigma^{2}$$

$$\int (x_{i} - x_{av})^{2} / \sigma^{2} + \frac{1}{\sigma} \int (x_{i} - x_{av})^{2} /$$





Worse fit, larger \mathcal{L}_{max}

Better fit, lower \mathcal{L}_{max}

$\boldsymbol{\mathcal{L}}_{max}$ and Goodness of Fit?

Conclusion:

 \mathcal{L} has sensible properties with respect to parameters NOT with respect to data

 \mathcal{L}_{max} within Monte Carlo peak is NECESSARY not SUFFICIENT

('Necessary' doesn't mean that you have to do it!)

Goodness of Fit: Kolmogorov-Smirnov

Compares data and model cumulative plots Uses largest discrepancy between dists. Model can be analytic or MC sample

Uses individual data points Not so sensitive to deviations in tails (so variants of K-S exist) Not readily extendible to more dimensions Distribution-free conversion to p; depends on n (but not when free parameters involved – needs MC)


Goodness of fit: 'Energy' test

Assign +ve charge to data \leftarrow ; -ve charge to M.C.

Calculate 'electrostatic energy E' of charges

If distributions agree, $E \sim 0$

If distributions don't overlap, E is positive

Assess significance of magnitude of E by MC



N.B.

- 1) Works in many dimensions
- 2) Needs metric for each variable (make variances similar?)
- 3) $E \sim \sum q_i q_j f(\Delta r = |r_i r_j|)$, $f = 1/(\Delta r + \varepsilon)$ or $-\ln(\Delta r + \varepsilon)$

Performance insensitive to choice of small $\boldsymbol{\epsilon}$

See Aslan and Zech's paper at:

http://www.ippp.dur.ac.uk/Workshops/02/statistics/program.shtml

Combining different p-values

Several results quote independent p-values for same effect: $p_1, p_2, p_3...$ e.g. 0.9, 0.001, 0.3 What is combined significance? Not just $p_{1*}p_{2*}p_3...$ If 10 expts each have p ~ 0.5, product ~ 0.001 and is clearly **NOT** correct combined p

$$\begin{split} & \mathsf{S} = z \; * \sum_{j=0}^{n-1} \; (-\ln \; z)^j \, / j! \; , \qquad z = p_1 p_2 p_3 \\ & (\text{e.g. For 2 measurements, } \mathsf{S} = z \; * \; (1 - \textit{lnz}) \geq z \;) \\ & \mathsf{Slight problem: Formula is not associative} \\ & \mathsf{Combining } \{ \mathsf{p}_1 \; \mathsf{and} \; \mathsf{p}_2 \}, \; \mathsf{and then } \mathsf{p}_3 \} \; \mathsf{gives different answe} \\ & \mathsf{from } \{ \mathsf{p}_3 \; \mathsf{and} \; \mathsf{p}_2 \}, \; \mathsf{and then } \mathsf{p}_1 \} \; , \; \mathsf{or all together} \\ & \mathsf{Due to different options for ``more extreme than \; x_1, \; x_2, \; x_3`'. \end{split}$$

Combining different p-values

Conventional: Are set of p-values consistent with H0? SLEUTH: How significant is smallest p?

$$1-S = (1-p_{smallest})^n$$



p₁ →

	p ₁ =	= 0.01	$p_1 = 10^{-4}$		
	p ₂ = 0.01	p ₂ = 1	$p_2 = 10^{-4}$	p ₂ = 1	
Combined S					
Conventional	1.0 10 ⁻³	5.6 10 ⁻²	1.9 10 ⁻⁷	1.0 10 ⁻³	
SLEUTH	2.0 10 ⁻²	2.0 10 ⁻²	2.0 10-4	2.0 10-4	

Example of ambiguity

Combine two tests:

a) $\chi^2 = 80$ for $\nu = 100$

b) $\chi^2 = 20$ for $\nu = 1$

1) b) is just another similar test:

$$\chi^2 = 100 \text{ for } \mathbf{v} = 101$$

ACCEPT

2) b) is very different test
 p₁ is OK, but p₂ is very small. Combine p's
 REJECT

Basic reason for ambiguity

Trying to transform uniform distribution in unit hypercube to uniform one dimensional distribution $(p_{comb} = 0 \rightarrow 1)$

Why 5σ ?

- Past experience with 3σ , 4σ ,... signals
- Look elsewhere effect:

Different cuts to produce data

Different bins (and binning) of this histogram

Different distributions Collaboration did/could look at Defined in SLEUTH

• Bayesian priors:

 $\frac{P(H0|data)}{P(H1|data)} = \frac{P(data|H0) * P(H0)}{P(data|H1) * P(H1)}$ Bayes posteriors
Likelihoods
Priors
Prior for {H0 = S.M.} >>> Prior for {H1 = New Physics}

Why 5σ ?

BEWARE of tails, especially for nuisance parameters

Same criterion for all searches? Single top production Higgs Highly speculative particle Energy non-conservation

BLIND ANALYSES

Why blind analysis? Selections, corrections, method Methods of blinding

Add random number to result * Study procedure with simulation only Look at only first fraction of data Keep the signal box closed Keep MC parameters hidden Keep unknown fraction visible for each bin After analysis is unblinded,

* Luis Alvarez suggestion re "discovery" of free quarks

What is p good for?

Used to test whether data is consistent with H0 Reject H0 if p is small : $p \le \alpha$ (How small?) Sometimes make wrong decision: Reject H0 when H0 is true: Error of 1st kind Should happen at rate α OR Fail to reject H0 when something else Error of 2nd kind (H1,H2,...) is true: Rate at which this happens depends on.....

Errors of 2nd kind: How often?



Error of 1st kind: $\chi^2 \ge 20$ Reject H0 when true

Error of 2nd kind: $\chi^2 \leq 20$ Accept H0 when in fact quadratic or... How often depends on:

- Size of quadratic term
- Magnitude of errors on data, spread in x-values,.....
- How frequently quadratic term is present

Errors of 2nd kind: How often?

e.g. 2. Particle identification (TOF, dE/dx, Čerenkov,.....) Particles are π or μ

Extract p-value for $H0 = \pi$ from PID information



Of particles that have $p \sim 1\%$ ('reject H0'), fraction that are π is

a) ~ half, for equal mixture of π and μ

b) almost all, for "pure" π beam

c) very few, for "pure" μ beam

What is p good for?

Selecting sample of wanted events e.g. kinematic fit to select t<u>t</u> events $t \rightarrow bW, b \rightarrow jj, W \rightarrow \mu\nu \quad \underline{t} \rightarrow \underline{b}W, \underline{b} \rightarrow jj, W \rightarrow jj$ Convert χ^2 from kinematic fit to p-value Choose cut on χ^2 to select t <u>t</u> events Error of 1st kind: Loss of efficiency for t t events Error of 2nd kind: Background from other processes Loose cut (large χ^2_{max} , small p_{min}): Good efficiency, larger bgd Tight cut (small χ^2_{max} , larger p_{min}): Lower efficiency, small bgd Choose cut to optimise analysis:

More signal events: Reduced statistical error More background: Larger systematic error

p-value is not

Does **NOT** measure Prob(H0 is true) i.e. It is **NOT** P(H0|data) It is P(data|H0) N.B. P(H0|data) \neq P(data|H0) P(theory|data) \neq P(data|theory)

"Of all results with $p \le 5\%$, half will turn out to be wrong" N.B. Nothing wrong with this statement

- e.g. 1000 tests of energy conservation
- ~50 should have $p \le 5\%$, and so reject H0 = energy conservation

Of these 50 results, all are likely to be "wrong"

P (Data;Theory) \neq P (Theory;Data)

- Theory = male or female
- Data = pregnant or not pregnant

P (pregnant ; female) ~ 3%

P (Data;Theory) \neq P (Theory;Data)

- Theory = male or female
- Data = pregnant or not pregnant

- P (pregnant ; female) ~ 3% but
- P (female ; pregnant) >>>3%

More and more data

1) Eventually p(data|H0) will be small, even if data and H0 are very similar.

p-value does not tell you how different they are.

- 2) Also, beware of multiple (yearly?) looks at data.
 - "Repeated tests eventually sure to reject H0, independent of value of α "
 - Probably not too serious -
 - < ~10 times per experiment.



Figure 1: P value versus sample size.

More "More and more data"



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OUNP-99-12



CONCLUSION FOR THIS CASE CONPARINE HI: p=1. d H2: p= p2 DECLINA DEFENDS ON DX²

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Choosing between 2 hypotheses

Possible methods:

 $\Delta \chi^2$ p-value of statistic \rightarrow *lnL*-ratio **Bayesian**: Posterior odds Bayes factor Bayes information criterion (BIC) (AIC) Akaike Minimise "cost"



Procedure: Choose α (e.g. 95%, 3σ , 5σ ?) and CL for β (e.g. 95%)

Given b, α determines n_{crit}

s defines β . For $s > s_{min}$, separation of curves \rightarrow discovery or excln $s_{min} =$ Punzi measure of sensitivity For $s \ge s_{min}$, 95% chance of 5 σ discovery Optimise cuts for smallest s_{min}

Now data: If $n_{obs} \ge n_{crit}$, discovery at level α

If $n_{obs} < n_{crit}$, no discovery. If $\beta_{obs} < 1 - CL$, exclude H1

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-			ы	-	-	-

N2 NPL; 06/11/2005

p-values or *L*ikelihood ratio?



£ = height of curve
p = tail area
Different for distributions that

a) have dip in middle
b) are flat over range

Likelihood ratio favoured by Neyman-Pearson lemma (for simple H0, H1)

Use *L*-ratio as statistic, and use p-values for its distributions for H0 and H1

- Think of this as either
- i) p-value method, with \mathcal{L} -ratio as statistic; or
- ii) *L*-ratio method, with p-values as method to assess value of *L*-ratio

Bayes' methods for H0 versus H1



N.B. Frequentists object to this (and some Bayesians object to p-values) Bayes' methods for H0 versus H1

P(H0|data) = P(data|H0) * Prior(H0)P(H1|data) P(data|H1) * Prior(H1) Posterior odds Likelihood ratio Priors e.g. data is mass histogram H0 = smooth background H1 = + peak 1) Profile likelihood ratio also used but not guite Bayesian (Profile = **maximise** wrt parameters. Contrast Bayes which **integrates** wrt parameters) 2) Posterior odds 3) Bayes factor = Posterior odds/Prior ratio (= Likelihood ratio in simple case) 4) In presence of parameters, need to integrate them out, using priors. e.g. peak's mass, width, amplitude Result becomes dependent on prior, and more so than in parameter determination. 5) Bayes information criterion (BIC) tries to avoid priors by

- BIC = $-2 * \ln{\mathcal{L} \text{ ratio}} + k* \ln{n}$ k= free params; n=no. of obs
- 6) Akaike information criterion (AIC) tries to avoid priors by

AIC = $-2 \ln{L \text{ ratio}} + 2k$

Why p ≠ Bayes factor

Measure different things:

p₀ refers just to H0; B₀₁ compares H0 and H1

Depends on amount of data: e.g. Poisson counting expt little data: For H0, $\mu_0 = 1.0$. For H1, $\mu_1 = 10.0$ Observe n = 10 $p_0 \sim 10^{-7}$ $B_{01} \sim 10^{-5}$ Now with 100 times as much data, $\mu_0 = 100.0$ $\mu_1 = 1000.0$ Observe n = 160 $p_0 \sim 10^{-7}$ $B_{01} \sim 10^{+14}$



p₀ versus p₁ plots



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Optimisation for Discovery and Exclusion

Giovanni Punzi, PHYSTAT2003:

"Sensitivity for searches for new signals and its optimisation" http://www.slac.stanford.edu/econf/C030908/proceedings.html Simplest situation: Poisson counting experiment,

Bgd = b, Possible signal = s, n_{obs} counts(More complex:Multivariate data,InL-ratio)

Traditional sensitivity:

Median limit when s=0

Median σ when $s \neq 0$ (averaged over s?)

Punzi criticism: Not most useful criteria

Separate optimisations



Procedure: Choose α (e.g. 95%, 3σ , 5σ ?) and CL for β (e.g. 95%)

Given b, α determines n_{crit}

s defines β . For $s > s_{min}$, separation of curves \rightarrow discovery or excln $s_{min} =$ Punzi measure of sensitivity For $s \ge s_{min}$, 95% chance of 5 σ discovery Optimise cuts for smallest s_{min}

Now data: If $n_{obs} \ge n_{crit}$, discovery at level α

If $n_{obs} < n_{crit}$, no discovery. If $\beta_{obs} < 1 - CL$, exclude H1

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S	id	е	6	3

N1 NPL; 06/11/2005

1) No sensitivity

Data almost always falls in peak

 β as large as 5%, so 5% chance of H1 exclusion even when no sensitivity. (CL_s)

2) Maybe

If data fall above n_{crit} , discovery

Otherwise, and $n_{obs} \rightarrow \beta_{obs}$ small, exclude H1

(95% exclusion is easier than 5σ discovery)

But these may not happen \rightarrow no decision

3) Easy separation

Always gives discovery or exclusion (or both!)

Disc	Excl	1)	2)	3)
No	No			
No	Yes			
Yes	No		(□)	
Yes	Yes			□!

Incorporating systematics in p-values

Simplest version: Observe n events Poisson expectation for background only is $b \pm \sigma_{h}$ $\sigma_{\rm h}$ may come from: acceptance problems jet energy scale detector alignment limited MC or data statistics for backgrounds

theoretical uncertainties

Luc Demortier, "p-values: What they are and how we use them", CDF memo June 2006 http://www-cdfd.fnal.gov/~luc/statistics/cdf0000.ps Includes discussion of several ways of incorporating nuisance parameters **Desiderata:** Uniformity of p-value (averaged over v, or for each v?) p-value increases as σ_{v} increases Generality Maintains power for discovery

Ways to incorporate nuisance params in p-values

- Supremum
- Conditioning
- Prior Predictive

Maximise p over all v. Very conservative

Good, if applicable

Box. Most common in HEP

 $p = \int p(v) \ \pi(v) \ dv$

- Posterior predictive Averages p over posterior
- Plug-in Uses best estimate of v, without error
- *L*-ratio
- Confidence interval Berger and Boos.

 $p = Sup\{p(v)\} + \beta$, where 1- β Conf Int for v

Generalised frequentist Generalised test statistic

Performances compared by Demortier

Summary

- $P(H0|data) \neq P(data|H0)$
- p-value is NOT probability of hypothesis, given data
- Many different Goodness of Fit tests Most need MC for statistic → p-value
- For comparing hypotheses, $\Delta\chi^2$ is better than $\chi^2_{\ 1}$ and $\chi^2_{\ 2}$
- Blind analysis avoids personal choice issues
- Different definitions of sensitivity
- Worry about systematics

PHYSTAT-LHC Workshop at CERN, June 2007 "Statistical issues for LHC Physics Analyses" Proceedings at http://phystat-lhc.web.cern.ch/phystat-lhc/2008-001.pdf₆₈